

Name	Usama Ayaz
ID	6977
Section	A
Paper	PRCD - 1
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Qno 2)

Ans 2)

A simply supported rectangular beam 16" ...  
of your final diagram.

Sol<sup>n</sup>:

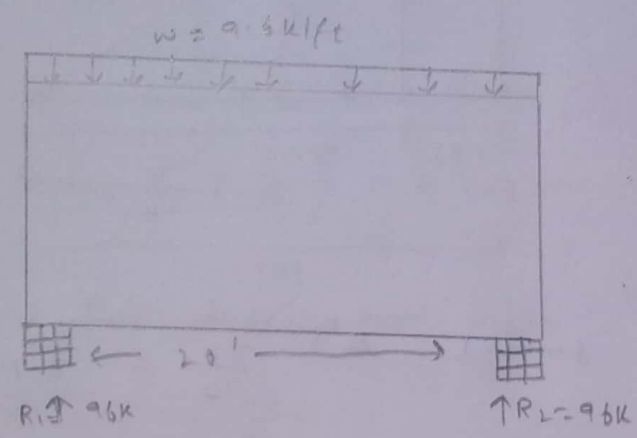
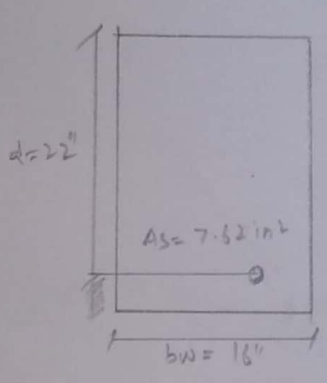
First of all find the unit load of beam

So  $b \times c$

$= \frac{16}{12} \times 150 \Rightarrow 200 \text{ lb/ft} = 0.2 \text{ k/ft}$

so total factored load =  $9.4 + 0.2$   
 $= 9.6 \text{ k/ft}$

$w = 9.6$



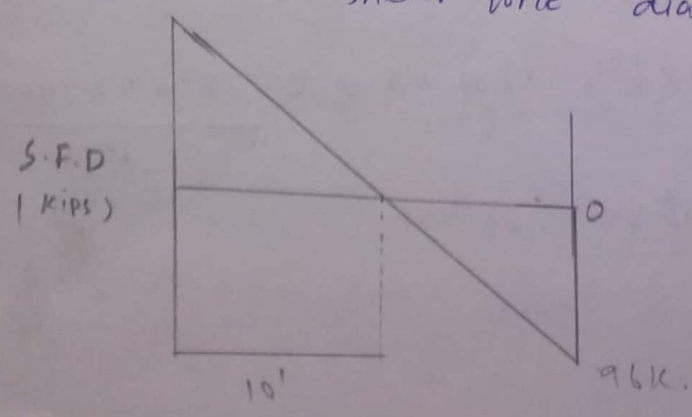
Step 1:-

Find the values of  $R_1$  &  $R_2$

total load =  $9.6 \times \frac{20}{2} = 96 \text{ k}$

Step 2:-

Draw its shear force diagram.

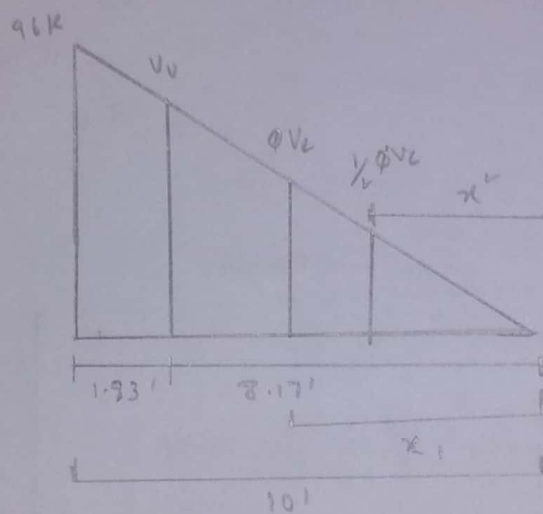


(2)

step 3r

Find the value of critical stress " $V_u$ "

and its location.

As we know that critical section is located at distance " $d$ " from face of support =  $9 - 22" = 1.83'$ value of critical shear at distance " $d$ " by similarity of triangles.

