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Section # B.

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Subject # Hydraulic Eng.

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Question No 01

A prototype gate valve which will control the flow in pipe system

conveying paraffine is to be studied in a model.

List the significant drop variable on which.....

⇒ Solution :->

The pressure drop ΔP is expected to depend upon the gate opening h , the overall depth d , the velocity v , density " ρ " and viscosity μ .

List the relevant variables.

$\Delta P, h, d, v, \mu$.

Write down dimensions:

ΔP	$ML^{-1}T^{-2}$
h	L
d	L
v	LT^{-1}
ρ	ML^{-3}
μ	MLT^{-1}

Number of variable $n = 6$

number of independal dimension:
 $m = 3$ (M, L and T)

Number of non-dimensional group: $n - m = 3$

Choose $m (=3)$ Scaling variables.

Geometric (d) : kinematic/time - dependant (v)
dynamic / mass - dependent (p).

Form dimensionless group by non-dimensionalising the remaining variable $\Delta p, h, \rho, \mu$.

$$\Pi_1 = \Delta p d a \nu^b \rho^c$$

$$M^0 L^0 T^0 = (M L^{-1} T^{-2}) (L)^a (L T^{-1}) (M L^{-3})^c$$
$$= M^{1+c} L^{-1+a+b-3c} T^{-2-b}$$

$$M = 0 = 1+c \Rightarrow c = -1$$

$$T = 0 = -2-b \Rightarrow b = -2$$

$$L = 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = 0.$$

$$\Pi_1 = \Delta P V^{-2} \rho^{-1} = \frac{\Delta P}{\rho V^2}$$

$$\Pi_2 = \frac{h}{d} \quad (\text{by inspection since } h \text{ is length})$$

$$\Pi_3 = u d^a v^b \rho^c$$

$$\begin{aligned} M^0 L^0 T^0 &= (M L^{-1} T^{-1}) (L)^a (L T^{-1})^b (M L^{-3}) \\ &= M^{1+c} L^{-1+a+b-3c} T^{-1-b} \end{aligned}$$

$$M: 0 = 1+c \quad \Rightarrow \quad c = -1$$

$$T: 0 = -1-b+0 \quad \Rightarrow \quad b = -1$$

$$L: 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = -1$$

$$\Rightarrow \Pi_1 = u d^{-1} v^{-1} \rho^{-1} = \frac{u}{\rho v d}$$

Recognition of the Reynolds number suggest that we replace Π_3 by

$$\Pi'_3 = (\Pi_3)^{-1} = \frac{\rho v d}{u}$$

Hence dimensional analysis yield:

$$II_3 = \left(\frac{\rho v d}{\mu} \right)_p = \left(\frac{\rho v d}{\mu} \right)_m$$

from the last, we have a velocity ratio.

$$\frac{v_p}{v_m} = \frac{\left(\frac{\mu}{\rho} \right)_p \frac{d_m}{d_p}}{\left(\frac{\mu}{\rho} \right)_m} = \frac{0.002/800}{1.0 \times 10^{-6}} \times \frac{1}{5} \Rightarrow 0.5$$

Hence $v_m = \frac{v_p}{0.5} = \frac{3.0}{0.5} = 6.0 \text{ m/s}$

b) The ratio of the quantities of flows.

$$\begin{aligned} \frac{Q_p}{Q_m} &= \frac{(\text{velocity} \times \text{area})_p}{(\text{velocity} \times \text{area})_m} \\ &= \frac{v_p}{v_m} \left(\frac{d_p}{d_m} \right)^2 = 0.5 \times 5^{-2} \\ &= 12.5 \end{aligned}$$

c) Finally for the pressure drop.

$$\begin{aligned} II_1 &= \left(\frac{\Delta P}{\rho v^2} \right)_P = \left(\frac{\Delta P}{\rho v^2} \right)_m \Rightarrow \frac{(\Delta P)_P}{(\Delta P)_m} \\ &= \frac{\rho_P}{\rho_m} \left(\frac{v_P}{v_m} \right)^2 \\ &= \frac{800}{1000} \times 0.5^2 = 0.2 \end{aligned}$$

