

NAME : SALMAN RASHID

SUBMITTED By : 7845

SUBMITTED TO : Sir. Anwar Shmim

SUBJECT : P & Statistics

SEMSTER : Summer

Date : ~~23 sept~~ 23 Sept 2020

Q1: Compare & analyse the result of the least square regression equation & coefficient of correlation of "y" on "x" of the following data

Compare your manual results with the outcome of SPSS?

Solution:

X	Y	XY	X ²
53	20	1060	2809
62	32	1984	3844
57	45	2565	3249
71	60	4260	5041
78	80	6240	6054
45	100	4500	2025
86	120	10320	7396
87	140	12180	7596
96	160	15360	9216
91	180	16380	8281
94	200	18800	8836
94	210	19740	8836
$\Sigma = 914$	$\Sigma = 1347$	$\Sigma = 104929$	$\Sigma = 72183$

$$y = a + bx \quad \text{--- (i)}$$

$$a = \bar{y} - b\bar{x} \quad \text{--- (ii)}$$

$$\text{So } \bar{y} = \frac{\sum y}{n} = \frac{1347}{12} = 112.25 \quad \text{--- (iii)}$$

$$\bar{x} = \frac{\sum x}{n} = \frac{914}{12} = 76.16 \quad \text{--- (iv)}$$

where

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12 [104929] - [1231158]}{12 [73183] - [835396]}$$

$$\boxed{b = 0.6539} \rightarrow \text{(v)}$$

Putting eq (iii), (iv) & v
in eq (i)

$$a = \bar{y} - b\bar{x}$$

$$a = 112.25 - 0.6539(76.16)$$

$$a = 62.448$$

- a A box contains 4 red, 4 white and 5 green balls. Three balls are drawn from the box together. Find the Probability that they may be (i) all of different colours (ii) all of the same colours.?

Solution :

(i) $n(S) = \binom{13}{3} = 286$

let $A =$ Draw all balls are Different Colours

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = \boxed{0.28}$$

(ii)

let $B =$ Draw all balls of same colours Red

white Green

$$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$$

$$= \binom{4}{3} + \binom{4}{3} + \binom{5}{3} =$$

$$4 + 4 + 10 = 18$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{18}{286} = \text{~~0.063~~}$$

$$\boxed{0.063}$$

(ii) Of 12 eggs in a basket, 2 are hard. From these 4 eggs are chosen at random to make a cake without replacement. Find the probabilities that (i) exactly one is hard (ii) At least one is hard?

Solution:

$$n(S) = \binom{12}{4} = 495$$

Let A = Denote the event

The exactly one egg is hard

$$n(A) = \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{240}{495} = \boxed{0.48}$$

Let B = be the event at
Least one eggs is hard
is selected

$$n(B) = \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2}$$

$$= 2 \times 120 + 1 \times 45 = 240 + 45 = 285$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{285}{495} =$$

$$\boxed{0.576}$$

Q3. The following are the score made by three batsmen A, B & C in a series of innings.

A = 12 15 6 73 7 10 (45) 199 36 84 29

B = 47 12 76 48 4 (45) 37 48 13 2

C = 15 23 52 4 24 (45) 74 52 13 4

(a) Find the range of batsmen

(b) who is consistent player?

(c) compare A with B, B with C & A with C?

Sol:-

A	B	C
12	47	15
15	12	23
6	76	52
73	48	4

A	B	C
27	4	29
45	45	45
199	37	74
36	48	52
84	13	13
29	3	4

$$\text{Range} = X_m - X_o$$

$$\begin{aligned} \text{Range of A} &= X_m - X_o \\ &= 199 - 6 \\ &= 193 \end{aligned}$$

$$\begin{aligned} \text{Range of B} &= X_m - X_o \\ &= 45 - 3 \\ &= 42 \end{aligned}$$

$$\begin{aligned} \text{Range of C} &= X_m - X_o \\ &= 45 - 4 \\ &= 41 \end{aligned}$$

Batsmen A		Batsmen B		Batsmen C	
X	X ²	Y	Y ²	Z	Z ²
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
7	49	4	16	24	576
45	2025	45	2025	45	2025
149	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma X = 506$	$\Sigma X^2 = 56602$	$\Sigma Y = 333$	$\Sigma Y^2 = 16325$	$\Sigma Z = 306$	$\Sigma Z^2 = 4440$

Now.

Batsmen A:

$$\bar{x} = \frac{\Sigma x}{n} \quad n = 10$$

$$= \frac{506}{10} = 50.6$$

$$s_x = \sqrt{\frac{\Sigma x^2}{n} - \left(\frac{\Sigma x}{n}\right)^2}$$

$$S_x = \sqrt{\frac{56602}{10} - \left(\frac{506}{10}\right)^2}$$

$$= \sqrt{\frac{56602}{10} - \left(\frac{506}{10}\right)^2}$$

$$S_{\bar{x}} = 56.676$$

$$C.V = \frac{56.676}{\bar{x}} \times 100$$

$$= \frac{56.676}{50.6} \times 100$$

$$C.V = 112.007$$

Batsmen B :

$$y = \frac{\sum Y}{n} = \frac{333}{10} = 33.3$$

$$S_Y = \sqrt{\frac{\sum Y^2}{n} - \left(\frac{\sum Y}{n}\right)^2}$$

$$S_Y = \sqrt{\frac{16325}{10} - \left(\frac{333}{10}\right)^2}$$

~~$$S_Y = \sqrt{\quad}$$~~

$$S_Y = 22.88$$

$$C.V = \frac{22.88 \times 100}{33.3} = 68.708$$

Batsmen C

$$\bar{Z} = \frac{\sum Z}{n} = \frac{306}{10} = \underline{30.6}$$

$$S_Z = \sqrt{\frac{\sum Z^2}{n} - \left(\frac{\sum Z}{n}\right)^2}$$

$$S_z = \sqrt{\frac{14440}{10} - \left(\frac{306}{10}\right)^2}$$

$$S_z = \frac{7\sqrt{259}}{5}$$

$$S_z = 22.53$$

$$C.V = \frac{S_z}{\bar{z}} = \frac{22.53}{30.6} \times 100$$

$$C.V = 73.627$$

Batsmen B is more consistent as its value of variance is smallest.

Compare "A" with "B"

"B" is consistent

Compare 'B' with 'A'

"B" is more consistent

Compare "A" with "C"

"C" is more consistent.