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SEMESTER : 2nd

ENGINEERING MECHANICS

QUESTION 15

WORK :

The product of force & displacement is called work.

A force is said to do positive work if (when applied) the force has a component in the direction of the point of application. A force does negative work if the force has a component opposite to the direction of the displacement at the point of the application of the force.

Example :

A baseball pitcher does positive work on the ball by applying a force to it over the distance it moves while in his grip.

Daily life: A man carrying book is doing work

Common symbols : W

SI unit : Joule.

Other units : Foot - Pound, Erg.

In SI base units : $1 \text{ kg} \cdot \text{m}^2 \cdot \text{s}^{-2}$.

Derivations from other equations.

$$W = F \cdot S$$

$$W = T \theta$$

Dimension = ML^2T^{-2}

Example:

When a ball is held above the ground E_1 then dropped the work done by the gravitational force on the ball as it falls is equal to the weight of the ball multiplied by the distance to the ground. When the force is constant and the angle between the force and displacement S is zero θ then the work done is given by $W = FS \cos \theta$

Energy:

Energy is the capacity of doing work.

→ It may exist in potential kinetic energy, thermal, electrical, chemical or other various forms.

→ Energy is not create nor destroy but it can be converted from one form to another.

After it has been transferred energy is always designated to its nature or other various forms.

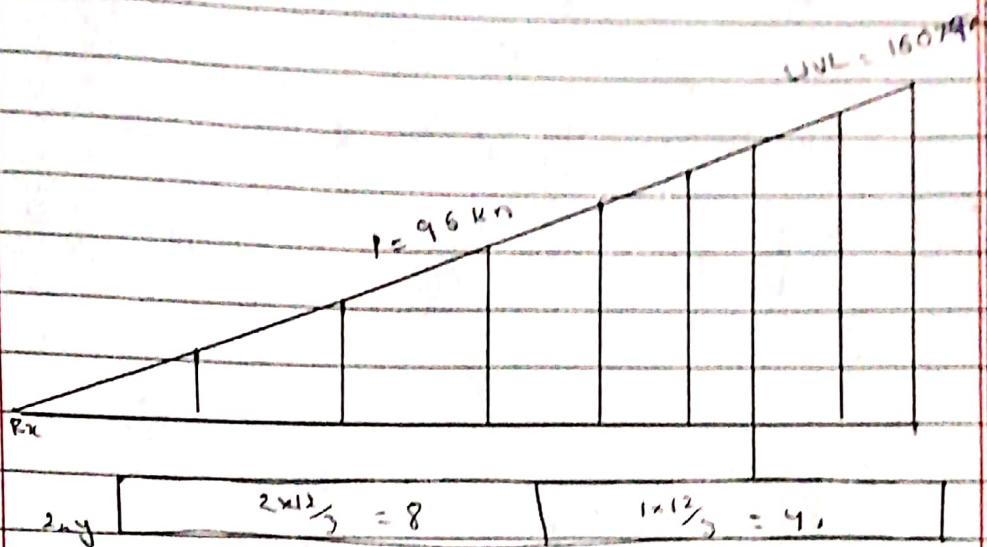
Examples:

(1) Watching television

(2) Washing clothes.

(3) Working from home on your laptop.

ANSWER 3:



$$UWL = \frac{16079}{1000} = 16.079$$

$$UWL \text{ resultant} = \frac{(16 \times \text{kN/m} \times 12)}{2}$$

$$= 96 \text{ kN}$$

This load will act $\frac{1}{3}$
of length from the
maximum side.

