

Course Title: Electrical Network Analysis Module: B-tech

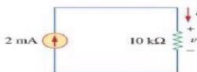
Instructor: Total Marks: 30

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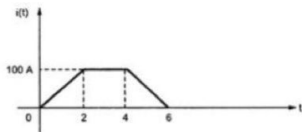
Q1 (a) For the circuit shown below, calculate the voltage V , the conductance G , and Marks 05 the power P .



(b) A resistor absorbs an instantaneous power of when connected to a voltage Marks 05 source. Find I and R ?

Q2 (a) The current in a $4H$ inductor raises at a rate of $4A/s$. Find the voltage across the Marks 04 inductor the energy stored in the magnetic field at after $2sec$.

(b) A current waveform flowing through an inductor of $1mH$ is shown in the figure. Obtain and sketch the waveform of voltage across the inductor.



Marks 06

Q3 (a) A series RLC circuit containing a resistance of 12Ω , an inductance of $0.15H$ and a Marks 07 capacitor of $100\mu F$ are connected in series across a $100V, 50Hz$ supply. Calculate the total circuit impedance, the circuits current, power factor and draw the voltage phasor diagram.

$R=12\ \Omega, L=0.15H, C=100\ \mu F, V_s=100V, 50Hz$

①

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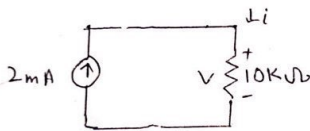
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Question #01

(a) For the circuit show below,
Calculate the Voltage V , Conductance G ,
and the power P .



Solution:

$$V = IR$$

$$V = (2 \times 10^{-3})(10 \times 10^3)$$

$$V = 2 \times 10 \times 10^{-3+3}$$

$$V = 20V$$

As we know that Capacitance is a
Reciprocal of Resistance

So,

$$R = \frac{1}{C}$$

②

$$\frac{I}{C} = \frac{V}{I}$$

$$\Rightarrow C = \frac{I}{V}$$

$$C = \frac{2 \times 10^{-3}}{20}$$

$$C = 0.0001$$

$$C = 1 \text{ mF}$$

Now

$$\text{Power} = V \times I$$

$$= 20 \times 2 \times 10^{-3}$$

$$= 40 \times 10^{-3}$$

$$P = 40 \text{ mW}$$

③

Question # 01

(b) A Resistor absorbs an instantaneous Power of $20 \cos^2(t)$ mW when connected to a Voltage source $V = 10 \cos(t)$ V.
Find I & R ?

Solutions:

Given a resistor absorbs an instantaneous power of $20 \cos^2(t)$ mW

$$P = 20 \cos^2(t) \text{ mW}$$

given Voltage source is

$$V = 10 \cos(t) \text{ V}$$

$$I = \frac{P}{V}$$

$$I = \frac{20 \cos^2(t) \times 10^{-3}}{10 \cos(t)}$$

$$I = 2 \cos(t) \times 10^{-3} \text{ A}$$

$$I = 2 \cos(t) \text{ mA}$$

④

$$V = IR$$

$$R = \frac{V}{I}$$

$$R = \frac{10 \cos(t)}{2 \cos(t) \times 10^3}$$

$$R = 5 \times 10^3 \Omega$$

$$R = 5 \text{ k}\Omega$$

Question # 02

(a) The current in a 4H inductor raises at a rate of 4 A/s. Find the voltage across the inductor the energy stored in the magnetic field at after 2 sec?

Solution:

$$L = 4 \text{ H}$$

$$\frac{di}{dt} = 4 \text{ A/s}$$

⑤

So

$$\text{Voltage} = L \frac{di}{dt}$$

$$= 4 \times 4$$

$$= 16 \text{ V}$$

$$W = \frac{1}{2} Li^2$$

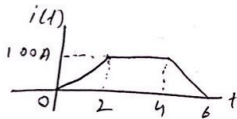
$$= \frac{1}{2} 4(4)^2$$

$$= \frac{1}{2} 4^2 \times 16$$

$$W = 32 \text{ J}$$

Question # 02

(b) A current waveform flowing through an inductor of 1 mH is shown in the figure. Obtain a sketch the waveform of voltage across the inductor



(6)

Solution:

From the given waveform:

For $0 < t < 2$:

$i(t)$ is a straight line of slope $= \frac{100}{2} = 50$

Therefore,

$$i(t) = 50t \text{ and } \frac{di(t)}{dt} = 50$$

For $2 < t < 4$:

$$i(t) = 100 \text{ and } \frac{di(t)}{dt} = 0$$

For $4 < t < 6$,

$i(t)$ is a straight line of slope $= -\frac{100}{2} = -50$

Therefore,

$$i(t) = -50t \text{ and } \frac{di(t)}{dt} = -50.$$

⑦

Now,

$$V_L(t) = L \frac{di(t)}{dt}$$

$$= 1 \times 10^3 \times 50$$

$$= 0.05 \text{ V} \quad , \quad 0 < t < 2$$

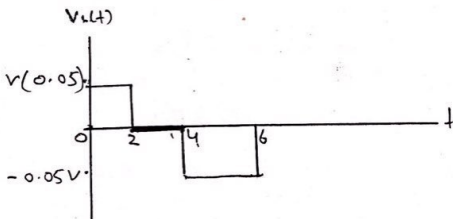
$$= 1 \times 10^3 \times 0$$

$$= 0 \text{ V} \quad , \quad 2 < t < 4$$

$$= 1 \times 10^3 \times (-50)$$

$$= -0.05 \text{ V} \quad 4 < t < 6.$$

The voltage waveform is shown in following figure.



(8)

Question # 03

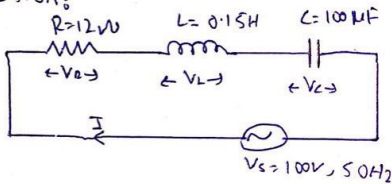
(a) A Series RLC Circuit Containing a

Resistance of 12Ω , an inductance of $0.15H$ and a capacitor of $100\mu F$ are connected in Series across a $200V, 50Hz$ supply.

Calculate the total circuit impedance and

Current = ? power factor = ? and Voltage phasor diagram?

Solution:



Inductive Reactance,

$$X_L = 2\pi fL$$

$$= 2\pi \times 50 \times 0.15$$

$$= 47.13 \Omega$$

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Capacitive Reactance

$$X_c = \frac{1}{2\pi fC}$$

$$= \frac{1}{2 \times 3.14 \times 50 \times 100 \times 10^6}$$

$$= 31.83 \Omega$$

Circuit Impedance:

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$= \sqrt{(12)^2 + (47.13 - 31.83)^2}$$

$$= \sqrt{144 + 234}$$

$$= 19.4 \Omega$$

Circuit Current:

$$I = \frac{V_s}{Z} = \frac{100}{19.4}$$

$$= 5.14 \text{ Amps.}$$

(10)

Voltage across the Series RLC Circuit.

$$V_R, V_L, V_C = ?$$

$$V_R = I \times R$$

$$= 5.14 \times 12$$

$$= 61.7 \text{ V}$$

$$V_L = I \times X_L$$

$$= 5.14 \times 47.13$$

$$= 242.2 \text{ V}$$

$$V_C = I \times X_C$$

$$= 5.14 \times 31.8$$

$$= 163.5 \text{ V}$$

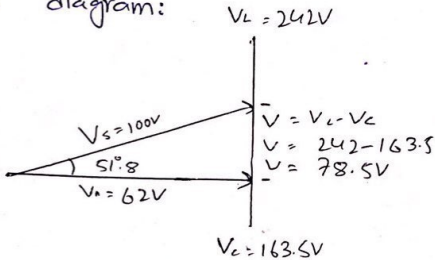
Circuit Power factor or Phase angle

$$\cos \phi = \frac{R}{Z} = \frac{12}{19.4} = 0.619$$

$$\therefore \cos^{-1} 0.619 = 51.8^\circ \text{ degree.}$$

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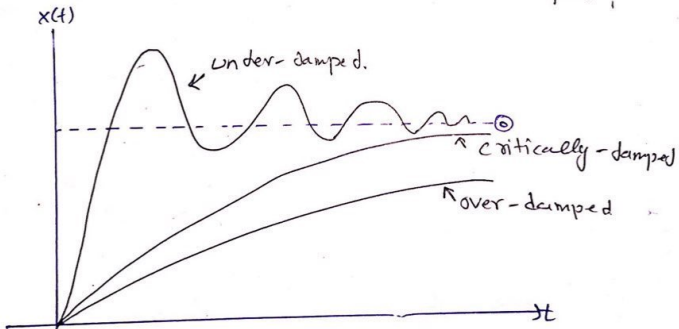
Phase diagram:



Question #03

(b) Write a short note on Under damped, Over damped & Critical damped.

Sol:



②

Under-Damped:

A system is called under-damped, if its damping ratio (denoted by ζ) is less than 1. Here the system oscillates with a gradual decrement to zero. i.e. automatic door or window closer is under damped it will close with considerable velocity or the door will swing too far before closing at its normal position.

Over-Damped:

A system is called over-damped, if the damping ratio is greater than one ($\zeta > 1$) here system shows tendencies to achieve equilibrium without oscillating.

(B)

Critically-Damped:

A system is called critically damped if damping ratio for the system is exactly one. ($\zeta=1$). here system shows the tendencies to come to equilibrium as quickly as possible without damping. Like automatic door or window closer mechanisms, they promptly come to original position without showing any further oscillation.