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Section

A

Assignment

Hydraulic Engg

# Assignment # 01

Q No. 1):

Answer: Venturi Flume: A Venturi flume is a critical flow open flume with a constricted flow which causes a drop in the hydraulic grade line, creating a critical depth.

→ It is used in flow measurement of very large flow rates, usually given in millions of cubic units.

→ A venturi meter would normally measure in millimetres, whereas a venturi flume measures in metres.

→ Measurement of discharge with venturi flumes requires two measurements, one upstream and one at the throat (narrowest cross section), if the flow passes in a subcritical state through the flume. If the flumes are designed so as to pass the flow from subcritical to supercritical state while passing through the flume, a single

measurement at the throat is sufficient for computation of discharge.

→ To ensure the occurrence of critical depth at the throat, the flumes are usually designed in such a way as to form a hydraulic jump on the downstream side of the structure. These flumes are called "Standing wave flumes".



QNO. 2): A 3m wide channel carries a total discharge of  $12 \text{ m}^3/\text{sec}$  calculate.

- \* ) Critical depth.
- \* ) Minimum specific energy.
- \* ) Alternate depth  $E = 4 \text{ m}$ .

Given Data:

width of channel =  $b = 3 \text{ m}$

Discharge =  $Q = 12 \text{ m}^3/\text{sec}$

Solution:

① Critical Depth:

Discharge per unit width

$$q = Q/b = \frac{12}{3}$$

$$q = 4 \text{ m}^3/\text{sec}$$

For Rectangular channel

$$h_c = \left( \frac{q^3}{g} \right)^{1/3} = \left( \frac{4^3}{9.81} \right)^{1/3}$$

$$h_c = 1.18 \text{ m}$$

② Minimum specific energy ( $E_c$ ) = ?

For Rectangular channel

$$E_c = \frac{3}{2} h_c = \frac{3}{2} \times 1.18$$

$$E_c = 1.77 \text{ m}$$

c) The Alternate depth  $E=4\text{m}$

As  $E > E_c$ , There are two possible depth For a given specific energy.

$$E = h + \frac{v^2}{2g} \quad \text{Where } v = \frac{Q}{A} = \frac{q}{h}$$

(For Rectangular channel)

$$E = h + \frac{q^2}{2gh^3}$$

$$4 = h + \frac{0.8155}{h^2}$$

For the subcritical solution the first term, associated with potential energy

$$h = 4 - \frac{0.8155}{h^2}$$

$\Rightarrow$  Iteration (from  $h=4$ ) gives  $h=3.948\text{m}$

For subcritical (First, Shallow) solution. The second term associated with kinetic energy.

dominates rearrange as;

$$\text{So } h = \sqrt{\frac{0.8155}{4-h}}$$

Iteration (from  $h=0$ ) gives  $h=0.4814\text{m}$

So Alternate depth are  $3.95\text{m}$  and  $0.4814\text{m}$

## Assignment #02

Question #01: Water flows at a depth of 0.1 m in a rectangular channel with a velocity of 6 m/s. Is the flow subcritical or supercritical? What is the alternate depth?

Solution:

First of all we find the Froude Number to find the flow.

As we know that

$$F_r = \frac{V}{\sqrt{gy}} = \frac{6 \text{ m/s}}{\sqrt{9.81 \times 0.1}}$$

$$F_r = 6.06 > 1$$

So the flow is supercritical.

Alternate Depth:

As we know that

$$E = y + \frac{V^2}{2g}$$

$$= 0.1 + \frac{6^2}{2 \times 9.81} = \boxed{1.935 \text{ m}}$$

The alternate depth for  $E = 1.935 \text{ m}$

yields  $\boxed{y_{\text{alt}} = 1.93 \text{ m}}$

Q#02: Water flow with a velocity of 2 m/s and at a depth of 3m in a rectangular channel. What is the change in depth and in water surface elevation produced by a gradual upward change in bottom elevations (upstep) to 60cm? What would be the depth and elevation changes if there were a gradual downstep of 15cm? What is the maximum size of upstep that would exist before upstream depth changes would result? Neglect head losses.