Hence

$$\Delta P_P = 0.2 \times 60 = 12.0 \text{ kPa.}$$

Q
No. 2

Given

Max length depth = 78 m

Specific Gravity = 2.4

$S_{av} = 784 \text{ T/m}^2$

Height of wave = 1.2 m

Solution \Rightarrow

$$1) \quad H_{\text{limiting}} = \frac{S_{av}}{\gamma_w (G - w + 1)}$$

$$= \frac{784 \times 1000}{1000 (2.4 - 0 + 1)}$$

$$H_{\text{limiting}} = 230.58$$

2) Top width, "a"

$$\text{Free board} = 1.5 \times h_{\text{wave}}$$

$$= 1.5 \times 1.2$$

$$= 1.8$$

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$$\text{Height of Dam} = H_w + F.B$$

$$= 78 + 1.8$$

$$H.D = 79.8$$

$$a = 14\% \text{ of } H.D$$

$$= 0.14 \times 79.8$$

$$= 11.172 \text{ m}$$

3) Base width \Rightarrow

$$b' = \frac{H_w}{\mu G} = \frac{78}{0.7 \times 2.4}$$

$$= 46.42 \text{ m}$$

$$= 47$$

4) For no tension criteria \Rightarrow

$$b' = \frac{H_w}{\sqrt{G}} = \frac{78}{\sqrt{2.4}}$$

$$\Rightarrow 50.34$$

→ Depth of vertical portion on u/s side

$$\begin{aligned}
 h' &= 2a \sqrt{G \cdot w} \\
 &= 2 \times 11.172 \sqrt{2.4 - 0} \\
 &= 34.60 \\
 &= 35 \text{ m}
 \end{aligned}$$

→ Upstream offset :-

$$\begin{aligned}
 \frac{a}{16} &= \frac{11.172}{16} \\
 &= 0.6
 \end{aligned}$$

Depth of below the water level to the end of inclined portion u/s = $3.14a \sqrt{G}$

$$\begin{aligned}
 &= 3.14 \times 11.172 \sqrt{2.4} \\
 &= 54.33
 \end{aligned}$$

Total width of the base of the dam.

$$\begin{aligned}
 b &= b' + \frac{a}{16} = 50.34 + \frac{11.172}{16} \\
 &= 51.03
 \end{aligned}$$

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$$\tan \theta = \frac{b'}{H} = \frac{50.34}{78}$$

$$\theta = \tan^{-1}(0.64)$$

$$= 44.80^\circ$$

Depth of vertical portion on D/s
(from WL on U/s side).

$$\tan \theta = \frac{a}{d'} = \frac{11.172}{d'}$$

$$\tan \theta = \frac{11.172}{d'}$$

$$d' = 17.30 \text{ m}$$

$$\left(\frac{839}{1300}\right) \times d' = 11.172$$

Depth of vertical portion:

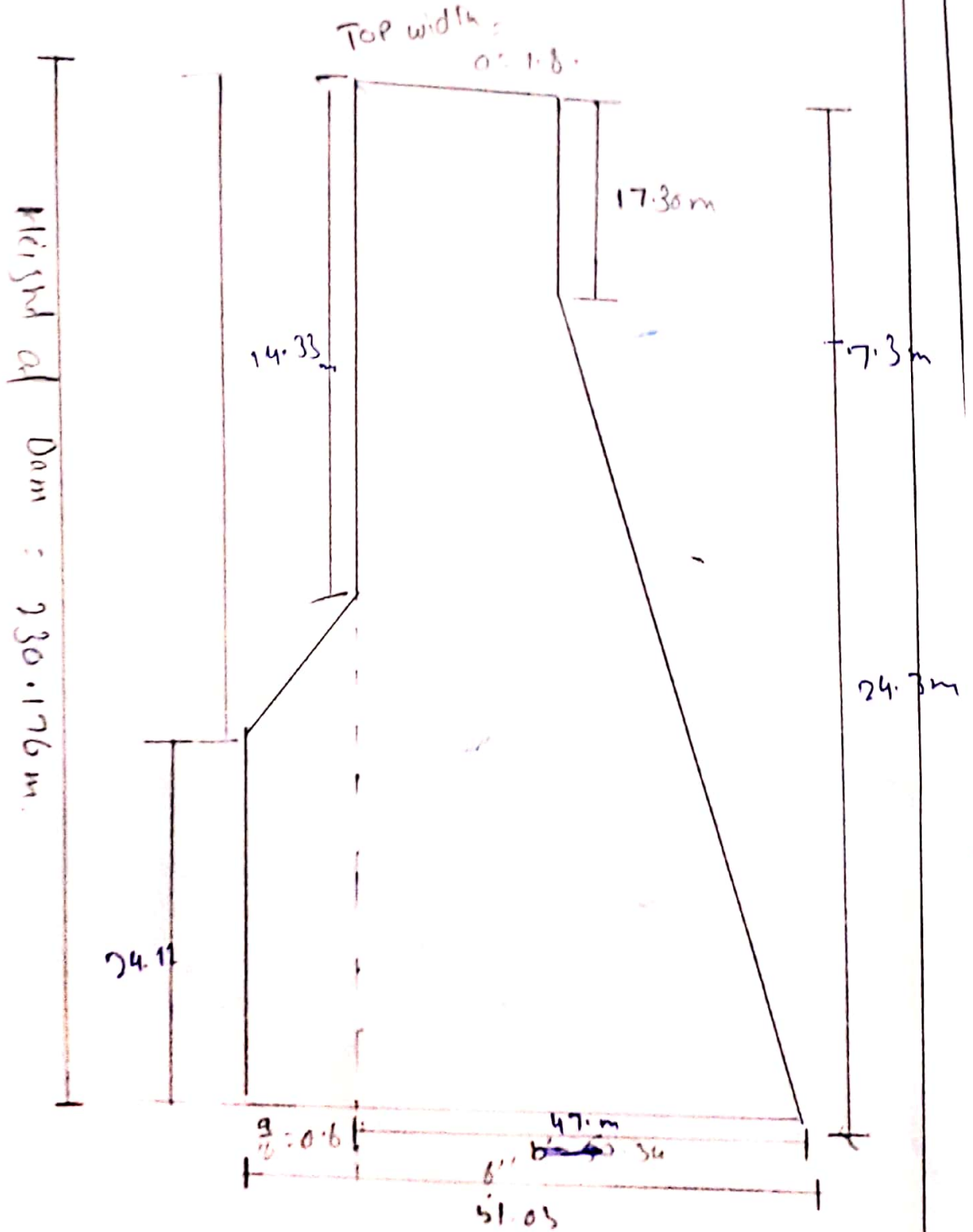
$$d = d' + F.B$$

$$= 17.30 + 1.8$$

$$= 19.1$$

Diagram.

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Dimensional analysis of Power.

Sol

- (i) head (H)
- (ii) discharge (Q)
- (iii) sp weight (w).

$$\text{OR } P = f [H, Q, w].$$

$$\Rightarrow P = K H^a \cdot Q^b \cdot w^c \rightarrow \text{①}$$

where $K = \text{const}$.

a, b, c arbitrary power.

Now:

L.H.S. i.e. Power = $[MLT^{-3}]$

dimension on R.H.S

$$\text{i.e. } H = [L]$$

$$Q = [L^3 T^{-1}]$$

$$w = [ML^{-2} T^{-2}].$$

Putting eq.

~~$$[ML^2 T^{-3}] = K [L]^a [L^3 T^{-1}]^b [ML^{-2} T^{-2}]^c$$~~

$$[ML^2 T^{-3}] = K [L]^a [L^3 T^{-1}]^b [ML^{-2} T^{-2}]^c$$

Power of M: $1 = C$

$$\therefore C = 1.$$

Power of L: $2 = a + 3b - 2c$

Power of T: $3 = -b - 2c$

$$\Rightarrow b = 1 \quad \checkmark$$

Thus putting values of b & c in

Power of L we get, $a = 1$

Thus: $a = b = c = 1$

$\textcircled{1} \Rightarrow P = KHQw$

Q. No: 04

What will be the effect of
 sediments particles diameter, particles
 density, particle concentration
 particle shape, viscosity of water,
 turbulence of water flowing in reservoir
 on fall velocity? explain in details.

