

A
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PRCD-I

Final Exam

26 - 06 - 2020

1.6" x 0.2 x
Q No 1

(1)

Live Load = 150 Psf

Service Load = 20 Psf

$f_c = 4000 \text{ psi}$

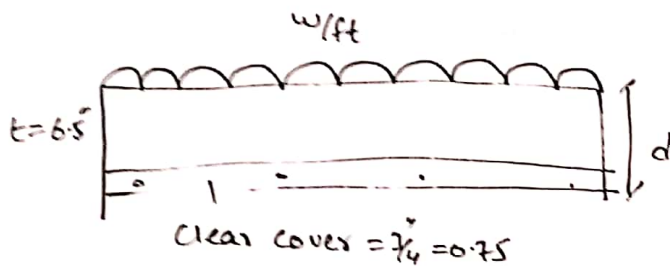
$f_y = 40 \text{ ksi}$

Solution:

Step: 01

$$l_{min} = \frac{L}{28} = \frac{15 \times 12}{28} = 6.42 \approx 6.5''$$

Step: 02 : Effective



$$d = t - (\text{clear cover} - \frac{1}{2} (d_{M.B.}))$$

$$= 6.5 - (0.75 - \frac{1}{2} (4/8))$$

$$= 6''$$

Step: 03 : Self wt of slab

$$= \frac{t}{12} \times \gamma_{\text{concrete}}$$

$$= \frac{6.5}{12} \times 150$$

(2)

$$= 81.25 \text{ Psf}$$

Step: 04 (Total factored Load)

$$w_u = 1.2(81.25 + 20) + 160$$

$$= 121.5 + 160$$

$$= 281.5$$

$$= 0.281 \text{ Ksf}$$

Step: 05

ultimate Moment

$$M_u = \frac{w_u \times l^2}{8} = \frac{0.281 \times 15^2}{8} \times 12$$

$$= 94.8 \text{ K''}$$

Step# 06

Area of steel for Main Bars By Trial
and Repeat Method

Trial# 01

let

$$a = 0.2 \times t$$

$$= 0.2 \times 6.5$$

$$= 1.3$$

(3)

$$A_s = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$= \frac{94.8}{0.90 \times 60 \times (6 - 1.3/2)} = 0.32 \text{ in}^2/\text{ft}$$

Trial 02:

$$a = \frac{A_s \times f_y}{\phi \times f_c' \times b} = \frac{0.32 \times 60}{0.85 \times 4 \times 15} = 0.37''$$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{94.8}{0.90 \times 60 \times (6 - \frac{0.37}{2})}$$