From similar  $\Delta$ 's  $\frac{96}{10} = \frac{V_u}{8.17}$

$$V_u = 78.43 \text{ k}$$

step 4r

Find the value of  $\phi V_c$  and  $\frac{1}{2} \phi V_c$  and  $\frac{1}{2} \phi V_c$ 

and also its distance from zero shear to right side.

$$\phi V_c = \phi \times 2 \times \sqrt{f'_c} \times b_w \times d \Rightarrow \frac{0.75 \times 2 \times \sqrt{4000} \times 16 \times 22}{1000}$$

$$\phi V_c = 33.40 \text{ k}$$

(3)

Location of  $\phi V_c$  by similarity of  $\Delta s'$

$$\frac{96}{10} = \frac{33.40}{x_1}$$

$$x_1 = 3.48'$$

Now  $\frac{1}{2} \phi V_c = \frac{33.40}{2} = 16.70 \text{ K}$

Location of  $\frac{1}{2} \phi V_c = \frac{96}{10} = \frac{16.70}{x_2}$

$$x_2 = 1.74'$$

STEP 5:-

Value of  $V_s$  ( $V_u = \phi V_s + \phi V_c$ )

$$\text{so } \phi V_s = V_u - \phi V_c$$

$$\phi V_s = 78.43 - 33.40$$

$$\phi V_s = 45.03 \text{ K}$$

STEP 6:- Check on section adequacy

$$\Rightarrow \phi \times 8 \times \sqrt{f'_c} \times b_w \times d = \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000}$$

$$= 133.57 \text{ K}$$

As  $\phi \times 8 \times \sqrt{f'_c} \times b_w \times d > \phi V_s \rightarrow$  It means section is adequate.

STEP 7:- Check on min spacing for stirrup:-

$$\phi \times 4 \times \sqrt{f'_c} \times b_w \times d = \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000} = 66.79 \text{ K}$$

As  $\phi 4 \sqrt{f'_c}$  bwd  $> \phi V_s = 45.03k$

Thus max spacing will be selected from the following for condition

$$1) \quad s_{max} = 24''$$

$$2) \quad \frac{d}{2} = \frac{22}{2} = 11''$$

$$3) \quad s_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$$

$$\therefore A_u = \frac{\pi}{4} \left( \frac{3}{8} \right)^2 = \frac{0.22 \times 60000}{0.75 \times \sqrt{14000} \times 16}$$

$$= 17.40''$$

$$A_u = 0.11 \times 2$$

$$A_u = 0.22$$

$$4) \quad s_{max} = \frac{A_u \times f_y}{50 \times b_w}$$

$$= \frac{0.22 \times 60000}{50 \times 16}$$

$$= 1650$$

From the above four condition, least value of spacing from #3, Ushaped will selected

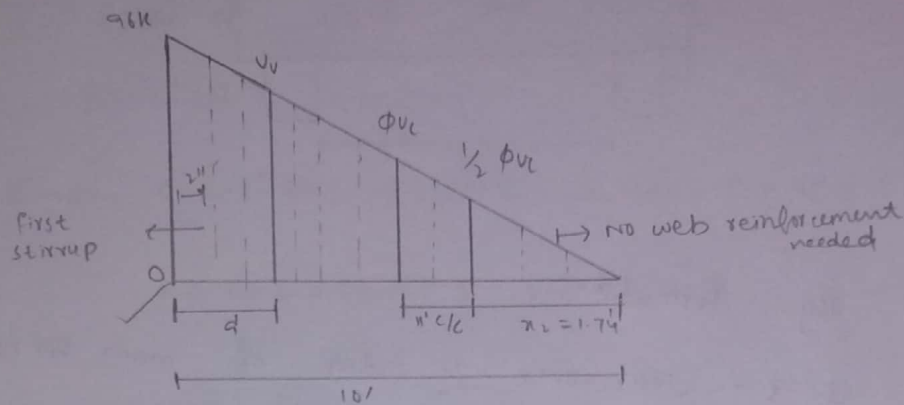
$$\text{So } s_{max} = 11'' \text{ c/c}$$

step # 8; spacing of stirrup from a critical section.

$$s = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40}$$

$$4.84'' \approx 5'' \text{ c/c}$$

Step 9: Find sketch

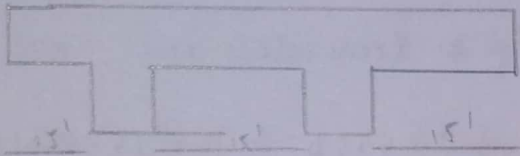


As we know that first stirrup from face of support

$$\Rightarrow \frac{5}{2} = 2.5 \approx 2''$$

Q no 1)

