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There are total 5 machines and 5 employments are to be relegated and the related cost network is as per the following:

Solution :-

		Machines				
		A	B	C	D	E
j o b s	1	6	12	3	11	15
	2	4	2	7	1	10
	3	8	11	10	7	11
	4	16	19	22	23	21
	5	9	5	7	6	10

Row minimization :-

		Machines					
		A	B	C	D	E	
J o b s	1	6	12	3	11	15	3
	2	4	2	7	1	10	1
	3	8	11	10	7	11	7
	4	16	19	12	23	21	16
	5	9	5	7	6	10	5

→ step 2 :-

Row subtraction :-

		MACHINES					
		A	B	C	D	E	
J o b s	3	9	0	8	12	1	
	3	1	6	0	9	2	
	1	4	3	0	4	3	
	0	3	10	6	5	4	
	4	0	2	1	5	5	

column minimization

	Machines					
	A	B	C	D	E	
J	1	3	9	0	8	12
o	2	3	1	6	0	9
b	3	1	4	3	0	4
S	4	0	3	6	6	5
	5	4	0	2	1	5
		0	0	0	0	4

→ step # 4

column subtraction:-

	Machine					
	A	B	C	D	E	
J	3	9	0	8	8	1
o	3	1	6	0	5	2
b	1	4	3	0	0	3
S	0	3	6	6	1	4
	4	0	2	1	1	5

Draw horizontal & vertical lines through circles :-

		Machine				
		A	B	C	D	E
Jobs	1	3	9	0	8	8
	2	3	1	6	0	5
	3	1	4	3	0	0
	4	0	3	6	6	1
	5	4	0	2	1	1

↓
↓
↓
↓
↓

Hence $5 = 5$

No. of circles = No. of lines.

optimal solution :

step # 6

Timing :-

		Machines				
		A	B	C	D	E
J	1	6	12	3	11	15
o	2	4	2	7	1	10
b	3	8	11	10	7	11
s	4	16	19	122	23	21
	5	9	5	7	6	10

Jobs	operators	Time
1	C	3
2	D	1
3	E	11
4	A	16
5	B	5
		36

Total processing time = 36 cr hr.
ANS

// ————— // ————— // ————— //

Question # 2.

minimization $Z = 2x_1 + 3x_2$

Subject to : $\frac{1}{2}x_1 + \frac{1}{4}x_2 \leq 4$

$$x_1 + 3x_2 \geq 20$$

$$x_1 + x_2 = 10$$

$$x_1, x_2 \geq 0$$

Solution :-

Step # 1

$$\frac{1}{2}x_1 + \frac{1}{4}x_2 + s_1 = 4$$

$$x_1 + 3x_2 - s_2 + a_1 = 20$$

$$x_1 + x_2 + a_2 = 10$$

Step # 02 :-

Set the objective function equal to zero.

$$Z = -2x_1 - 3x_2 \quad \therefore \text{for minimization} \\ \text{xing by (-1).}$$

$$Z = -2x_1 - 3x_2 - ma_1 - ma_2$$

$$Z + 2x_1 + 3x_2 + ma_1 + ma_2 = 0$$

$$2x_1 + 3x_2 + ma_1 + ma_2 + Z = 0$$

create a simple table.

	x_1	x_2	s_1	s_2	a_1	a_2	z	
$\rightarrow R_1$	s_1	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
$\rightarrow R_2$	a_1	1	3	0	-1	1	0	20
$\rightarrow R_3$	a_2	1	1	0	0	0	1	10
$\rightarrow R_4$	z	2	3	0	0	m	m	1

$$R_4 \rightarrow R_4 + (-mR_3)$$

2	3	0	0	m	m	1	0
$-m$	$-m$	0	0	0	$-m$	0	$-10m$
$2-m$	$3-m$	0	0	m	0	1	$-10m$

	x_1	x_2	s_1	s_2	a_1	a_2	z	
$\rightarrow R_1$	s_1	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
$\rightarrow R_2$	a_1	1	3	0	-1	1	0	20
$\rightarrow R_3$	a_2	1	1	0	0	0	1	10
$\rightarrow R_4$	z	$2-m$	$3-m$	0	0	m	0	$-10m$

$$\begin{array}{cccccccc}
 2-m & 3-m & 0 & 0 & m & 0 & 1 & -10m \\
 -m & -3m & 0 & m & -1 & 0 & 0 & -20m \\
 \hline
 2-2m & 3-4m & 0 & m & 0 & 0 & 1 & -30m
 \end{array}$$

$\rightarrow R_1$
 $\rightarrow R_2$
 $\rightarrow R_3$
 $\rightarrow R_4$

	x_1	x_2	S_1	S_2	a_1	a_2	Z
S_1	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
a_1	1	3	0	-1	1	0	20
a_2	1	1	0	0	0	1	10
Z	$2-2m$	$3-4m$	0	m	0	0	$-30m$

Step #4:-

Select the pivot column.

	x_1	x_2	S_1	S_2	a_1	a_2	Z
	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
	1	3	0	-1	1	0	20
	1	1	0	0	0	1	10
	$2-2m$	$3-4m$	0	m	0	0	$-30m$

Select the pivot Row.

	x_1	x_2	s_1	s_2	a_1	a_2	z
s_1	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	0
a_1	1	3	0	-1	1	0	0
a_2	1	1	0	0	0	1	0
z	$8-2m$	$3-4m$	0	m	0	0	$-30m$

$4 = \frac{4}{1/4} = 16$
 $20 : \frac{20}{3} = 6.6 \checkmark$
 $10 : \frac{10}{1} = 10$

Step #6:

Select the pivot which is the entry in the pivot column. z_1 pivot Row.

	x_1	x_2	s_1	s_2	a_1	a_2	z
s_1	$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
a_1	1	3	0	-1	1	0	20
a_2	1	1	0	0	0	1	10
z	$8-2m$	$3-4m$	0	m	0	0	$-30m$

perform Row operations to make pivot equal to 1 z_1 the remaining elements in the pivot column equal to zero.