$$R_{1x} = 0$$

$$E_{ay} = 0$$

$$E_{fx} = 0$$

$$R_{1y} - R_{2y} - 96 \text{ kN} = 0 \quad \text{eq. 2}$$

$$(R_{2x} \times 12) - (96 \times 8) = 0 \quad \text{eq. 11}$$

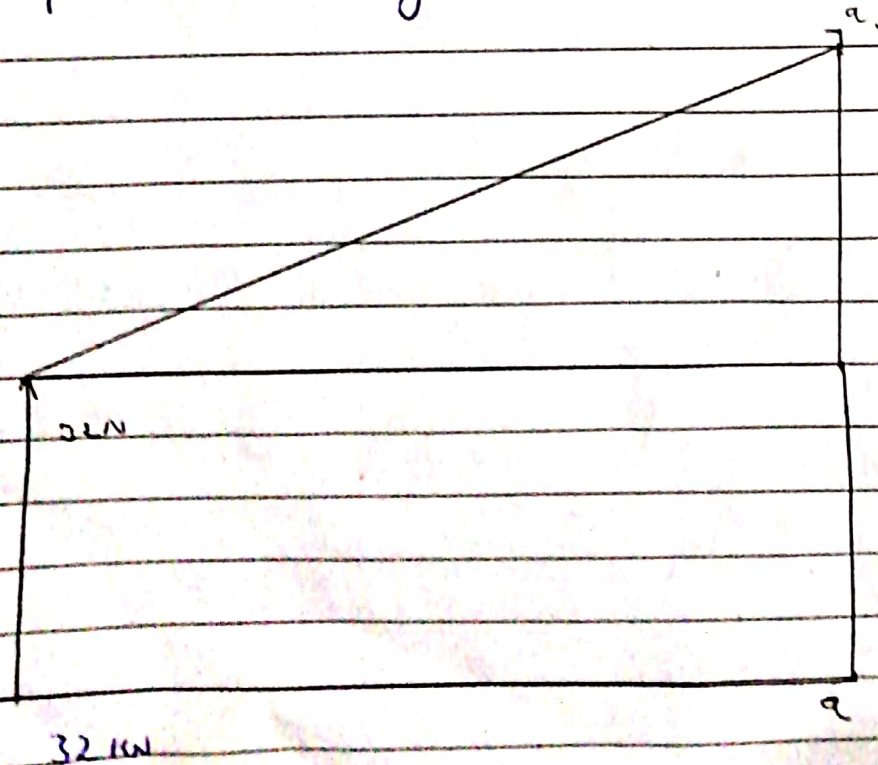
$$R_{2y} = \frac{96 \times 8}{12} = 64 \text{ kN}$$

$$R_{1y} + R_{2y} = 96 \text{ kN}$$

$$R_{1y} - 96 = R_{2y}$$

$$R_{2y} = 96 - 64 = 32 \text{ kN}$$

$$\uparrow R_{1x} = 0, \quad R_{1y} = 32 \text{ kN}, \quad R_2 = 96 \text{ kN}$$



from law of similar triangle

$$\frac{16 \text{ kN/m}}{12} = \frac{w \cdot \text{kN/m}}{n \text{ m}}$$

$$w = \left[\frac{10 \text{ kN}}{12} \right] \text{ kN/m}$$

Summation

$$\sum F_y = 0$$

$$-V_{aa} - P_1 + 32 \text{ kN}$$

$$-V_{aa} - \frac{16x^2}{24} + 32$$

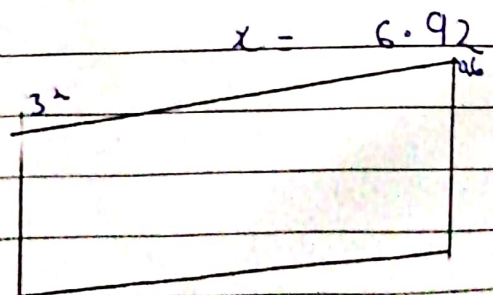
$$V_{aa} = 32 - \frac{16x^2}{24} \rightarrow \text{eq(1)}$$