Ans 1) Solution:-



Step 1: Minimum thickness:-

By using formula

$$t_{min} = \frac{L}{28} = \frac{15}{28} = 6.4 \approx 6.5''$$

As  $f_y \rightarrow 40 \text{ ksi}$

so we will multiply a factor with this thickness

$$\text{Factor} = \left( 0.4 + \frac{f_y}{100} \right)$$

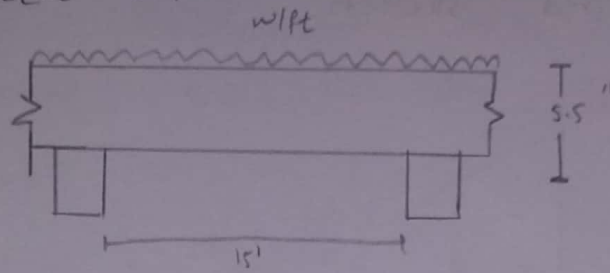
$$= 0.4 + \frac{40}{100} = 0.8$$

Hence the minimum thickness will be

$$6.5 \times 0.8$$

$$t_{min} = 5.2 \approx 5.5''$$

STEP 2:- Effective Depth.



By formula

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bars})$$

$$= 5.5 - 0.75 - \frac{1}{2} \left( \frac{5}{8} \right)$$

$$d \approx 4.5''$$

STEP 3 :- (self wt of slab)

By formula

$$\frac{t}{12} + \gamma_{\text{concrete}}$$

$$\frac{5.5}{12} \times 150 = 68.75 \text{ lb/ft}^2$$

STEP 4:- Total factored load,

$$\text{Factored live load} = 160 \text{ lb/ft}^2$$

Hence the minimum thickness will be

$$6.5 \times 0.8$$

$$t_{\text{min}} = 5.2 \approx 5.5''$$

So the factored dead load will be

$$D.L = 1.2 (20 + 68.75) = 106 \text{ lb/ft}^2$$

$$\text{total factored load} = D.L + L.L$$

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft}^2 = 0.2665 \text{ k/ft}^2$$

(7)

Step 5:- ultimate moment

By using formula

$$M_u = \frac{W_u \times L^2}{8} = \frac{0.2665 \times (15)^2}{8} \times 12$$

$$= 89.94 \text{ kip-inches}$$

Step 6:- Area of steel for main bars by trial  
 $\Sigma$  repeat method.

Trial #01:-

let depth of compression block

$$a = 0.2 \times t$$

$$= 0.2 \times 5.5 = 1.1''$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})}$$

Trial #02

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12}$$

$$= 0.62 \text{ in}$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.6}{2})}$$

$$A_{st} = 0.59 \text{ in}^2$$

Trial 3:-

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.507}{2})} = 0.59 \text{ in}^2$$



8

so we will use  $A_{st} = 0.59 \text{ in}^2$

step # 07:-

Area of steel for distribution reinforcement

By formula

$$A_{min} = 0.002 \times b \times t \rightarrow (\text{for grade 40 steel})$$

$$= 0.002 \times 12 \times 55 \Rightarrow 0.132 \text{ in}^2$$

step 8:-

spacing for main bars.

By formula

$$A_{min} = 0.002 \times b \times t \rightarrow \text{for grade 40 steel}$$

$$0.002 \times 12 \times 55 \Rightarrow 0.132 \text{ in}^2$$

$$\text{spacing} = \frac{A_b}{A_{st}} \times 12$$

we use #6 bar dia =  $\left(\frac{6}{8}\right)''$

$$\text{Area} = \frac{\pi}{4} \left(\frac{6}{8}\right)^2 = 0.442 \text{ in}^2$$

step 9:-

spacing for distribution bars.

