

④

Name

Asim Ali

ID

7763

Sec

C

Exam Type

Improvement for  
GPA (Summer 2020)

Paper

Structural Analysis<sup>(II)</sup>

Submitted to

Engr. Adeed Khan

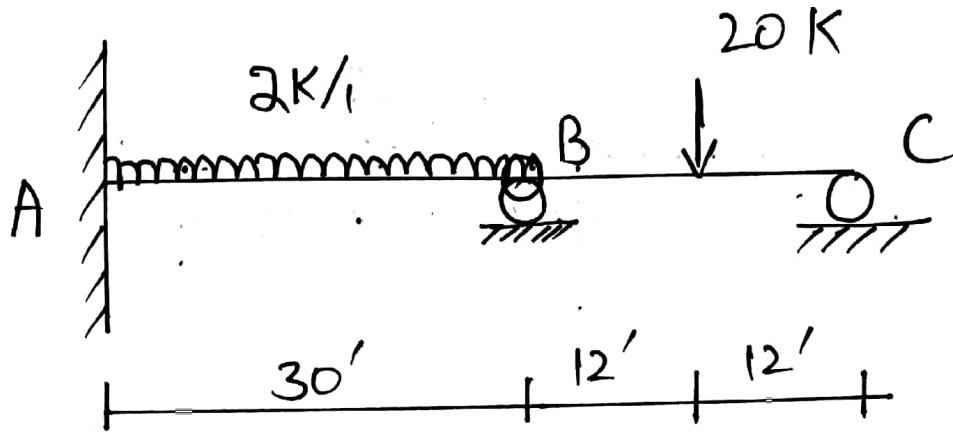
Department

BS Civil

INU Peshawar

Q: NO 1

(2)



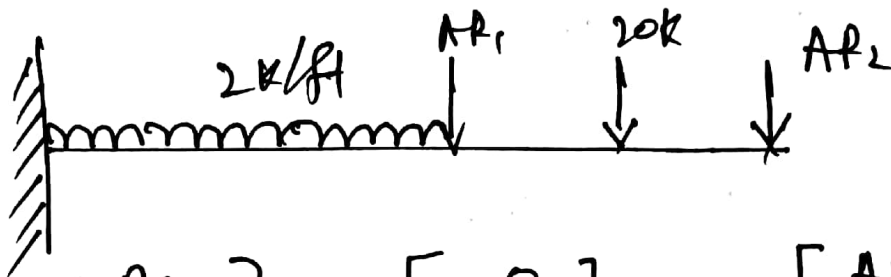
Required:

Analyze the given beam by flexibility method.  $EI$  is constant

Solution:

Structural Indeterminacy = 2°

Step # 1 Select Redundant Actions

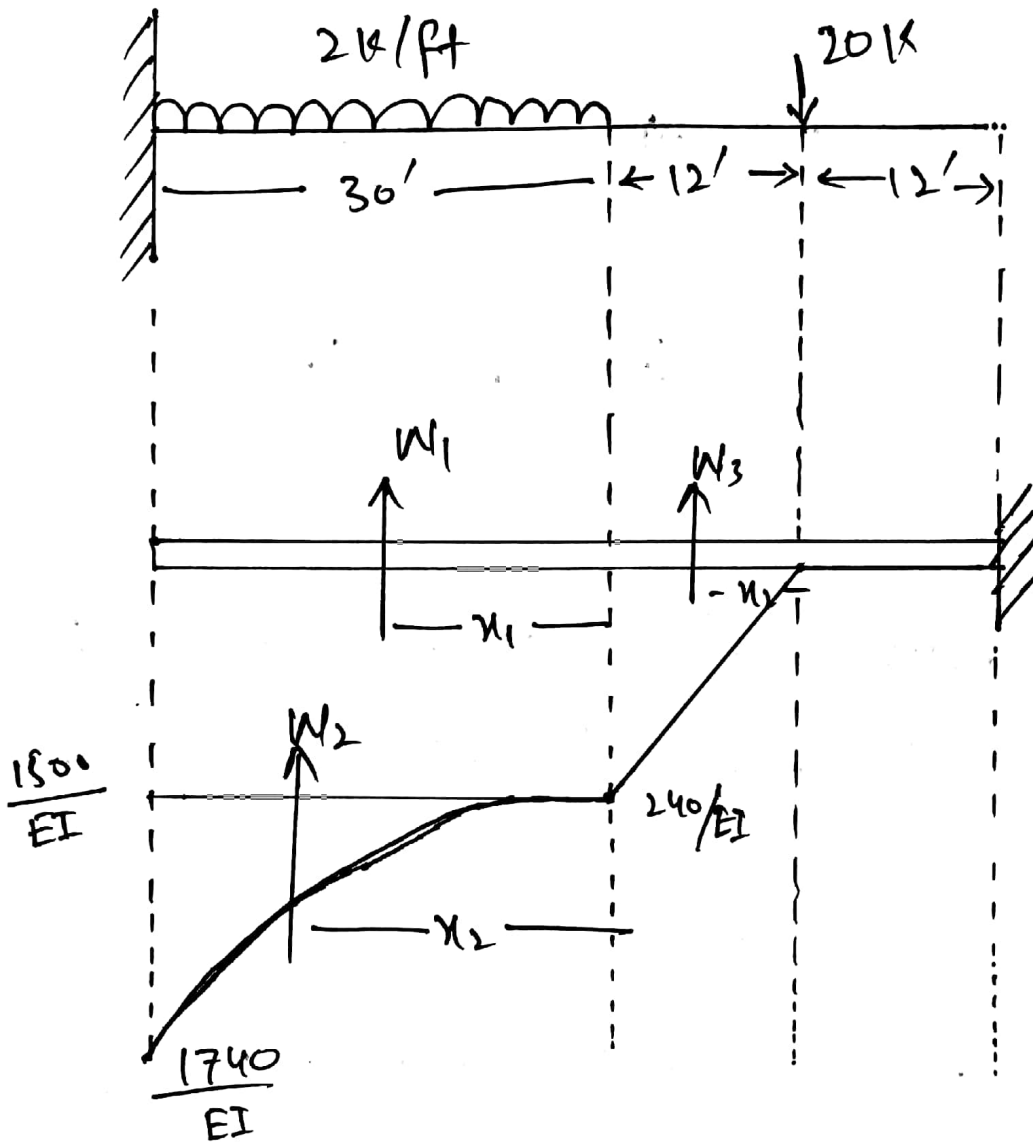


$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + [F] \times [AR]$$

3

Step #02 Compute the values of [DRL]



$$W_1 = 1500 \times 30 = 45000$$

$$20 \times 12 = 240$$

$$20 \times (12 + 30) +$$

$$2 \times 30 \times 15 = 1740$$

$$W_2 = \frac{1}{3} \times 30 \times 240 = 2400$$

$$W_3 = \frac{1}{2} \times 12 \times 240 = 1440$$

$$x_1 = \frac{b}{2} = \frac{30}{2} = 15'$$

$$x_2 = \frac{3}{n+2} \times L = \frac{3}{2+2} \times 30 = 22.5'$$

$$x_3 = \frac{2}{3} \times L = \frac{2}{3} \times 12 = 8'$$

Now finding DRL

$$\begin{aligned} DRL_2 &= W_1 \times (x_1 + 24) + W_2 \times (x_2 + 24) + \\ &W_3 \times (x_3 + 12) \\ &= 45000(15+24) + 2400(22.5+24) + \\ &1440(8+12) \\ &= 1755000 + 11600 + 28800 \end{aligned}$$

$$DRL_2 = 1895400 / EI$$

$$\begin{aligned} DRL_1 &= W_1(x_1) + W_2(x_2) \\ &= 45000(15) + 2400(22.5) \\ &= 675000 + 54000 \\ &= 729000 \end{aligned}$$

