## Mid Semester Assignment

## Spring 2020

## Subject: Probability and Statistics

Q1: Students were asked how long it took them to walk to school on a particular morning. A cumulative frequency distribution was formed

| Time taken(in <br> minutes) | $<5$ | $<10$ | $<15$ | $<20$ | $<25$ | $<30$ | $<35$ | $<40$ | $<45$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 25 | 45 | 81 | 143 | 280 | 349 | 374 | 395 | 400 |

a) Draw a cumulative frequency curve and estimate how many students took less than 18 minutes.

## ANSWER:

| Time Taken | Frequency | Cumulative <br> frequency |
| :---: | :---: | :---: |
| 5 | 25 | 25 |
| 10 | 45 | $25+45=70$ |
| 15 | 81 | $70+81=151$ |
| 20 | 143 | $151+143=294$ |
| 25 | 380 | $294+280=574$ |
| 30 | 374 | $574+349=923$ |
| 35 | 395 | $923+374=1297$ |
| 40 | 400 | $1297+395=1692$ |
| 45 |  | $1692+400=2092$ |
|  |  |  |

Cumulative Frequency Graph


Only 3 students took less than 18 minutes
b) Take equal class intervals of $0-$, $5-$, 10-, etc., construct frequency distribution and draw a histogram.

ANSWER:

## Data:

$\begin{array}{lllllllll}5 & 10 & 15 & 20 & 25 & 30 & 35 & 40 & 45\end{array}$
Classes $=5$
Width: $\frac{45-5}{5}=\frac{40}{5}=8$

| Classes | Frequency |
| :---: | :---: |
| $5-12$ | 2 |
| $13-20$ | 2 |
| $21-28$ | 1 |
| $29-36$ | 2 |
| $37-44$ | 2 |



Q2: Construct a grouped distribution table for the following data and Calculate Mean, Mode and Quartiles.
$423,369,387,411,393,394,371,377,389,409,392,408,431,401,363,391$, $405,382,400,381,399,415,428,422,396,372,410,419,386,390$

## ANSWER:

## Mean:

## $=\underline{423+369+387+411+393+394+-------------419+386+390}$

30
$=397.1$
Mode:

## Most repeated Value = 369

## Quartile:

## Arrange them in according to order

$=394+0.5(15-14)$
$=394.5=395$

Q3: By multiplying each of the numbers $3,6,2,1,7,5$ by 2 and then adding 5 , we obtain $11,17,9,7,19,15$. What is the relation between the standard deviation and the means of the two sets?

## ANSWER:

The mean of the first Data set is $=4$

The Standard Deviation of First data set is $\mathbf{= 2 . 3 6 6 4}$
The mean of the first Data set is $=13$
The Standard Deviation of First data set is $\mathbf{= 7 . 5 4 9 8 3}$

## Relation between the standard deviation and the mean of two sets:

The standard deviation (SD) measures the amount of variability, or dispersion, for a subject set of data from the mean, There will be a lot of values that will be closer to the mean which makes the distribution less spread out and less details. In contrast a higher standard deviation indicates higher amount of data variability to the data sets, in other words there will be a lot more values which will be far from mean which makes the distribution more spread out.

Q4: For the following grouped distribution table Calculate the Variance and Standard Deviation

| Class | $64-84$ | $85-104$ | $105-124$ | $125-144$ | $145-164$ | $165-184$ | $185-204$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 15 | 18 | 27 | 10 | 6 | 5 | 13 |

ANSWER:

|  | F | MID-POINT |
| :--- | :--- | :--- |
| $64-84$ | 15 | 74 |
| $85-104$ | 18 | 94.5 |
| $105-124$ | 27 | 114.5 |
| $125-144$ | 10 | 134.5 |
| $145-164$ | 6 | 154.5 |
| $165-184$ | 5 | 174.5 |
| $185-204$ | 13 | 194.5 |

## Q5: Comment on the following sentences

a) The depth of a river at four different points is $2,7,5,6$ feet respectively. The average depth is 5 feet. Therefore all the people with heights 5 feet can cross it
b) The average marks of one class of students are 30 . Therefore every student is hopeless.
c) The average income of a king and his household servants is $£ 20,000$ per month, therefore all the household servants must be fabulously paid.

ANSWER a) The average on 5 , which means not all bridges have a depth of 5 feet
ANSWER b) Not true: Many students would have scored high marks, but the opposing factor i-e students with mediocre marks are also present hence average comes out to be 30.

ANSWER c) Not true: King is very rich and his income is combined with all the servants will makes an average of high amount

