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SEMESTER : 4th

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SUBJECT : Structure Analysis - I

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Question No 1st:

Determine the vertical displacement of free end Point C on .....

Ans:

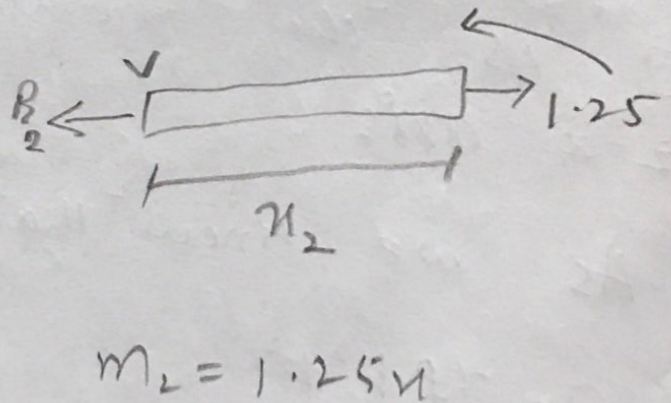
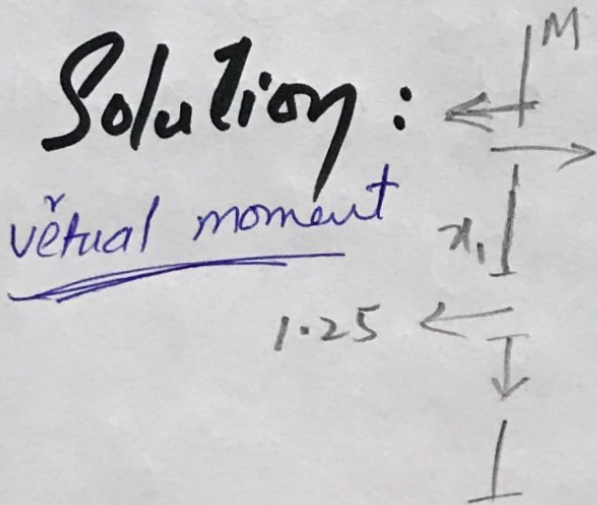
Given data

Uniform load = 4 k/ft

$E = 29 \times 10^3 \text{ Ksi}$

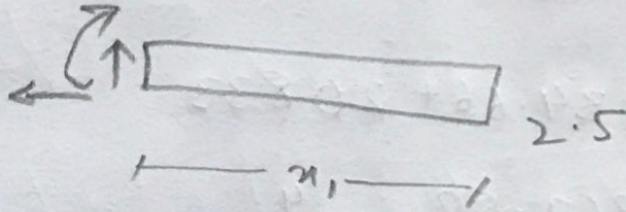
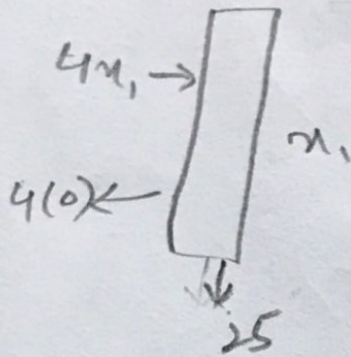
$I = 600 \text{ in}^4$

Required: vertical displacement





# Real moment



$$m_2 = 25 - x_2$$

$$m'' = \frac{40x_1 - \frac{1}{2}x_1(x_2)}{40x_1 - 2x_1^2}$$

Now! By virtual work equation

$$\Delta DC = \int_0^L \frac{m M du}{EI}$$

$$\Delta L = \int_0^{10} (1x_1) \left( \frac{40x_2 - 2x_2^2}{EI} \right) du + \int_0^8 (1 \cdot 25x_2) \left( \frac{2.5x_2}{EI} \right) du$$