$$\text{at } x=0 \quad \text{eq(1)} = 32$$

The point at which
similar forces are negative

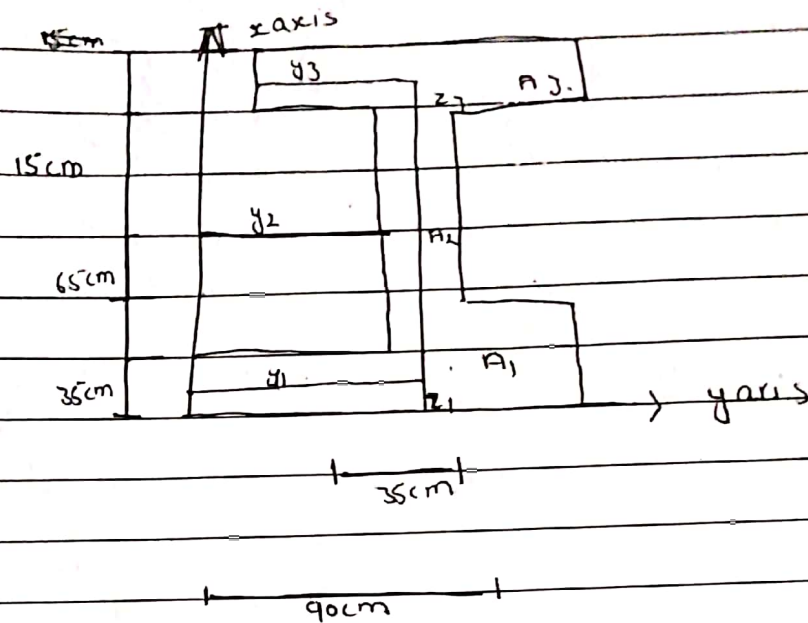
$$0 = \frac{16x^2}{24} + 12 - \frac{16x^2}{24} = 32$$

$$\sqrt{x^2} = \frac{\sqrt{12 \cdot 24}}{16} \quad x = \sqrt{48}$$



Hence the
shear force is
positive.

Q4. a) Find the centroid of the given shape.



Sol: Establishing the coordinate system

→ Dividing the composite area into different simple areas.

$$A_1 = 0.35 \times 0.9 = 0.315 \text{ m}^2$$

$$A_2 = 0.65 \times 0.35 = 0.2275 \text{ m}^2$$

$$A_3 = 0.65 \times 0.15 = 0.0975 \text{ m}^2$$

finding centre point of each from the origin.

$$y_1 = 0.9/2 = 0.45 \text{ m}$$

$$y_2 = 0.9/2 = 0.45 \text{ m}$$

$$y_3 = 0.9/2 = 0.45 \text{ m}$$

$$z_1 = 0.35/2 = 0.175 \text{ m}$$

$$z_2 = 0.35 + (0.65/2) = 0.675 \text{ m}$$

$$z_3 = 0.35 + 0.65 + 0.15/2 = 0.975 \text{ m}$$

$$y_c = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

$$A_1 + A_2 + A_3$$

$$= \frac{(0.315 \times 0.45) + (0.2275 \times 0.45 \text{ m}) + (0.0975 \times 0.45)}{0.315 + 0.2275 + 0.0975}$$

$$0.315 + 0.2275 + 0.0975$$

$$= \frac{0.14175 + 0.102375 + 0.043875}{0.43525}$$

$$0.43525$$

$$= 0.28794$$

$$0.43525$$

$$y_c = 0.6615 \text{ m}$$

$$z_c = \frac{A_1 z_1 + A_2 z_2 + A_3 z_3}{A_1 + A_2 + A_3}$$

$$A_1 + A_2 + A_3$$

$$z_c = \frac{(0.315 \times 0.175) + (0.2275 \times 0.675) + (0.0975 \times 0.975)}{0.43525}$$

$$0.43525$$

$$= 0.3134945$$

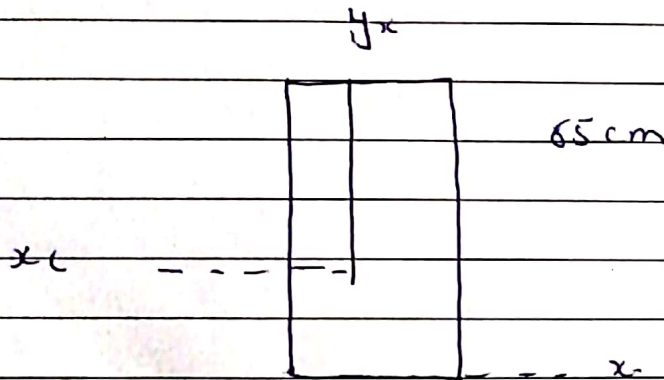
$$0.43525$$

$$z_c = 0.72026 \text{ m}$$

(b)