So

$$DRL = \frac{1}{EI} \begin{bmatrix} 729000 \\ 1895400 \end{bmatrix}$$

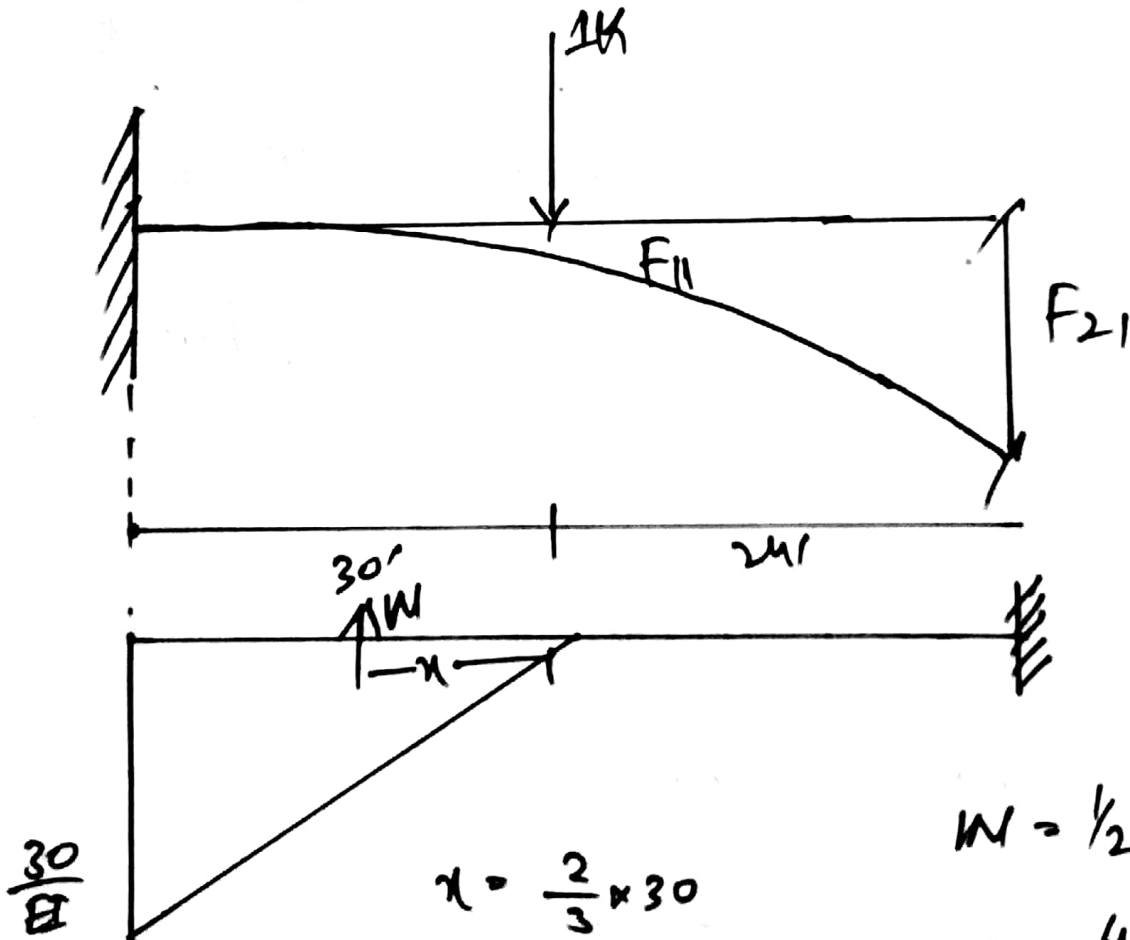
Step # 03

(5)

