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Section B

Subject Mos 2

Assignment 3

Semister 4th

Question No 1

Given data

Factor of Safety = 2

$$E = 10.3 \times 10^6 \text{ Psi}$$

$$\text{Length} = 6 \text{ ft}$$

$$b = 3/4 \text{ inch}, h = 2 \text{ inch}$$

one ~~to~~ end hinged and one end
fix

$$\text{So } L_e = 0.7L$$

Reqd

safe central load

Soln

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

$$P_{cr} = \frac{\pi^2 E A r^2}{L_e^2}$$

$$I = A r^2$$

(2)

Now

$$\gamma = \sqrt{\frac{I}{A}}$$

$$\gamma = \sqrt{\frac{hb^3/12}{bh}}$$

$$= \sqrt{\frac{b^2}{12}}$$

$$= \frac{b}{2\sqrt{3}}$$

$$= \frac{3/4}{2\sqrt{3}}$$

$$= \frac{0.75}{3.46}$$

$$\gamma = 0.216 \text{ inch}$$

Now we will find crippling load

So

$$P_{cr} = \frac{\pi^2 EA}{(L_e/K)^2}$$

$$= \frac{(\pi)^2 (10.5 \times 10^6) (1.5 \text{ in})}{(0.7/r)^2}$$

$$P_{cr} = \frac{152.33}{54444.4}$$

$$P_{cr} = 2.7979 \times 10^3 \text{ psi}$$

$$P_{cr} = 2.7979 \text{ ksi}$$

$$\text{For safe} = \frac{P_{cr}}{\text{Factor of safety}}$$

$$= \frac{2.79}{2}$$

$$= 1.3989 \text{ ksi}$$

Question No # 2

Given data:

$$\text{Load} = 20 \text{ kips} = 2.4 \times 10^5 \text{ psi}$$

$$\text{Length} = 10 \text{ ft}$$

$$E = 29 \times 10^6 \text{ psi}$$

Reqd

length of each side.

Sol.

$$\frac{L_e}{r} = \sqrt{\frac{\pi^2 E}{6P}}$$

$$= \sqrt{\frac{\pi^2 \times 29 \times 10^6}{2.4 \times 10^5}}$$

$$\frac{L_e}{r} = \sqrt{1.19 \times 10^3}$$

$$\frac{L_e}{r} = 34.5$$

$$r = \frac{Le}{34.5}$$

$$r = \frac{10 \times 12}{34.5}$$

$$r = 3.4 \text{ in}$$

9st method

$$r = \sqrt{\frac{b^2}{12}}$$

$$r^2 \times 12 = b^2$$

$$b^2 = (3.4)^2 \times 12$$

$$\sqrt{b^2} = \sqrt{138.72}$$

$$b = 11.77$$

2nd method ..

$$\bar{I} = Ar^2$$

$$A = \frac{\bar{I}}{r^2}$$

$$b = \frac{b^2}{12} / r^2$$

$$1 = \frac{b^2}{12r^2}$$

$$b^2 = 12r^2$$

$$b = 11.77$$

(7)

Question No = 3

Given

$$\text{load} = 20 \text{ kips} = 2.4 \times 10^5 \text{ psi}$$

$$\text{length} = L = 10 \text{ ft}$$

$$E = 1.6 \times 10^6 \text{ psi}$$

Required data

length of each side = ?

Sol.

$$\frac{L_e}{r} = \sqrt{\frac{\pi^2 E}{61}}$$

$$\frac{L_e}{r} = \sqrt{\frac{(3.14)^2 \times (1.6) \times 10^6}{2.4 \times 10^5}}$$

$$\frac{L_e}{r} = \sqrt{\frac{9.8596 \times 1.6 \times 10^6 \times 10^5}{2.4}}$$

$$\frac{L_e}{r} = 8.107.$$

(8)

$$r = \frac{Le}{8.107}$$

$$r = \frac{10 \times 12}{8.107}$$

$$r = 14.802 \text{ inch}$$

2nd method

$$r = \sqrt{\frac{b^2}{12}}$$

$$r^2 \times 12 = b^2$$

$$b^2 = (14.802)^2 \times 12$$

$$b = 57.275$$

(9)

2nd method

$$I = Ar^2$$

$$A = \frac{I}{r^2}$$

$$h^2 = \frac{hr^2}{12} / r^2$$

$$I = \frac{h^2}{12r^2}$$

$$h^2 = 12r^2$$

$$\sqrt{h^2} = \sqrt{2629.190}$$

$$h = 51.275$$

Question No = 4

Given data

$$\text{Column} = 310 \text{ mm} \times 45 \text{ mm}$$

$$E = 200 \times 10^9 \text{ Pa}$$

$$BP = 240 \times 10^6 \text{ Pa}$$

$$L = 12 \text{ m}$$

$$\text{Factor of safety} = 2.5$$

Req 1.

~~BP = ?~~

$$L_{\text{min}} = ?$$

$$P_{\text{saf}} = ?$$

Sol.

$$BP = \frac{E \pi^2}{(L_e/r)^2}$$

(11)

$$\frac{l_e}{r} = \sqrt{\frac{E \pi^2}{\delta P}}$$

$$\frac{l_e}{r} = \sqrt{\frac{(3.14)^2 \times 200 \times 10^9}{240 \times 10^6}}$$

$$\frac{l_e}{r} = 90.64$$

Now $r = \sqrt{\frac{D^2}{12}}$

$$r = \sqrt{\frac{(45)^2}{12}}$$

$$r = 12.99 \text{ mm}$$

Now $l_e = 90.64 \times 12.99$

$$l_e = 1177.44 \text{ mm}$$

Now for pin hinge

12

$$L \leq L_e$$

$$L_{mm} = 1177.44 \text{ m.}$$

Part (b)

$$P_{cr} = \frac{\pi^2 E A r^2}{L_e^2}$$

$$P_{cr} = \frac{\pi^2 (200 \times 10^9) (13950) (1299)^2}{12 \times 1000}$$

$$P_{cr} = 32.23 \text{ kN}$$

Now

$$P_{safe} = \frac{P_{cr}}{\text{factor of safety}}$$

$$P_{safe} = \frac{32.2343}{2.5}$$

$$P_{safe} = 12.89 \text{ kN}$$