$$\text{spacing} = \frac{A_b}{A_{st}}$$

we use #5 bars so

$$\text{dia} = \left(\frac{5}{8}\right)'' , \text{Area} = \frac{\pi}{4} \left(\frac{5}{8}\right)^2 = 0.31 \text{ in}^2$$

$$\text{spacing} = \frac{0.31}{0.132} \times 12 = \frac{28.1''}{\cancel{28.1}} \approx 28'' \text{ c/c}$$

step #10:-

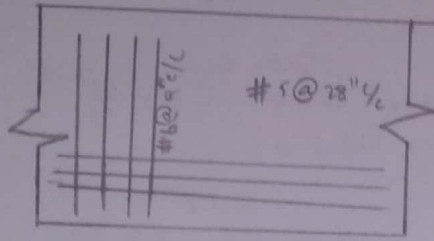
Find sketch

$$f'c = 4 \text{ ksi} , f_y = 40 \text{ ksi}$$

Main steel #6 at 9" c/c

Distribution steel #5 at 28" c/c

(a)



Qn03)

Ans3) Step 1:-

Find gross area of concrete

$$A_g = b \times b \text{ (since it is square tied column)}$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step 2:-

Find area of steel

$$\text{since } A_s = 5\% \text{ of } A_g$$

$$= 0.05 \times 144$$

$$A_s = 7.2 \text{ in}^2$$

Step 3:-

Ultimate load carrying capacity

$$P_u = \phi \times 0.80 \times [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y]$$

$$= 0.65 \times 0.80 [0.85 \times 4 [1144 - 7.2] + 7.2 \times 60]$$

$$P_u = 466.50 \text{ k}$$

Step 4:- sketch & design of ties (c/c distance)

From below values we choose the

least value of all these.

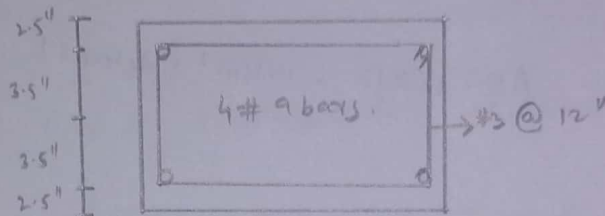
(10)

1)  $16 \times \text{dia}$  of long bar =  $16 \times \frac{9}{8}$   
=  $18''$

2)  $48 \times \text{dia}$  of tie bar =  $48 \times \frac{3}{8}$   
=  $18''$

3) least column dimension =  $12''$

so c/c b/w ties =  $12''$



since it is a tied square column so there is no spiral stirrup used, the stirrup used is of rectangular shape due to the specification of the structure thus we will use tie stirrups instead.

Qno 4)

Ans 4) step 1r let  $h = 24''$

Step # 2r

Total weight = wt of soil + wt of RC

=  $3 \times 120 + 2 \times 150$

=  $660 \text{ psf} = 0.660 \text{ ksi}$

(11)

STEP 3:- Effective bearing capacity

$$q_{ve} = q_a - u$$
$$= 2.50 - 0.660$$
$$q_{ve} = 1.84 \text{ ksi}$$

STEP 4:- Required area for foundation.

$$\text{Area} = \frac{\text{Service load}}{q_{ve}} = \frac{100 + 120}{1.84}$$
$$= 119.57 \text{ ft}^2$$

STEP 5:- Since foundation is square

$$\text{Area} = b \times b = 119.57 \Rightarrow B \approx 11'$$

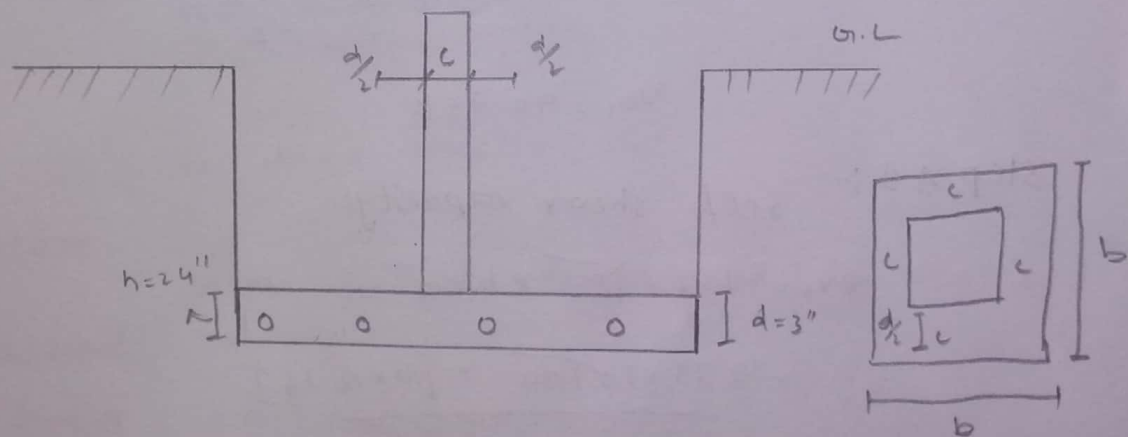
STEP 6:- upward bearing capacity of soil