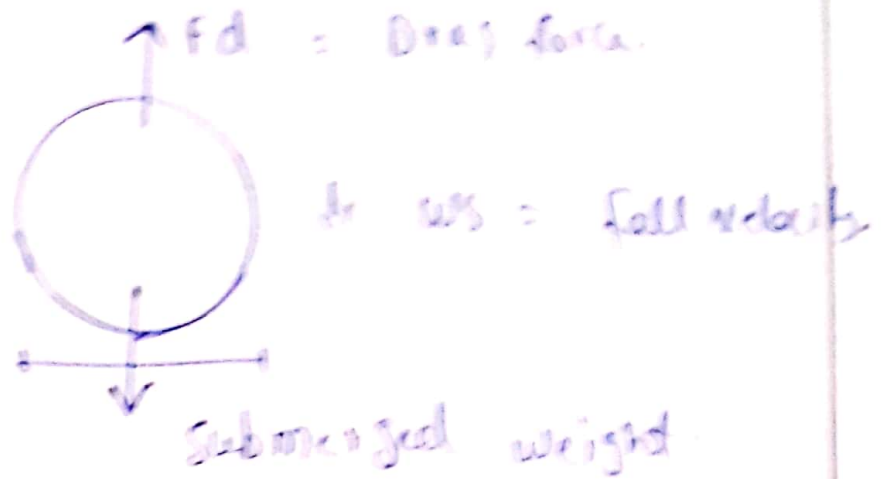
Fall velocity :-

When a grain falls down in still water
 it obtains a constant velocity when
 the upward fluid drag force on the
 grain is equal to the downward submerged
 weight of the grain. This constant
 velocity is defined as the fall velocity
 of the grain
 This is also called settling velocity

Fall velocity depends on -

- 1) Particle diameter.
- 2) Particle density
- 3) Particle concentration
- 4) Particle shape.

- 5) Viscosity slope of water. (Temperature)
- 6) Turbulence.



The force balance b/w the drag force and the submerged weight gives,

$$F_D = \text{Submerged weight.}$$

$$\frac{1}{8} C_D \rho \frac{\pi d^2}{4} w_s^2 = (\rho_s - \rho) g \frac{\pi d^3}{6}$$

$$A = \frac{\pi d^2}{4} \Rightarrow \text{projected area.}$$

$C_D = \text{Drag coefficient}$

$w_s = \text{Fall velocity of sediment}$

$\rho = \text{Density of water.}$

$\rho_s = \text{Density of sediment particle.}$

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⇒ Particle diameter:→

The diameter of the particle is directly proportional to the fall velocity b/c of greater the size of particle so it will tend to move faster as compared to the particles of small size. Thus there will be more gravitational force on particle of greater size so it will be more gravitational force on particle of greater size so it will fall quickly due to its weight.

Particle Density:→

Density of particle is directly proportional to the rate of fall velocity. Since particle with velocity density tends to settle down early compared with particle of low density.

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⇒ Particle Concentration: →
Concentration of Particle size will considerably affect its fall velocity as the section having greater concentration will be settled down at the place thus causing more fall velocity comparing with section of low concentration

Particle Shape:

Particles having regular shape tends to be effected more than irregular shape since regular shape particles have even surfaces which offer very little or no friction. While particles with irregular shape offer more friction as the particles with smaller surface area are more likely to be effected due to their resistance.

⇒ Viscosity of water:→

from the experimental study we can see that parameter such as temperature and pressure changes section of water having more temperature and pressure will fall objectively more due to increase in the kinetic energy so fall velocity will be more

⇒ turbulence of water:→

turbulence of water depends upon the different factor such as velocity. It will affect the fall velocity b/c of its zigzag motion. Thus the velocity of it varies at every point which is why it affects the fall velocity more. Increase in the kinetic energy tends to affect the fall velocity compared with steady fluid.