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Section ~ A

Semester ~ 4<sup>th</sup>

Sub ~ Structure Analysis

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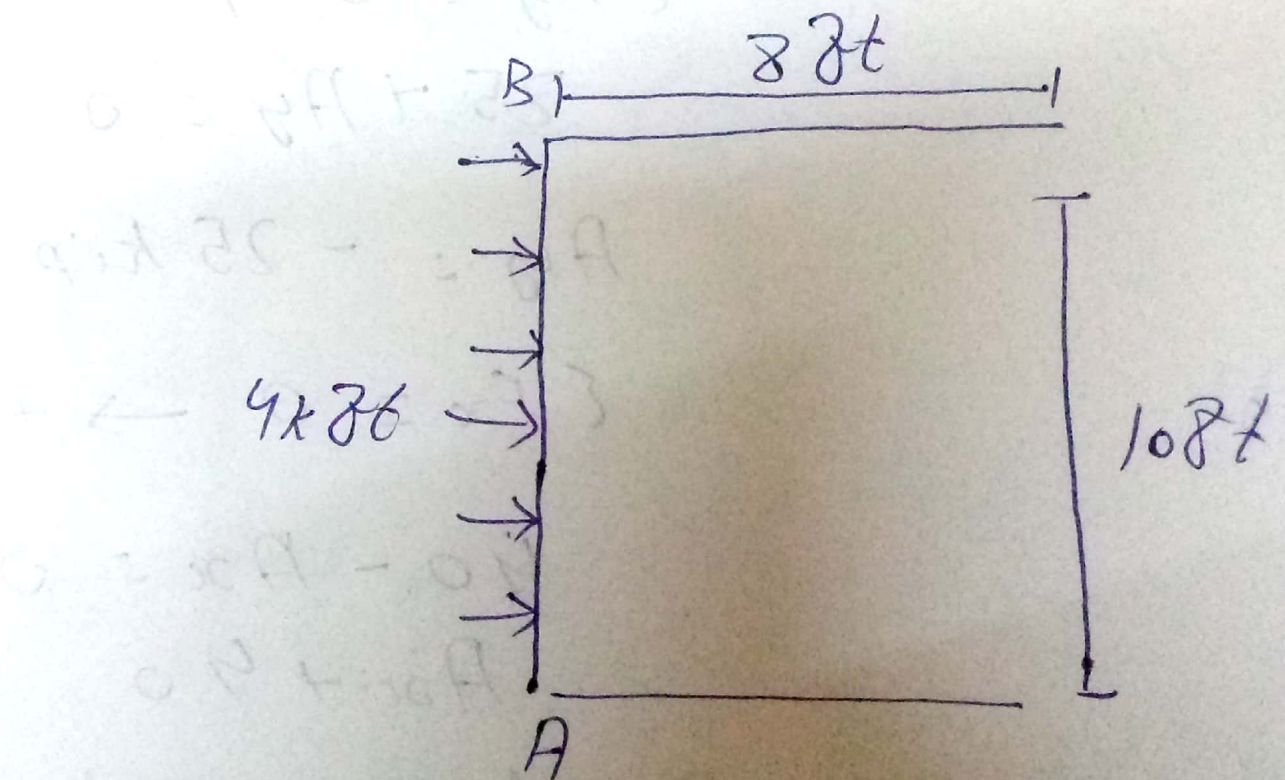
Date ~ 26 jun 2020

# Question No 1

Given data

$$E = 29 (10^3) \text{ ksi}$$

$$I = 600 \text{ in}^4$$



Req<sup>x</sup>

Vertical displacement = ?

Sol<sup>n</sup>

Now vertical moment

For reaction

$$\sum MA = 0$$

$$-4(10)(5) + (4)(8) = 0$$

$$(4) = 25 \text{ kips}$$

$$\sum Fy = 0 \uparrow +$$

$$25 + Ay = 0$$

$$Ay = -25 \text{ kip}$$

$$\sum Fx = 0 \rightarrow +$$

$$40 - Ax = 0$$

$$Ax = +40$$

Real moment;