$$= 0.30 \text{ in}^2/\text{ft}$$

Trial : 03

$$a = 0.35$$

$$A_s = 0.30 \text{ in}^2/\text{ft}$$

Step : 07

Area of steel for distribution bar

$$A_{smin} = 0.0018 \times b \times t$$

$$= 0.0018 \times 15 \times 6.5 = 0.17 \text{ in}^2/\text{ft}$$

Step: 08

spacing for Main Bar

$$S = \frac{A_b}{A_s} \times 12$$

$$= \frac{0.20}{0.30} \times 12 = 8 \approx 8.5 \text{ } \#4$$

Step: 09

Spacing for Distribution bar

$$S = \frac{A_b}{A_s} \times 12$$

let try #4 bar

$$= \frac{0.20}{0.175} \times 12 = 13.71 \approx 14$$

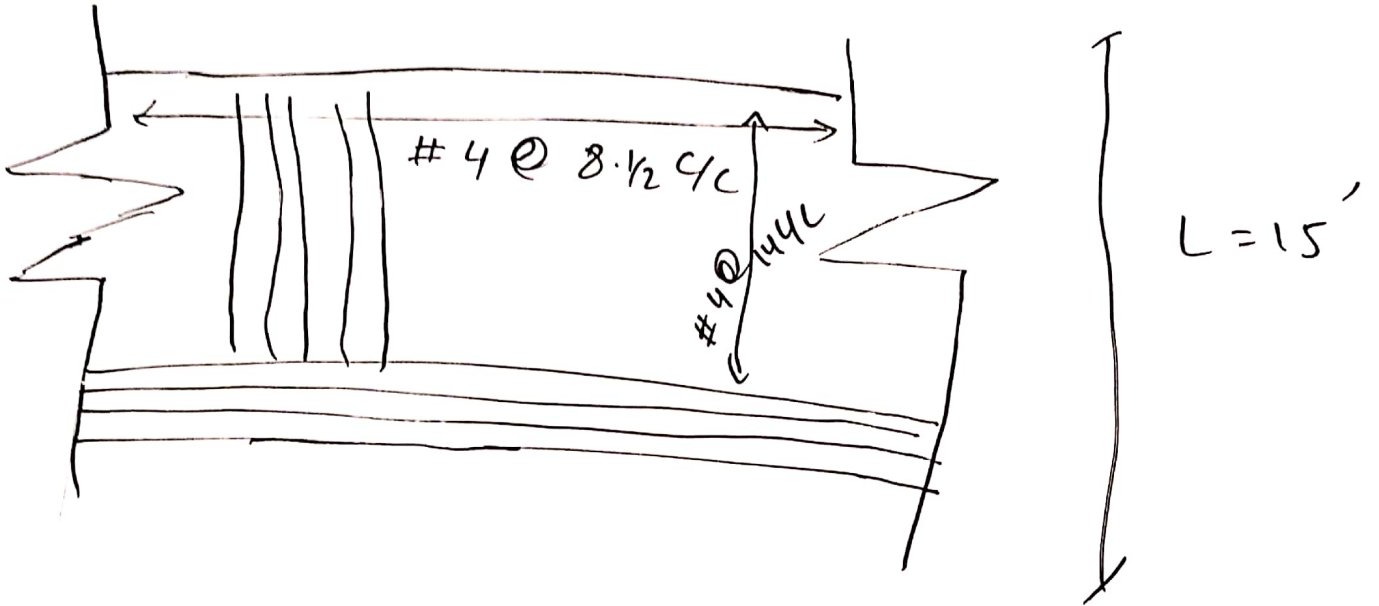
Step: 10 Final Summary

$$f'_c = 4 \text{ ksi}, f_y = 40 \text{ ksi}, t = 6.5$$

Main steel #4 at 8.5 #4

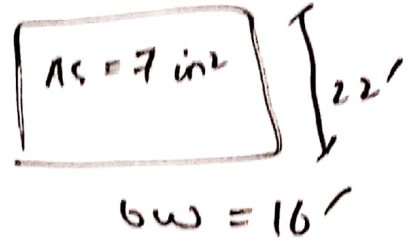
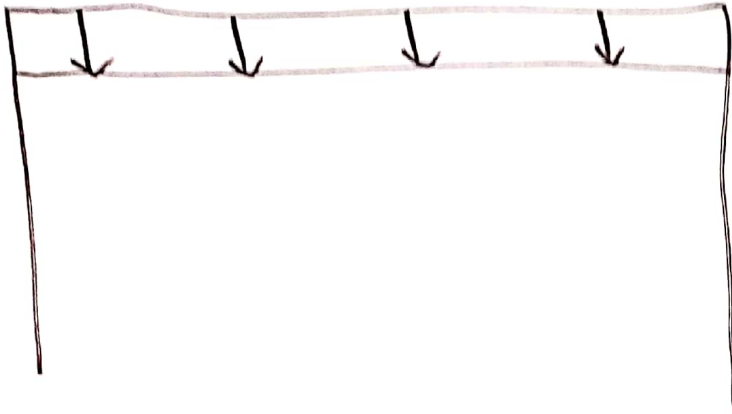
Distribution steel #4 at 14 #4

(5)