Flexibility Matrix

$$[F]_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

a) Applying unit load on  $AR_1$



$$x = \frac{2}{3} \times 30$$

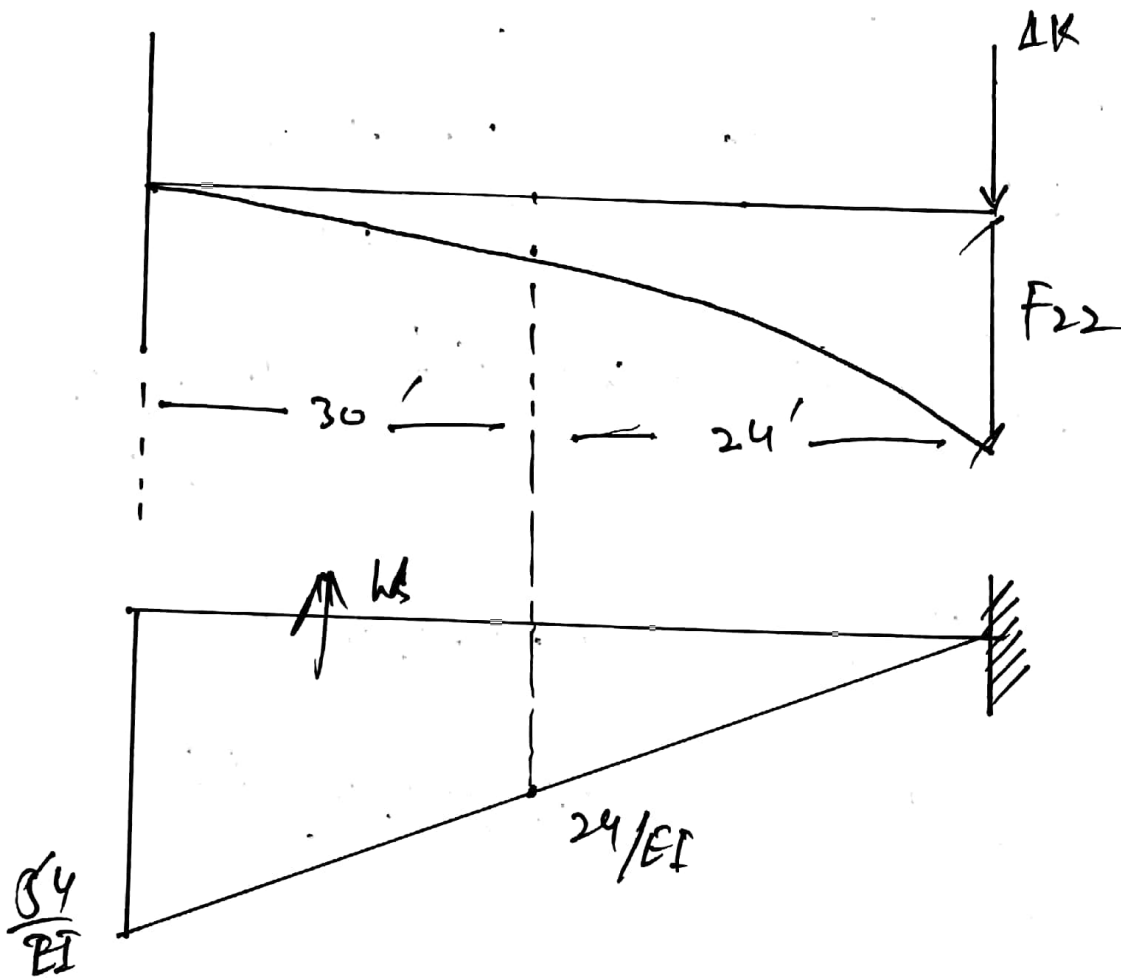
$$x = 20'$$

$$W = \frac{1}{2} \left( \frac{30}{EI} \times 30 \right) = 450/EI$$

$$F_{11} = \frac{450}{EI} (20) = 9000/EI$$

$$F_{21} = \frac{450}{EI} (20 + 24) = 19800/EI$$

Now Apply unit load (6) on  $AB_2$



$$W = \left( \frac{54 + 24}{2EI} \right) \times 30$$

$$= 1170/EI$$

Now the Distance,

$$x = \frac{L}{3} \left[ \frac{b + 2(a)}{a + b} \right]$$

(7)

$$= \frac{30}{3} \left[ \frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$\Rightarrow F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19796.4}{EI}$$

$$\Rightarrow F_{22} = \frac{1170}{EI} \times \{(16.92) + (24)\} = \frac{47876.4}{EI}$$

Hence

$$F_{2 \times 2} = \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix} \frac{1}{EI}$$

Step # 4

Compute the values of AR

$$[DRS] = [DRL] + [F] \times [AR]$$

$$[AR] = [DRS - DRL] \times [F]^{-1}$$

$$[F]^{-1} = \frac{1}{|F|} \times \text{Adj } F$$

⑧

$$= \frac{1}{\begin{vmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{vmatrix}} \times \text{Adj} \begin{bmatrix} 9000 & 19796.4 \\ 19800 & 47876.4 \end{bmatrix}$$

$$|F| = (9000 \times 47876.4 - 19796.4 \times 19800)$$

$$= (430887600 - 391968720)$$

$$\Rightarrow |F| = 38918880$$

$$\Rightarrow \text{Adj } A = \begin{bmatrix} 0 & -729000 \\ 0 & -1895400 \end{bmatrix} \times \frac{1}{EI} \times \frac{1}{38918880}$$

$$\Rightarrow \text{Adj } A = \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 0 & -729000 \\ 0 & -1895400 \end{bmatrix} \frac{1}{EI} \times \frac{1}{38918880} \begin{bmatrix} \checkmark \\ \checkmark \end{bmatrix}$$

$$= \begin{bmatrix} -729000 \\ -1895400 \end{bmatrix} \frac{1}{EI} \times \begin{bmatrix} 47876.4 & -19796.4 \\ -19800 & 9000 \end{bmatrix}$$

38918880

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 66.193 \\ -67.505 \end{bmatrix}$$

The End.