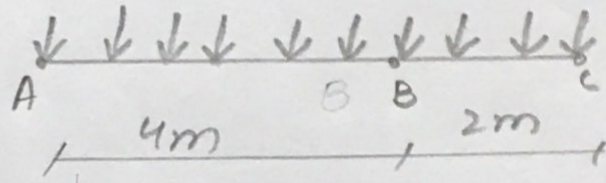


$$\Delta L = \frac{1}{EI} \left[ \frac{40x^3}{3} - \frac{2x^3}{4} \right]_0^{10} + \left[ \frac{(31.25x^2)^3}{3} \right]_0^8$$

$$\Delta L = 10649.60184$$



## Question NO 2nd

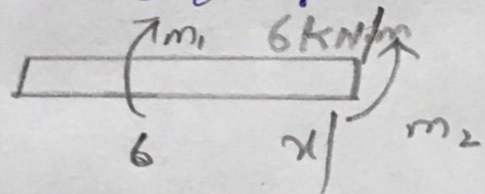
Ans  
?Given data:

$$E = 200 \text{ GPa}$$

$$I = 60 \times 10^6 \text{ mm}^4$$

Required:

Slope &amp; displacement = ?

Solution:

$$m_1 = m_2 = \frac{1}{2} (x_2) (6 + x_1)$$

$$m' = -m' - \frac{6x_2 + x_1^2}{2}$$

Taking partial derivative with respect to  $m$ .



$$\frac{\partial m_2}{\partial p} = -x$$

$$\Delta B = \int_0^2 m \frac{\partial m}{\partial p} \frac{du}{E}$$

$$= \int_0^6 \frac{-3x^2(-x) dx}{EI} + \int_0^4 \frac{-3x^2(-x) dx}{EI}$$

$$\Delta B = \frac{-3x^2}{4EI} \Big|_0^6 + \frac{-3x^4}{4EI} \Big|_0^4$$

→ Pull the value of EI and I.

$$= \frac{-3x^2}{2(200)(60 \times 10^6)} \Big|_0^6 + \frac{-3x^4}{4(200)(60 \times 10^6)} \Big|_0^4$$

$$= \frac{-216 \text{ kNft}^3}{4.8 \times 10^{10}} + \frac{-614.4 \text{ kNft}^3}{4.8 \times 10^{10}}$$



$$\Delta B = 5.76 \times 10^{-10} \text{ inch} \rightarrow \text{Displacement}$$

$$\Delta B = 5.76 \times 10^{-10} \text{ inch}$$

NOW!

Slope :-

$$m + \frac{1}{2} \times (6x_1) = 0$$

$$m = -\frac{1}{2} \times (6x_2) = -3x^2$$

So;

$$\frac{2m_1}{2m_1} = 0$$

$$m_1 - m_2 - \frac{1}{2} (x_2) (6 + x_2)$$

$$m = -m_1 + 3x^2 + \frac{x^2}{2}$$

$$\frac{2m_1}{2m_1} = -1$$

$$= \int_0^6 \frac{-3x^2}{EI} dx + \int_0^{10} \left( -2 + 6x + \frac{x^2}{2} \right) dx$$

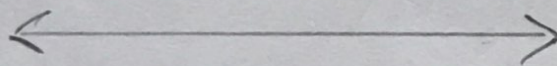


$$0 + \left( -x + \frac{6x^3}{3} + \frac{x^3}{6} \right) \Big|_0^{10} \left( \frac{1}{EI} \right)$$

$$= \frac{1}{200 \times (60 \times 10^6)} \left( -x + \frac{6x^3}{3} + \frac{x^3}{6} \right) \Big|_0^{10}$$

$$\Rightarrow \theta = 4.125 \times 10^{-7} \text{ inch}$$

$$\text{Slope} = 4.125 \times 10^{-7} \text{ inch}$$





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Question NO 3rd.

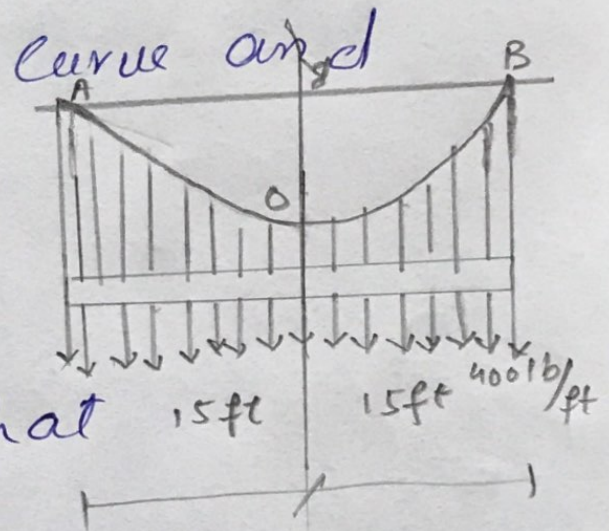
Given data:

$W_0 =$  uniform load = 400 lb/ft

$h = 10$  ft

$L = 15$  ft

Required: equation of curve and force in cable = ?