Q NO 2

9.4 k/f



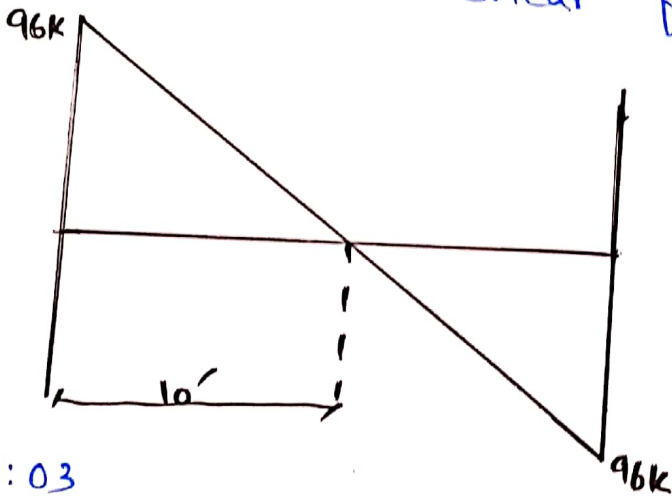
Step: 01

Find value of R_{ns}

$$= 9.6 \times \frac{20}{2} = 96k$$

Step: 02

Draw its shear force diagram



Step: 03

Find the value of critical stress σ_{cr} and its location

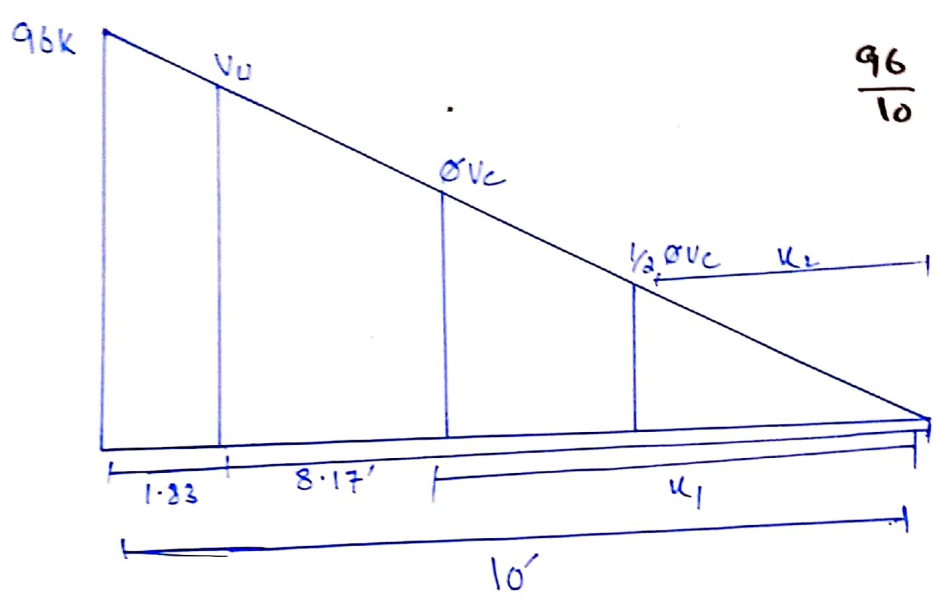
As we know that critical section is located at distance 'd' from face of support = 1-83'

Value of critical shear at distance "d" by Similarity of Δ_s

For similar Δ_s

$$\frac{96}{10} = \frac{V_u}{8.17}$$

$$V_u = 78.43$$



Step: 04

Find value of ϕV_c and $1/2 \phi V_c$ and also its distance from zero shear to right side

$$\phi V_c = \phi \times 2 \times \sqrt{f_c} \times b_w \times d$$

$$= \frac{0.75 \times 2 \times \sqrt{4000} \times 16 \times 22}{1000} = 33.40k$$

Location of ϕV_c by similar Δ_s

$$\frac{96}{10} = \frac{33.40}{x_1}$$

$$x_1 = 3.47$$

Now

$$\frac{1}{2} \phi V_c = \frac{33.40}{2} = 16.70 \text{ K}$$

$$\text{Location of } \frac{1}{2} \phi V_c \Rightarrow \frac{96}{10} = \frac{16.70}{K_2}$$

$$K_2 = 1.73$$

Step: 05

Value of ϕV_s :

$$V_u = \phi V_s + \phi V_c$$

$$\begin{aligned} \phi V_s &= V_u - \phi V_c \\ &= 78.43 - 33.40 \\ &= 45.03 \text{ K} \end{aligned}$$

Step: 06:

Check on section adequacy

$$\begin{aligned} \phi \times 8 \times \sqrt{f'_c} \times b_w \times d &= \frac{0.75 \times 8 \sqrt{4000} \times 16 \times 22}{1000} \\ &= 133.57 \text{ K} \end{aligned}$$