Moment of inertia

(65 cm x 35 cm)



$$I = \frac{bh^3}{12} = \frac{(35)(65^3)}{12}$$

$$I = 800,989.58 \text{ cm}^4$$

Radius of gyration

$$r_x = \frac{h}{\sqrt{12}} = \frac{65}{\sqrt{12}} = 18.76 \text{ cm}$$

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$$r_y = \frac{b}{\sqrt{12}} = \frac{35}{\sqrt{12}} = 10.1 \text{ cm}$$

$$r_x = \frac{h}{\sqrt{3}} = \frac{65}{\sqrt{3}} = 37.5 \text{ cm}$$

Section modulus :-

$$S = \frac{bh^2}{6}$$

$$S = \frac{35 \times 65^2}{6}$$

$$S = 26845.83 \text{ cm}^3$$

Q n 2

Share force diagram

$$P_1 = 100 + 16079 = 16179 \text{ kN}$$

$$WDL = 150 + 16079 = 16229 \text{ kN}$$

$$WDL \text{ Point load} = 16229 \times 6$$

$$= 97374$$

FBD

$$\sum F_x = 0 \Rightarrow A_x = 0$$

$$\sum F_y = 0 \Rightarrow A_y + D_y$$

$$= 16179 + 97374$$

$$= 113553 \text{ kN}$$

$$\sum M_A = 0 \Rightarrow (D_y \times 12) - (16179 \times 3) - (97374 \times 6)$$

$$D_y \times 12 = 48537 + 584244$$

$$D_y = \frac{632781}{12}$$

$$=$$

$$= 77075.25 \text{ kN}$$

Put in eq(1)

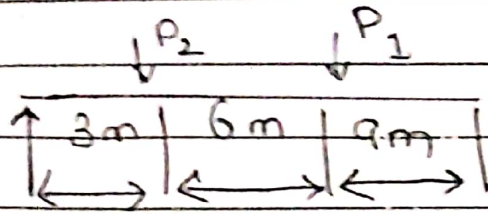
$$A_y + B_y = 1135$$

$$A_y = 1135.53 - 77075.25$$

$$= 36477.75 \text{ KN.}$$



Q: Find the support reaction show all your calculation.



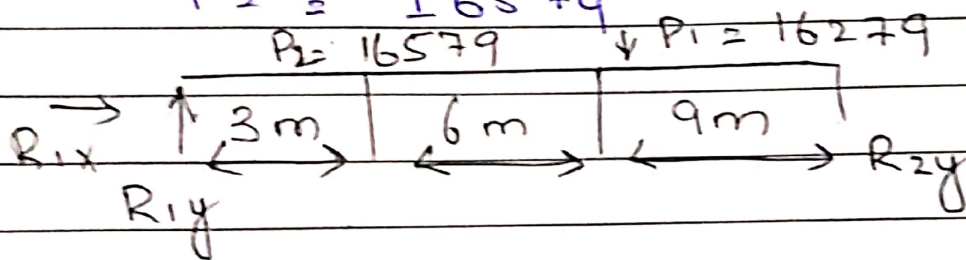
SOLUTION:-

$$P_1 = 200 + 16079$$

$$P_1 = 16279$$

$$P_2 = 500 + 16079$$

$$P_2 = 16579$$



$$R_{1x} = 0 \quad \sum \tau = 0$$

$$R_{1y} + R_{2y} = 16279 + 16579 = 0 \quad \sum F_y = 0$$

$$R_{1y} + R_{2y} = 16279 + 16579$$

$$R_{1y} + R_{2y} = 32858 \quad \text{eq (1)}$$

$$R_{1y} = \left[(16279 \times 9) + (16579 \times 15) \right] / 18$$

$$R_{1y} = \frac{146511 + 248685}{18}$$

$$R_{1y} = 21955.33 \quad \text{eq (2)}$$

Put eq (2) in eq (1)