Solution:

We know that

$$y = \frac{h}{L^2} x^2$$

Putting the values

$$y = \frac{10}{(15)^2} x^2 = \frac{400 \times (15)^2}{2 \times 10}$$

$$T_B = F_H = \frac{W_0 \cdot L^2}{2h} = \frac{400 \times (15)^2}{2 \times 10}$$



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$$T_0 = 4500 \text{ lb} = 4.5 \text{ K}$$

$$T_B = T_{\max} = \sqrt{\left(\frac{P}{H}\right)^2 + (hbl)^2} = \sqrt{(4500)^2 + (400 \times 15)^2}$$

$$T_{\max} = 7500 \text{ lb} = 7.5 \text{ K}$$

NOW!

" $T_{\max}$ " By another equation

$$T_B = T_{\max} = W_0 L \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$

$$= 400 \times 15 \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

$$= T_{\max} = 7500 \text{ lb} = 7.5 \text{ K}$$



# Question No 4th.

Given data

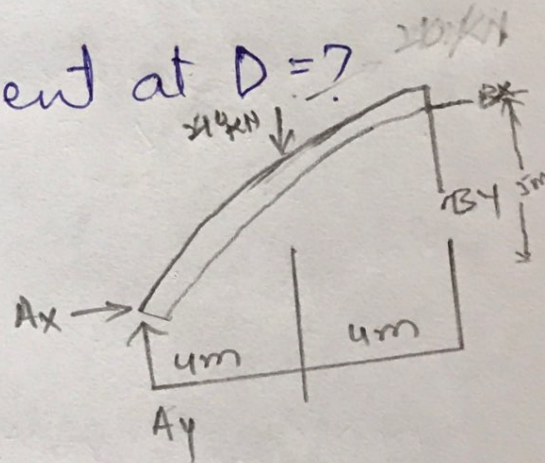
uniform load =  $30 \text{ kN/m}$

Required:-

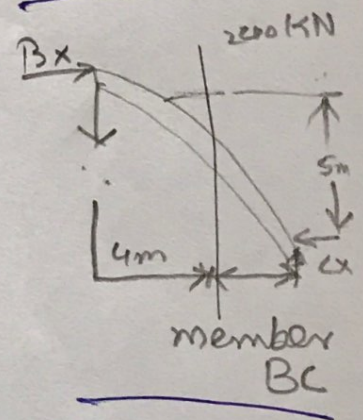
internal moment at D = ?

Solution:

Dividing into two members AB & BC



Member AB



• AB

$$\sum M_A = 0$$

$$B_x(5) + B_y(8) - 240(4) = 0 \quad (*)$$

• BC

$$\sum M_C = 0$$

$$-B_x(5) + B_y(8) + 240(4) = 0 \quad (**)$$



Adding equation  $(*)$  &  $(**)$

$$\cancel{B_x(5)} + B_y(8) - 240(4) = 0$$

$$\cancel{-B_x(5)} + B_y(8) + 240(4) = 0$$

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$$0 + 2B_y(8) + 0 = 0$$

$$2B_y(8) = 0$$

$$\Rightarrow B_y = 0 \text{ kN}$$

Putting the value of "B<sub>y</sub>" in  
eq  $(**)$

$$\text{eq } (**) = -B_x(5) + 0(8) + 960 = 0$$

$$B_x(5) = 960$$

$$\frac{B_x(5)}{(5)} = \frac{960}{5}$$

$$B_x = 192 \text{ kN}$$



Now!

at Segment DB<sup>m</sup>

$$192(2) - 150(2.5) - M_D = 0$$

$$384 - 375 - M_D = 0$$

$$9 - M_D = 0$$

$$\Rightarrow M_D = 9 \text{ kN} \cdot \text{m}$$