9

Q.NO:2

Differentiate between force Method and displacement method.

Force Method

$$D_s < D_k$$

Forces are redundant  
or unknowns

Starts with equilibrium  
of forces.

Forces found by  
compatibility equations  
of displacements

$$\text{no. of redundants} = D_s$$

not suitable for  
computer

Displacement Method

$$D_s > D_k$$

Displacements are  
redundant or unknowns

Starts with compatible  
deformations

Displacements found  
by equilibrium equations  
of forces

$$\text{no. of redundants} = D_k$$

not suitable for  
truss.

(11)

## Force Method

- i) Method of consistent deformation
- ii) Theorem of least work
- iii) Column analogy method
- iv) Flexibility Matrix Method

## Displacement Method

- i) Slope deflection method
- ii) Moment of distribution method
- iii) Kani's method
- iv) Stiffness matrix method

Q:2 Part (B)

(12)

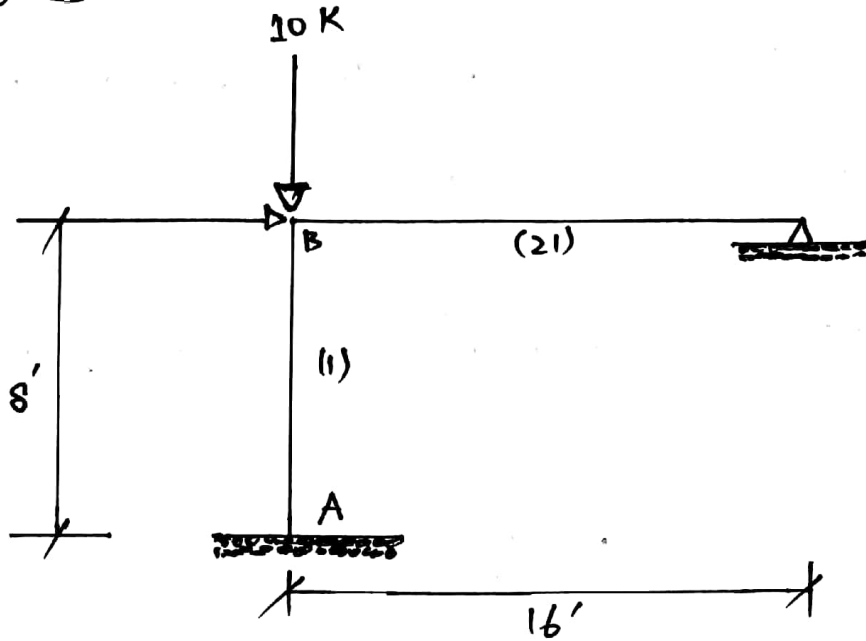
Which method is more suitable :

Stiffness Method also called Displacement Method is more suitable for structure analysis matrix approach, as it is a primary method used in matrix analysis. The main advantage of this method over flexibility method is that it is conducive to computer programming. Once the analytical model of the structure has been defined, no further engineering decisions are required in the stiffness method in order to carry out the analysis.

(13)

Q NO: 3

(14)



Required:

Analyse the rigid-joint frame by flexibility Method. Assume  $EI$  is constant, for all members.

Solution:

$$E = \text{constant}$$

$$I_c = I$$

$$I_B = 2I$$

Total Statical Indeterminacy

$$\Rightarrow R - 3 = 5 - 3 = 2$$

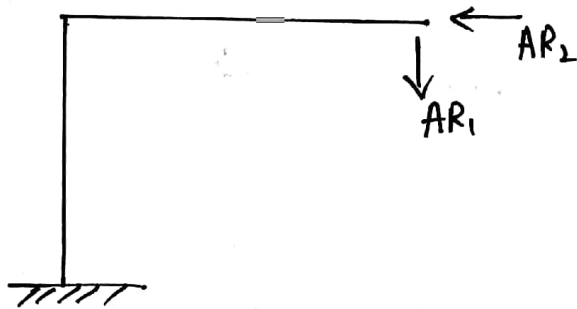
Step # 01

(15)