As

$\phi \times 8 \times \sqrt{f'_c} \times b_w \times d$

Section is adequate

Step: 07: Check on Maximum Spacing for Stirrups

$$\phi \times 4 \sqrt{f_c'} \times b_w \times d = \frac{0.75 \times 4 \sqrt{4000} \times 16 \times 22}{1000}$$

$$= 66.79 \text{ kip}$$

$$\text{As } \phi 4 \sqrt{f_c'} b_w d > \phi U_s = 45.03 \text{ k}$$

So, ~~Max~~ ^{Mini} spacing will be selected from following four condition

$$1 - S_{\max} = 24''$$

$$2 - \frac{d}{2} = \frac{22}{2} = 11''$$

$$3 - S_{\max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f_c'} \times b_w} = 17.40''$$

$$4 - \frac{A_u \times f_y}{S_o \times b_w} = \frac{0.22 \times 60,000}{S_o \times 16} = 16.50''$$

From above four condition, Least value of spacing for #3, 2 legged stirrup will selected

$$\text{So, } S_{\max} = 11'' \text{ c/c}$$

Step: 08

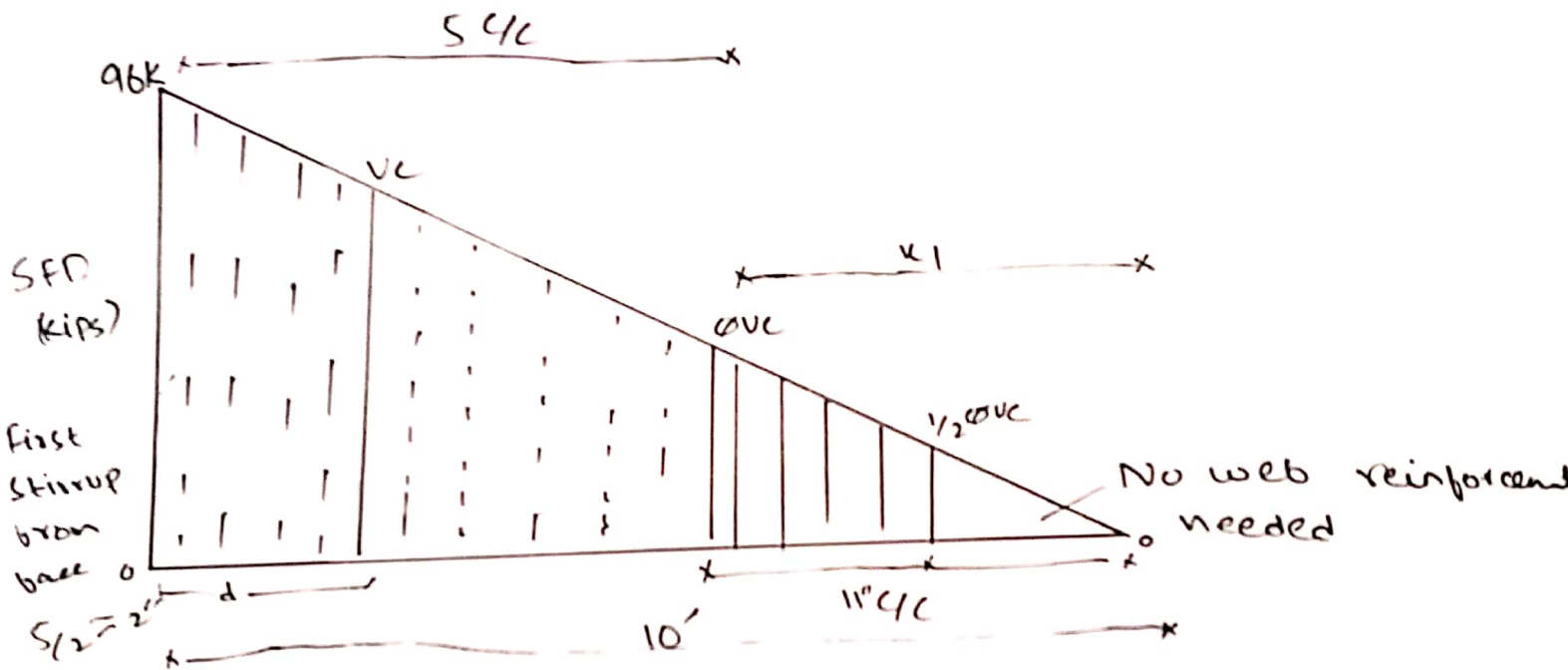
$$S = \frac{\phi + A_v \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40}$$

~~S~~

$$S = 54C$$

Step: 09

Final sketch



Q No: 3

Step: 01:

Find Gross area of concrete

$$\begin{aligned} A_g &= b \times b \quad (\text{Square footing}) \\ &= 12 \times 12 = 144 \text{ in}^2 (\text{Actual}) \end{aligned}$$