$$R_{1y} + R_{2y} = 32858$$

$$21955.3 + R_{2y} = 32858$$

$$R_{2y} = 32858 - 21955.3$$

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$$R_{2y} = 10902.7$$

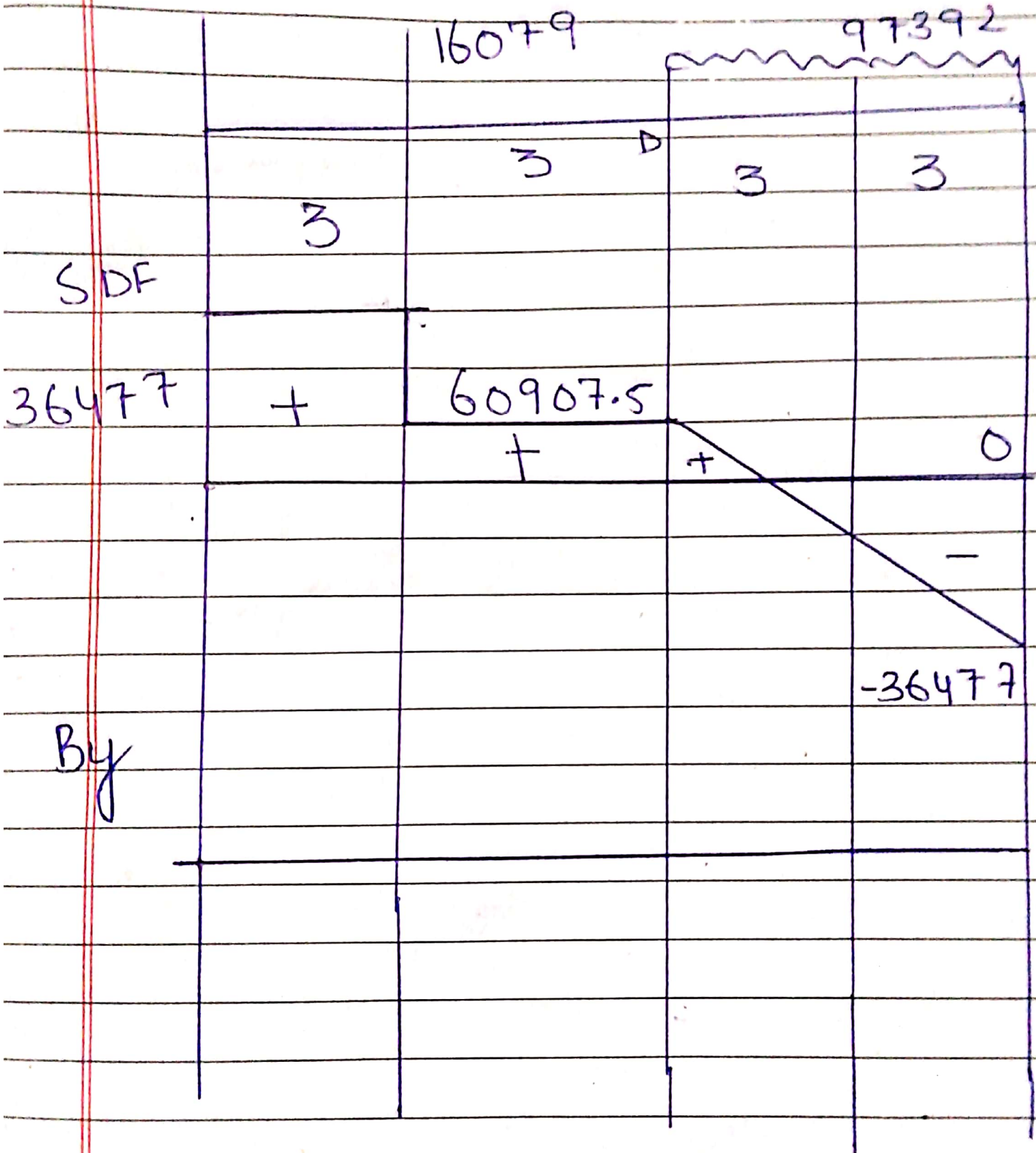
$$R_{1y} = 21955.3N$$

$$R_{1x} = 20N$$

$$R_{2y} = 10902.7$$



Q - 2 Diagram



By