Identify <sup>Total</sup> Statical Indeterminacy

$$\Rightarrow R - 3 = 5 - 3 = 2^{\circ}$$

Identify Redundant Actions



$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Step # 02

Compute Value of  $[DRL]$

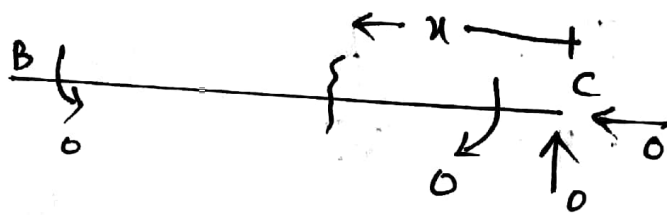
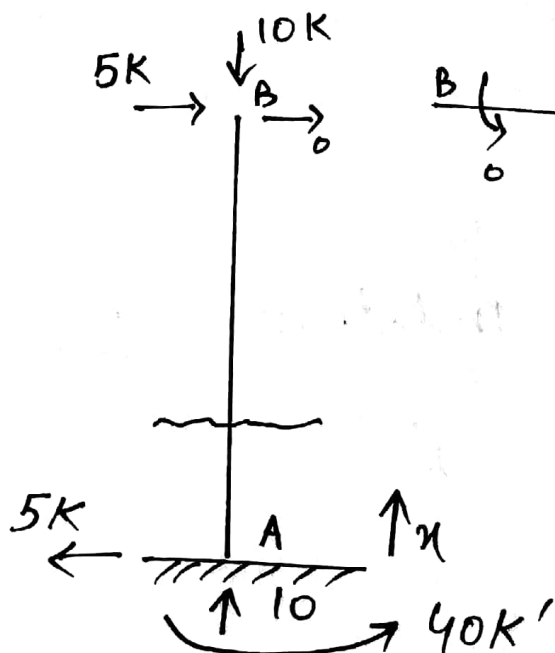


Fig : AML Values  
(M-values)

Step # 03

[F] <sup>(16)</sup> 0Y [AMR]

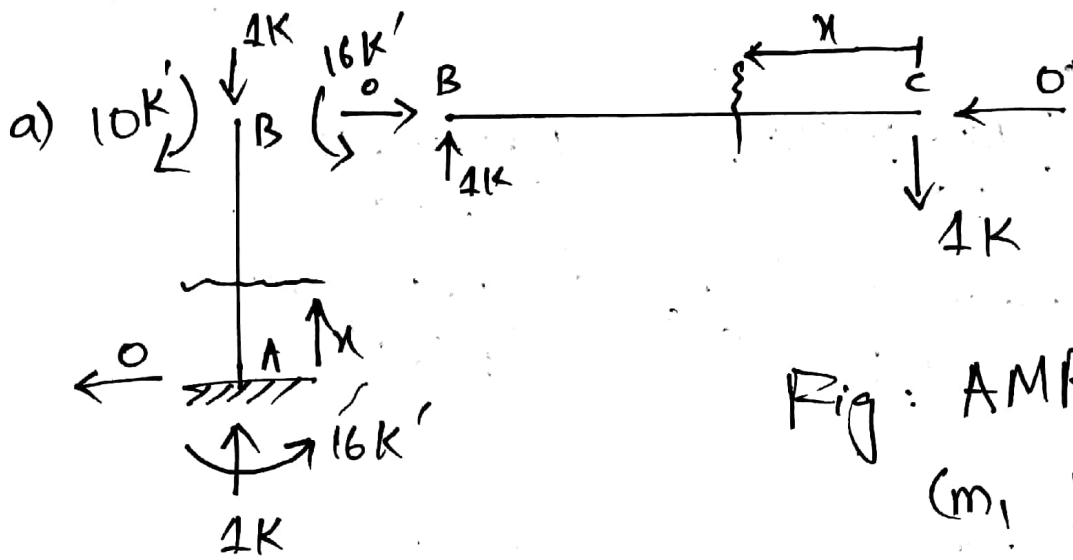


Fig: AMR-Values  
( $m_1$  values)