Step: 02

Find the area of steel

$$\begin{aligned} A_s &= 5\% \text{ of } A_g \\ &= 0.05 \times 144 \\ &= 7.2 \text{ in}^2 \end{aligned}$$

Step: 03 Ultimate load carrying Capacity

$$\begin{aligned} P_u &= \phi \times 0.80 [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y] \\ &= 0.65 \times 0.80 [0.85 \times 4 [144 - 7.2] + 7.2 \times 60] \end{aligned}$$

$$P_u = 466.50 \text{ k}$$

Step: 04

Sketch & design of ties (c/c to distance)

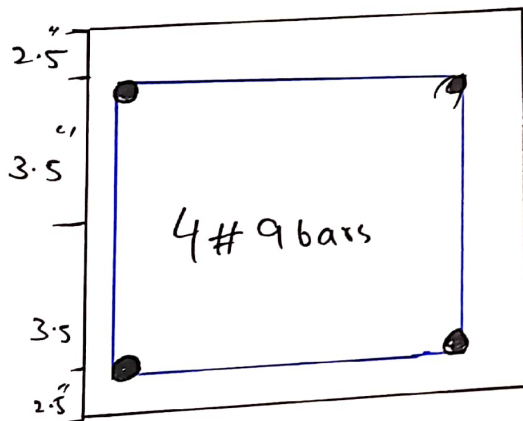
From below value we choose the least value of all these.

- $16 \times \text{dia of long bars} = 16 \times 9/8$
 $= 18''$

1- $48 \times \text{dia of tie bar} = 48 \times 3/8$
 $= 18''$

3- Least Column dimension = $12''$

So c/c distance b/w tie = $12''$



It is a tied square column.

So there is no spiral column used, the stirrup used is of rectangular shape due to the specific of the structure thus we use tie stirrup instead of spiral stirrup.

Q No 4

①

Design a square footing
Sketch the diagram.

Step: 01

let

$$h = 24''$$

Step: 02

$$\begin{aligned} \text{Total weight} &= \text{wt of soil} + \text{wt of Rc} \\ &= 3 \times 120 + 2 \times 150 \\ &= 660 \text{ Psf} = 0.66 \text{ ksf} \end{aligned}$$

Step: 03 Effective bearing Capacity

$$\begin{aligned} q_e &= q_a - w \\ &= 2.50 - 0.660 \\ &= 1.84 \text{ ksf} \end{aligned}$$

Step: 04

Required area for foundation

$$\begin{aligned} \text{Area} &= \frac{\text{Service Load}}{q_e} = \frac{100 + 120}{1.84} \\ &= 119.57 \text{ ft}^2 \end{aligned}$$

(8)

Step: 05

$$A_{req} = b \times b$$
$$= 119.57 \Rightarrow B \approx 11$$

Step: 06 Upward Bearing Capacity of Soil

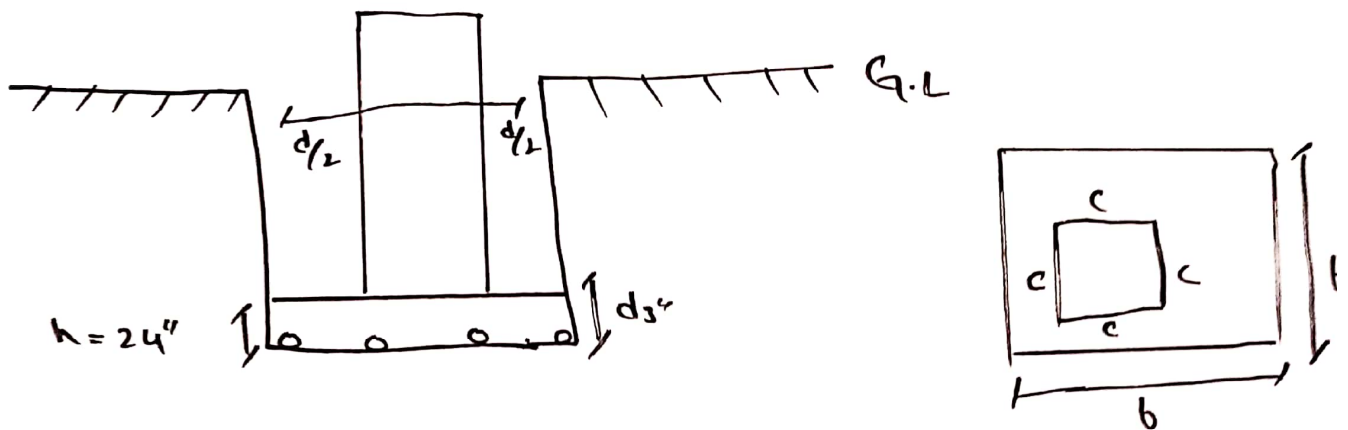
$$q_{up} = \frac{\text{Factored Load}}{B^2} = \frac{1.2 \times 100 + 1.6 \times 120}{11^2}$$

