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SUBJECT THEORY OF AUTOMATA

SEMESTER 6TH

PROGRAM BS(CS)

**Q#1. Keeping in view the Kleene's Theorem, proof for any language S.
 $S^+ = (S^+)^+$**

Ans:

$$S^+ = (S^+)^+$$

Solution: since S^+ generates all possible strings that can be obtained by concatenation the strings of S, so $(S^+)^+$ generates all possible strings that can be obtained by concatenating the strings of S^+ will not generate any new string.

Hence $(S^+)^+ = S^+$ so,

$$S^{++} \subset S^+ \longrightarrow \text{EQ1}$$

Also we know that

$$A \subset A^+ \longrightarrow \text{EQa}$$

Now, if in equation (EQa) we replace A with S^+ we get

$$S^+ \subset S^{++} \longrightarrow \text{EQ2}$$

Form both the EQ1 and EQ2 proved that

$$S^+ = S^{++}$$

$$(S^+)^+ = S^+$$

Solution: since S^+ generates all possible strings that can be obtained by concatenating the strings of S, so $(S^+)^+$ generates all possible strings

that can be obtained by concatenating the strings of S^+ , will not generate any new string.

$$\text{Hence } (S^+)^+ = S^+$$

Q#2. How many words does S^* will have of length 3, 4 and 5, if

$$S = \{ab \ ba\}$$

(Design S^* and then write answers on the basis of words of S^*)

Ans:

$S^* = \{\epsilon, ab, ba, abab, baab, baba, ababab, ababba, abbaba, bababa, babaab, baabba, baabab, \dots\}$

Total length is $= n^n$

Total number of 4 $= 2^2 = 16$

For length 3 and 5 we can't find length because it odd and we have language fo even numbers.

Q#3. Fill in the blanks.

1. A dictionary is arranged in _____ **Alphabetical** _____ order.
2. + is called _____ **positive** _____ instances.
3. * is called _____ **Kleene** _____ instances.
4. ? is called _____ **zero/one** _____ instances.
5. A Formal Language is game of _____ **focus** _____ on paper.
6. ^ is included in _____ **Kleene** _____ closure.
7. _____ **Palindrome** _____ is a word whose reverse is equal to itself.
8. _____ **Concatenation** _____ is an operation in which symbols are placed side by side.
9. $\{a\}^* \{b\}^* = \{b\}^* \{a\}^*$ for _____ **Matrice** _____ operation.
10. Two words having same symbols in same order are called _____ **same** _____ words.