$$q_{vup} = \frac{\text{Factored load}}{(B)^2} = \frac{1.2 \times 100 + 1.6 \times 120}{11^2}$$

$$q_{vup} = 2.58 \text{ k/ft}^2$$

STEP 7:- Punching shear

$$b_o = 4 \times (l + d)$$



$$d = h - c.c - \text{dia of bar} = \frac{1}{2} db$$

$$\therefore \text{Take \#8 bar} \\ \text{dia} = \frac{8}{8} = 1''$$

$$= 24 - 3 - 1 - \frac{1}{2}(1) = 19.5''$$

$$b_o = 4 \times (16 + 19.5) = 142''$$

Step #8:-

$$V_{U2} = q_{UP} \times \left[ B^2 - (c+d)^2 \right] \\ = 2.58 \times \left[ 11^2 - \frac{(16+19.5)^2}{12} \right]$$

$$V_{U2} = 289.60 \text{ k}$$

Step #9:-

$$\phi V_{cp} = \phi \times 4 \times \sqrt{f'_c} \times b \times d \\ = \frac{0.75 \times 4 \times \sqrt{4000} \times 142 \times 19.5}{1000}$$

$$\phi V_{cp} = 525.38$$

Step 10:-

Beam shear / one way shear check

$$V_{U1} = q_{UP} \times B \times \left[ \frac{B}{2} - \frac{c}{2} - d \right]$$

$$V_{U1} = 2.58 \times 11 \times \left[ \frac{11}{2} - \frac{16}{2} - 19.5 \right]$$

$$V_{U1} = 90.95 \text{ k}$$

Step 11:- self shear capacity:-

$$\phi V_c = \phi \times 2 \times \sqrt{f'_c} \times b \times d \\ = \frac{0.75 \times 2 \times \sqrt{4000} \times 11 \times 12.16}{1000}$$

$$= 110.04 \text{ k} > V_{U1} \Rightarrow \text{D.K}$$

Step 12 ultimate moment

$$M_u = \frac{w_u p l B}{8} \times (B - c)^2 = \frac{2.58 \times 11}{8} \times \left(11 - \frac{1.6}{12}\right)^2$$

$$M_u = 331.49 \text{ k}' \approx 3977.93 \text{ k}$$

Step 13:- Area of steel for main bars by Trial & repeat method.

Trial #1:-

$$\text{let } a = 0.2 \times h = 0.2 \times 24 = 4.8''$$

$$A_s = \frac{M_u}{\phi \times f_y \times \left(d - \frac{a}{2}\right)} = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{4.8}{2}\right)} = 8.56 \text{ in}^2$$

Trial #2:-

$$a = \frac{A_s \times f_y}{0.85 \times f_c' \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.53''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)} = \boxed{7.197 \text{ in}^2}$$

Trial No 3:-

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.28}{2}\right)} = 7.1 \text{ in}^2$$

so that area = 7.1 in<sup>2</sup>

STEP 14:-

check the min reinforcement by the 03 method

$$\begin{aligned} a) A_{s, \min} &= 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24 \\ &= 5.70 \text{ in}^2 \end{aligned}$$

$$B) A_{smin} = \frac{200}{f_y} \times B \times d = \frac{200}{60000} \times (11 \times 12) \times 19.5$$

$$= 8.58 \text{ in}^2$$

$$C) A_{smin} = \frac{3 \times \sqrt{f'_c}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000}}{60000} \times (11 \times 12) \times 19.5$$

$$= 7.05 \text{ in}^2$$

From above value greater value will be selected thus  $A_{smin} = 8.58 \text{ in}^2$

STEP 15: using #8 bar

$$A_b = 0.785 \text{ in}^2$$

$$\text{No of bars} = \frac{A_s}{A_b} = \frac{8.58}{0.785} = 10.92 \approx 11 \text{ bars in each direction}$$