$$q_{up} = 2.58 \text{ K/ft}^2$$

Step: 07

Punching area

$$b_o = 4 \times (c + d)$$



$$d = h - c - \text{dia of bar} - \frac{1}{2} d_b$$

$$= 24 - 3 - 1 - \frac{1}{2} (1) = 19.5''$$

$$= 4 \times (16 + 19.5) = 142''$$

Step: 08

$$\begin{aligned}V_{u2} &= \phi V_{up} \times \left[B^2 - (e \times d)^2 \right] \\ &= 2.58 \left[11^2 - \frac{(16 + 19.5)^2}{12} \right] \\ &= 289.60 \text{ K}\end{aligned}$$

Step: 09

$$\begin{aligned}\phi V_{up} &= \phi \times 4 \times \sqrt{f_c} \times b \times d \\ &= \frac{0.75 \times 3 \sqrt{4000} \times 142 \times 19.5}{1000} \\ &= 525.38 \text{ K} \quad 394.0 \text{ K}\end{aligned}$$

Step: 10

Beam shear / one way shear check

$$\begin{aligned}V_u &= \phi V_{up} \times B \times \left[\frac{B}{2} - \frac{e}{2} - d \right] \\ &= 2.58 \times 11 \left[\frac{11}{2} - \frac{16}{2} - \frac{19.5}{12} \right]\end{aligned}$$

$$V_u = 90.95 \text{ K}$$

Step: 11

Self Shear Capacity

$$\begin{aligned}\phi V_c &= \phi \times 2 \times \sqrt{f'_c} \times b \times d \\ &= \frac{0.75 \times 2 \sqrt{10000} \times (11 \times 12.16)}{1000} \\ &= 110.04 > V_{U_1} \Rightarrow \text{O.K.}\end{aligned}$$

Step: 12

ultimate Moment

$$\begin{aligned}M_u &= \frac{V_{U_1} \times B}{8} \times (B - c)^2 = \frac{2.58 \times 11}{8} \times \left(11 - \frac{16}{12}\right)^2 \\ &= 331.49 \text{ k}' = 3977.93 \text{ k}\end{aligned}$$

Step: 13

Area of steel for mainbars by trial
& Repeat Method

Trial 1:

$$\text{let } a = 0.2 \times h = 0.2 \times 24 = 4.8''$$

$$\begin{aligned}A_s &= \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{3977.93}{0.9 \times 60 \left(11 - \frac{4.8}{2}\right)} \\ &= 8.56 \text{ in}^2\end{aligned}$$

trial: 2

$$a = \frac{A_s \times f_y}{0.85 \times f'_c \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12}$$
$$= 1.53''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)} = 7.197 \text{ in}^2$$

Trial 3:-

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \left(11 - \frac{1.28}{2}\right)}$$

So thus area = 7.1 in²

Step: 14

Check the min reinforcement by the following as method,

$$A_{s_{min}} = 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24$$

$$A_{s_{min}} = 5.7 \text{ in}^2$$

$$A_{smin} = \frac{200}{f_y} \times B \times d = \frac{200}{60,000} \times (11 \times 12) \times 19.5$$
$$= 8.58 \text{ in}^2$$

$$A_{smin} = \frac{3 \times \sqrt{f_c}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000}}{60,000} \times (11 \times 12) \times 19.5$$
$$= 7.05 \text{ in}^2$$

From above values greater value will be selected thus $A_{smin} = 8.58 \text{ in}^2$

Step : 15

Using # 8 bars

$$A_b = 1 \text{ in}^2$$

$$\text{No of bars} = \frac{8.585}{1 \text{ in}^2} = 9$$

≈ 9 bars in each direction.