Multiplying R_2 by $1/3$.

	x_1	x_2	S_1	S_2	a_1	a_2	z	
S_1	$1/2$	$1/4$	1	0	0	0	0	4
a_1	$1/3$	1	0	$-1/3$	$1/3$	0	0	$20/3$
a_2	1	1	0	0	0	1	0	10
z	$2-4m$	$3-4m$	0	m	0	0	1	$-30m$

Multiply R_1 by 4.

	x_1	x_2	S_1	S_2	a_1	a_2	z	
S_1	2	1	4	0	0	0	0	16
a_1	$1/3$	1	0	$-1/3$	$1/3$	0	0	$20/3$
a_2	1	1	0	0	0	1	0	10
z	$2-2m$	$3-4m$	0	m	0	0	1	$-30m$

$$\begin{array}{cccccccc}
 2 & -1 & 4 & 0 & 0 & 0 & 0 & 16 \\
 -\frac{1}{3} & -1 & 0 & \frac{1}{3} & -\frac{1}{3} & 0 & 0 & -\frac{20}{3} \\
 \hline
 \frac{6-1}{3} & 0 & 4 & \frac{1}{3} & -\frac{1}{3} & 0 & 0 & \frac{48-20}{3} \\
 \frac{5}{3} & 0 & 4 & \frac{1}{3} & -\frac{1}{3} & 0 & 0 & \frac{28}{3}
 \end{array}$$

	x_1	x_2	s_1	s_2	a_1	a_2	Z
s_1	$\frac{5}{3}$	0	4	$\frac{1}{3}$	$-\frac{1}{3}$	0	$\frac{28}{3}$
a_1	$\frac{1}{3}$	1	0	$-\frac{1}{3}$	$\frac{1}{3}$	0	$\frac{20}{3}$
a_2	1	1	0	0	0	1	10
Z	$2-2m$	$3-4m$	0	m	0	0	$-30m$

$$R_3 \rightarrow R_3 + (-1)R_2$$

$$\begin{array}{cccccccc}
 1 & 1 & 0 & 0 & 0 & 1 & 0 & 10 \\
 -\frac{1}{3} & -1 & 0 & \frac{1}{3} & -\frac{1}{3} & 0 & 0 & -\frac{20}{3} \\
 \hline
 \frac{2}{3} & 0 & 0 & \frac{1}{3} & -\frac{1}{3} & 1 & 0 & \frac{10}{3}
 \end{array}$$

	x_1	x_2	s_1	s_2	a_1	a_2	z
s_1	$\frac{5}{3}$	0	4	$\frac{1}{3}$	$-\frac{1}{3}$	0	0
a_1	$\frac{1}{3}$	1	0	$-\frac{1}{3}$	$\frac{1}{3}$	0	0
a_2	$\frac{2}{3}$	0	0	$\frac{1}{3}$	$-\frac{1}{3}$	1	0
z	$2-2m$	$3-4m$	0	m	0	0	1

$\frac{28}{3}$
 $\frac{20}{3}$
 $\frac{10}{3}$
 $-30m$

$$R_4 \rightarrow R_4 + (- (3-4m)R_2)$$

$2-2m$	$3-4m$	0	m	0	0	1	$-30m$
$-1+4m$	$-3+4m$	0	$1-4m$	$1+4m$	0	0	$-10+80m$
$1+2m$	0	0	$1-3m$	$1+4m$	0	1	$-10+50m$

Step # 8

	x_1	x_2	s_1	s_2	a_1	a_2	z
x_2	$\frac{5}{3}$	0	4	$\frac{1}{3}$	$-\frac{1}{3}$	0	0
s_1	$\frac{1}{3}$	1	0	$-\frac{1}{3}$	$\frac{1}{3}$	0	0
a_2	$\frac{2}{3}$	0	0	$\frac{1}{3}$	$-\frac{1}{3}$	1	0
z	$1+2m$	0	0	$1-3m$	$1+4m$	0	1

$\frac{28}{3}$
 $\frac{20}{3}$
 $\frac{10}{3}$
 $-10+50m$

Step # 8 :-

Repeat the identifying process by the most

$$x_2 = \frac{28}{3} \quad | \quad z = -10 + 50m$$

$$s_1 = \frac{20}{3}$$

$$a_2 = \frac{10}{3}$$

Ans

Use Vogel's approximation Method to obtain the initial feasible solution of:

origin	1	2	3	4	supply
1	20	22	17	4	120
2	24	37	9	7	70
3	32	37	20	15	50
Demand	60	40	30	110	240

Solution

	1	2	3	4	
1	X	40	X	80	30
	20	22	17	4	120
2	10	X	30	30	20 40
	24	37	9	7	
3	50	X	X	X	40 0
	32	37	20	15	50
	60	40	30	110	240
4	15	8	3		
4			8	3	
8			8		
8				8	
8					
24					

$$\text{Total cost} = 40 \times 22 + 80 \times 4 + 10 \times 24 + \\ 30 \times 9 + 50 \times 7 + 50 \times 32$$

$$= 880 + 320 + 240 + 270 + 210 + \\ 1600$$

$$\text{Total cost} = \boxed{3520}$$