$$\sum M_1 = 0$$

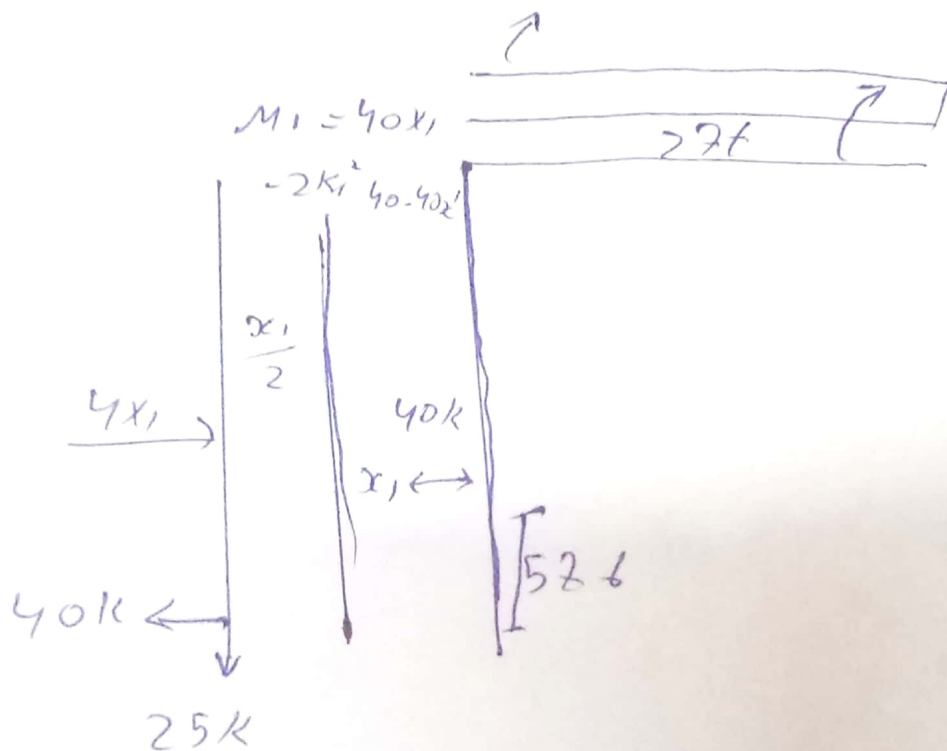
$$-40(x_1) + 4\left(\frac{x_1}{2}\right) + M_1 = 0$$

$$M_1 = 40x_1 - 2x_1^2$$

$$-25x_2 + M_2 = 0$$

$$M_2 - 25x_2 = -25$$

$$M_2 = 25x_2$$



Virtual Moments:

$$\sum m_i = 0$$

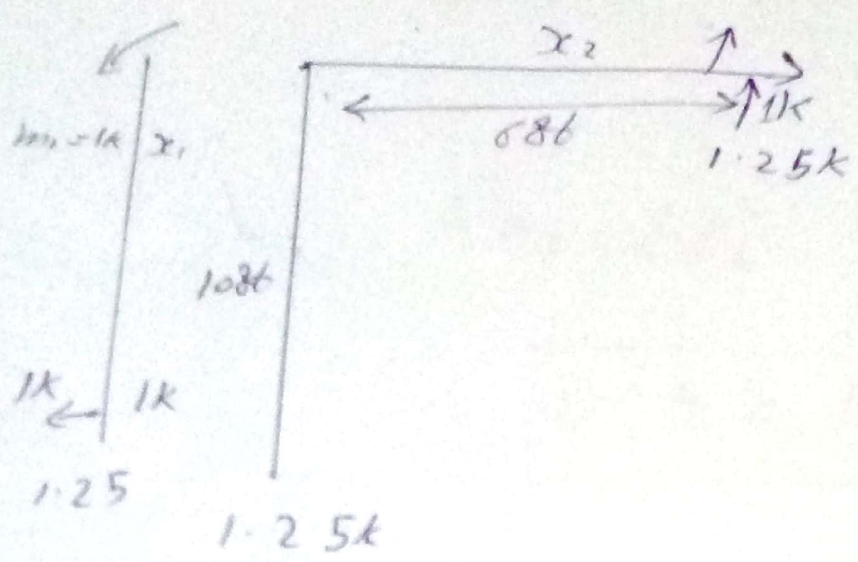
$$-1(x_1) + m_1 = 0$$

$$m_1 = 1x_1$$

$$-m_2 + 1 \cdot 25x_2 = 0$$

$$m_2 = 1 \cdot 25x_2$$

$$m_2 = 1.25k$$



Now from virtual work eq

$$1k \cdot \Delta Ch = \int_0^{108t} m \frac{m dx}{EI}$$

$$1k \cdot \Delta C = \int_0^{108t} \frac{(40x_1 - 2x_1^2)(1x_1) dx}{EI}$$

$$\Delta Ch = \frac{8333.3}{EI} + \frac{5333.3}{EI}$$

$$\Delta Ch = \frac{13666.7 \text{ k}^3 \cdot \text{ft}^3}{EI}$$

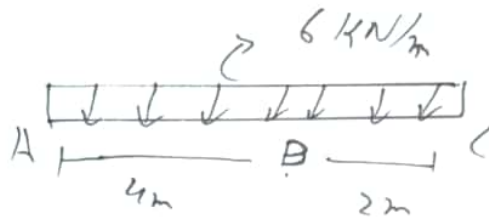
$$\Delta Ch = \frac{1366.7 \text{ k}^2 \cdot \text{ft} (12^3 \cdot 119^3) (12 \text{ft}^3)}{(29 \times 10^6 \text{ k/in}^2) (600)}$$

Results

$$\Delta Ch = 1.35 \text{ Finch}$$

## Question No. 2

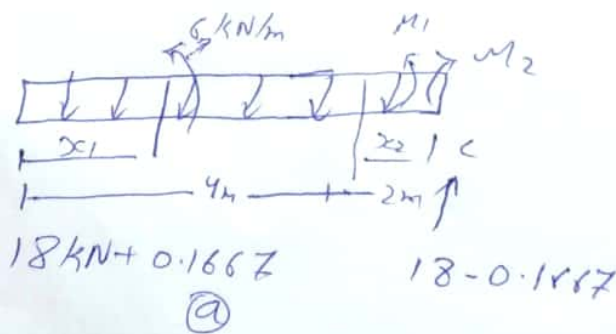
Given data:



Required:

Slope and displacement at point 'B'

Solution:



$$R_1 + R_2 = 0 \quad \text{--- (1)}$$

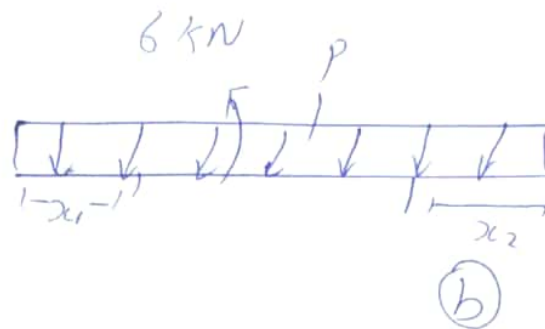
$$\sum M_A = 0 \quad \text{--- (2)}$$

$$1 + R_2(6) = 0$$

$$\Rightarrow -0.16667 \text{ Pub m (2)}$$

$$R_1 + (-0.1667) = 0$$

$$R_1 = 0.1667 \text{ kN}$$



$$R_1 + R_2 = 1$$

$$\sum M_A = 0$$

$$-(11)(9) + R_2(6) = 0$$

$$R_1 = 0.6667 \text{ kN}$$

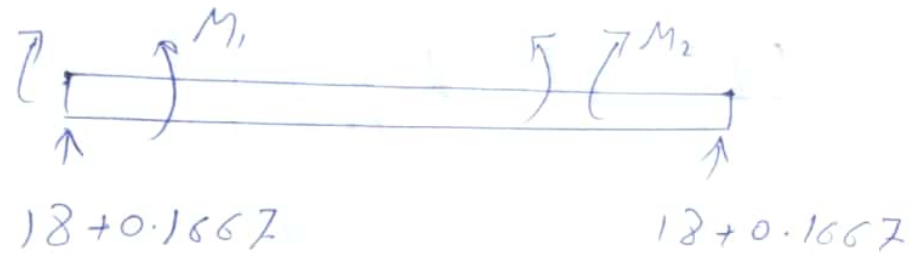
$$R_2 = 1 - 0.6667 \text{ kN}$$

$$R_2 = 0.3333 \text{ kN}$$



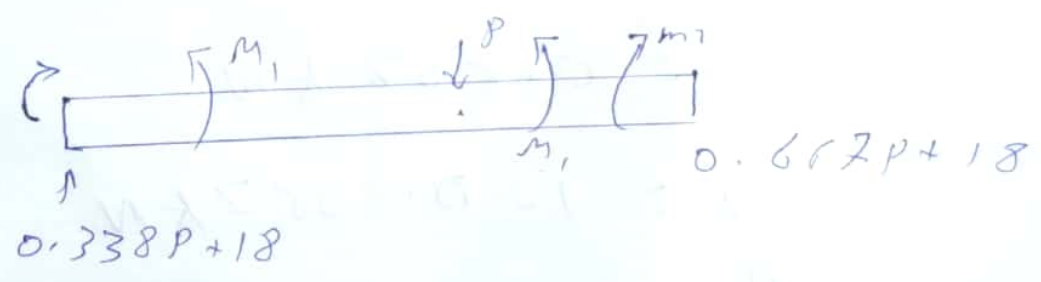
$$M_1 = (18 + 0.1667M')x_1 - 2x_1^2$$

$$M_2 = (18 - 0.1667M')x_2 - 2x_2^2$$



$$M_1 = (0.333P + 18)x_1 - 2x_1^2$$

$$M_2 = (18 - 0.1667M')x_2 - 2x_2^2$$



The displacement function shown in the figure "a" above

$$\frac{\delta M_1}{\delta x_1} = 0.1667x_1, \text{ and } \frac{\delta M_2}{\delta x_2} = 0.1667x_2, \text{ Id.}$$

$$\text{Set } M' = 0$$

$$M_1 = (18 + 0.1667(0))x_1 - 2x_1^2 \quad \text{Id.}$$

$$\rightarrow M_1 = (18x_1 - 2x_1^2)$$

$$M_2 = (18x_2 - 2x_2^2)$$

$$\Theta B = \int_0^2 M \left( \frac{\delta M}{\delta x_1} \right) \frac{dx_1}{EI} = \int_0^2 \frac{(18x_1 - 2x_1^2)}{EI}$$

$$\frac{(0.1667) dx_1}{EI}$$

$$+ \int_0^2 \frac{(18x_2 - 2x_2^2)(0.1667x_2) dx_2}{EI}$$

$$\Theta B = \frac{42.85}{EI} + \frac{6.66}{EI}$$

$$\Theta B = \frac{49.51}{EI}$$

$$\theta_B = \frac{49.31}{(200 \times 10^6)(0.0006)}$$

$$\theta_B = 0.444 \text{ rad}$$

For the displacement function are shown in figure "b"

$$\frac{\delta M_1}{\delta P} = 0.333x_1 \text{ and } \frac{\delta M_2}{\delta P} = 0.6667x_2$$

$$\text{then } M_1 = (16x_1 - 2x_1^2) \text{ KN}\cdot\text{m}$$

$$M_2 = (18x_2 - 2x_2^2) \text{ KN}\cdot\text{m}$$

Thus

$$\Delta B = \int_0^L M \left( \frac{\partial M}{\partial P} \right) \frac{dx}{EI}$$

2 (6)

$$\Delta B = \int_3^4 \frac{(3000x_1 - 2x_1^2)(0.333x_1)dx}{EI} + \int_0^2 \frac{(3000x_2 - 2x_2^2)(0.667x_2)dx}{EI}$$

$$\Delta B = \frac{218.5}{EI}$$

$$\Delta B = \frac{218.5}{(200 \times 10^9)(0.0006)} = 0.018 \text{ m}$$

$$\boxed{\Delta B = 18 \text{ mm}}$$

Rec  
Ans

Question No (03)

Solution

Given data

$$W_0 = \text{Uniform load} = 400 \text{ lb/ft}$$

$$h = \text{height} = 10 \text{ ft}$$

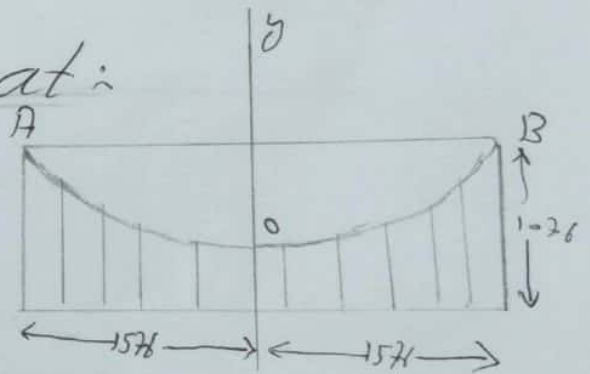
$$\text{Length } (L) = 15 \text{ ft}$$

Required:

Equation of curve and forces in cable = ?