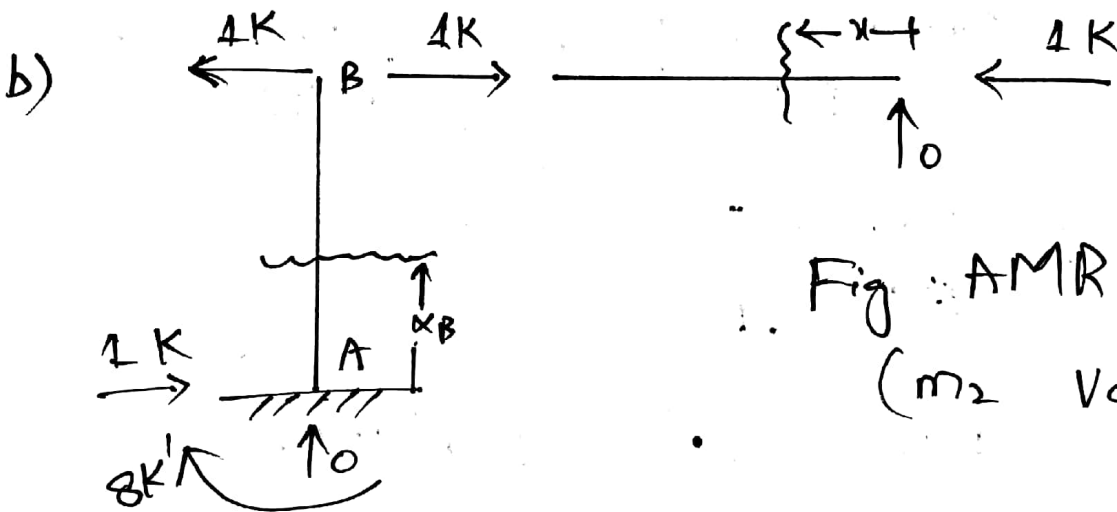


Fig: AMR values  
( $m_2$  values)

Member

Select origin  
(should be select  
the support)

← Origin

Limits

I

← M

Take x-section  
from origin  
AML Fig and  
Find moment

$m_1$

$m_2$

AB

A

0-8

I

$5x - 40$

-16

8-x

BC

C

0-16

2I

0

x →

0

Take x  
section  
on  $m_2$   
Fig from  
the origin



(17)

⇒ For Finding Values of DRL:

$$\begin{aligned} DRL_1 &= \int_0^8 \frac{M_{AB} \cdot m_1(CAB)}{EI} dx + \int_0^{16} \frac{M_{BC} \cdot m_2(CBC)}{EI} dx \\ &= \int_0^8 \frac{(5x-40)(-16) dx}{EI} + \int_0^{16} \frac{0 \cdot x}{E(2I)} dx \end{aligned}$$

$$DRL_1 = \frac{2560}{EI}$$

$$DRL_2 = \int_0^8 \frac{(5x-40)(8-x) dx}{EI} + \int_0^{16} \frac{0 \cdot 0}{E(2I)} dx$$

$$DRL_2 = \frac{-853.33}{EI}$$

⇒ Compute Flexibility Matrix:

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

$$\Rightarrow F_{11} = \int_0^8 \frac{m_1^2(CAB)}{EI} dx + \int_0^{16} \frac{m_2^2(CBC)}{EI} dx = \int_0^8 \frac{(-16)^2}{EI} dx + \int_0^{16} \frac{x^2}{E(2I)} dx$$

$$F_{11} = \frac{2730.67}{EI}$$

$$F_{12} = F_{21} = \int_0^8 m_1(CAB) \cdot m_2(CAB) dx + \int_0^{16} m_1(CBC) \cdot m_2(CBC) dx$$

$$= \int_0^8 \frac{(-16)(8-x)}{EI} dx + \int_0^{16} \frac{(x)(0)}{2EI} dx.$$

$$F_{12} = F_{21} = \frac{-512}{EI}$$

$$F_{22} = \int_0^8 (m_2)_{AB}^2 dx + \int_0^{16} (m_2)_{BC}^2 dx$$

$$= \int_0^8 \frac{(8-x)^2}{EI} dx + \int_0^{16} \frac{0^2}{2EI} dx$$

$$F_{22} = 170.67$$

As we know that

$$[DRS] = [DRL] + [AR] \times [F]$$

$$\Rightarrow [AR] = \frac{[DRS] - [DRL]}{[F]}$$

$$\Rightarrow [AR] = [F]^{-1} \times [DRS - DRL]$$

$$= \begin{bmatrix} 2730.67 & -515 \\ -512 & 170.67 \end{bmatrix}^{-1} \times \begin{bmatrix} 0 & -2560 \\ 0 & +853.33 \end{bmatrix}$$

(19)

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} -0.00005 \\ 4.997 \end{bmatrix} = \begin{bmatrix} 0 \\ 5 \end{bmatrix}$$

The End

Asim Ali  
for  
(Improvement)