Given Data:

$$\text{velocity} = v_1 = 2 \text{ m/s}$$

$$\text{depth} = y_1 = 3 \text{ m}$$

$$\text{Elevation } \Delta x = 60 \text{ cm} = 0.6 \text{ m}$$

$$\text{downstep} = 15 \text{ cm} = 0.15 \text{ m}$$

Solution: As we know that

$$\begin{aligned} E_1 &= y_1 + \frac{v_1^2}{2g} \\ &= 3 + \frac{2^2}{2 \times 9.81} \end{aligned}$$

$$E_1 = 3.20 \text{ m}$$

Now  $E_2 = E_1 - \Delta x$

$$= 3.2 - 0.6$$

$$E_2 = 2.60 \text{ m}$$



Also

$$E_2 = y_2 + \frac{v^2}{2g y_2^3}$$

$$2.60 = y_2 + \frac{6^2}{2 \times 9.81 \cdot y_2^3}$$

$$\Rightarrow \boxed{y_2 = 2.24 \text{ m}}$$

$$\Delta y = y_2 - y_1$$

$$\Delta y = 2.24 - 3$$

$$\boxed{\Delta y = -0.76 \text{ m}}$$

So water surface drop = 0.16 m

\* For downward step of 15 cm or 0.15 m we have

$$E_2 = E_1 - \Delta z = 3.20 - (-0.15)$$

$$\boxed{E_2 = 3.35 \text{ m}}$$

Now

$$y_2 = 3.17 \text{ m}$$

and  $\Delta y = y_2 - y_1 = 3.17 - 3$

$$\boxed{\Delta y = 0.17 \text{ m}}$$

So water surface rises 0.02 m

\* The maximum upstep possible before affecting upstream water surface level is 70.



$$y_2 = y_c$$

$$y_c = 3 \sqrt{\frac{v^2}{g}}$$

$$y_c = 3 \sqrt{\frac{6^2}{9.18}}$$

$$y_c = 1.54 \text{ m}$$

# Assignment #03

Q. NO. 1):

Given Data:  $y_1 = 3.6 \text{ m}$  ,  $y_2 = 0.9 \text{ m}$   
 $b = 3.9 \text{ m}$

Solution:

As we know that

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

Also

$$Q = A_1 v_1 = A_2 v_2$$

$$(b = b_1 = b_2)$$

$$b_1 y_1 \cdot v_1 = b_2 y_2 \cdot v_2$$

$$b \cdot y_1 \cdot v_1 = b \cdot y_2 \cdot v_2$$

$$y_1 \cdot v_1 = y_2 \cdot v_2$$

$$v_2 = \frac{y_1}{y_2} \times v_1$$

$$v_2 = \frac{3.6}{0.9} \times v_1$$

$$\boxed{v_2 = 4 v_1} \quad \text{--- (2)}$$

putting in eqn --- (1)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{(4v_1)^2}{2g}$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{16v_1^2}{2g}$$

$$\frac{v_1^2}{2g} - \frac{16v_1^2}{2g} = 0.9 - 3.6$$

$$\frac{v_1^2 - 16v_1^2}{2g} = -2.7$$

$$-\frac{15v_1^2}{2g} = -2.7$$

$$\sqrt{v_1^2} = \sqrt{\frac{2.7 \times 2(9.81)}{15}}$$

$$v_1 = 1.879 \text{ m/sec} \quad \downarrow \text{ putting in eq 2}$$

$$v_2 = 4v_1$$

$$v_2 = 4(1.879)$$

$$v_2 = 7.516 \text{ m/sec}$$

$$\text{AS } Q_1 = A_1 v_1 = b y_1 \cdot v_1$$

$$= 3.9 \times 3.6 \times 1.879$$

$$Q_1 = 26.38 \text{ m}^3/\text{sec}$$

$$Q_2 = A_2 v_2 = b y_2 \cdot v_2$$

$$= 3.9 \times 0.9 \times 7.516$$

$$Q_2 = 26.38 \text{ m}^3/\text{sec}$$

$$Q = Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec}$$

① Froude Number  $\rightarrow$  at Upstream side

$$Fr_1 = \frac{V_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}} = 0.31$$

$\downarrow$   
Sub-critical  
Flow

② Froude Number  $\rightarrow$  at downward Stream

$$Fr_2 = \frac{V_2}{\sqrt{g y_2}} = \frac{7.516}{\sqrt{9.81 \times 0.9}} = 2.52$$

$\downarrow$   
Super-critical  
Flow.