We know that:

$$y = \frac{h}{L^2} x^2$$



Putting values

$$y = \frac{10}{(15)^2} x^2 = \boxed{0.044 x^2}$$

$$T_0 = F_H = \frac{W_0 L^2}{2h} = \frac{400 \times (15)^2}{2(10)}$$

$$\boxed{T_0 = 4500 \text{ lb} = 4.5 \text{ klb}}$$

$$T_B = T_{max} = \sqrt{(Wh)^2 + (W \cdot L)^2}$$
$$= \sqrt{(4500)^2 + (400 \times 15)^2}$$

$$T_{max} = 7500 \text{ lb} = 7.5 \text{ kb}$$

" $T_{max}$ " By another equation

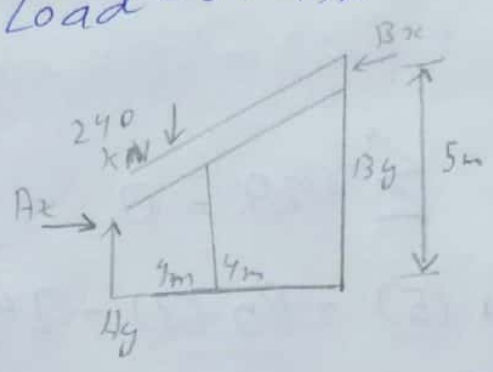
$$T_B T_{max} = W \cdot L \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$
$$= 400 \times 15 \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

$$T_{max} = 7500 \text{ lb} = 7.5 \text{ k}$$

# Question No 4

## Given data

Uniform Load =  $30 \text{ kN/m}$

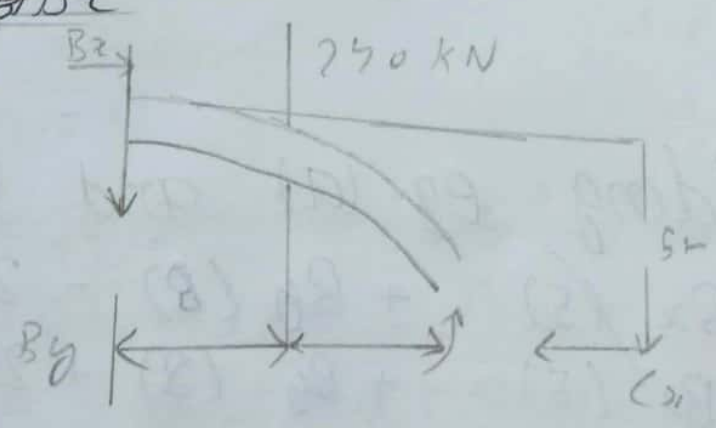


Member AB

## Require data

Internal moment at D = ?

## Member BC



Solution:

Dividing into two members  
AB and BC.

AB

$$\curvearrowleft + \sum M_A = 0$$

$$B_x (5) + B_y (8) - 240 (4) = 0$$

→ (a)

BC

$$\curvearrowright + \sum M_C = 0$$

$$-B_x (5) + B_y (8) + 240 (4) = 0$$

→ (b)

Adding eq (a) and (b)

$$\begin{array}{r} B_x (5) + B_y (8) - 240 (4) = 0 \\ -B_x (5) + B_y (8) + 240 (4) = 0 \end{array}$$

---


$$0 + 2B_y (8) + 0 = 0$$



$$\sum R_y (8) = 0$$

$$R_y = 0 \text{ kN}$$

Putting the values of " $R_y$ " in eq (b)

$$\text{eq (b)} \Rightarrow -B_x (5) + 0(8) + 960 = 0$$

$$B_x (5) = 960$$

$$\frac{B_x (5)}{5} = \frac{960}{5}$$

$$\boxed{B_x = 192 \text{ kN}}$$

Now at Segment "DB"

$$\hookrightarrow \sum M_D = 0$$

$$192(2) - 150(2.5) - M_D = 0$$

$$384 - 375 - M_D = 0$$

$$9 - M_D = 0$$

$$\boxed{M_D = 9 \text{ kNm}}$$