

"MID EXAM"

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Subject # MOS(2)

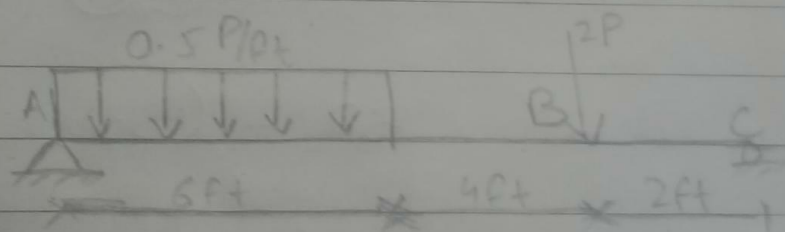
Section # "C"

Submitted to #

"Engr. Muhammad Saqib"

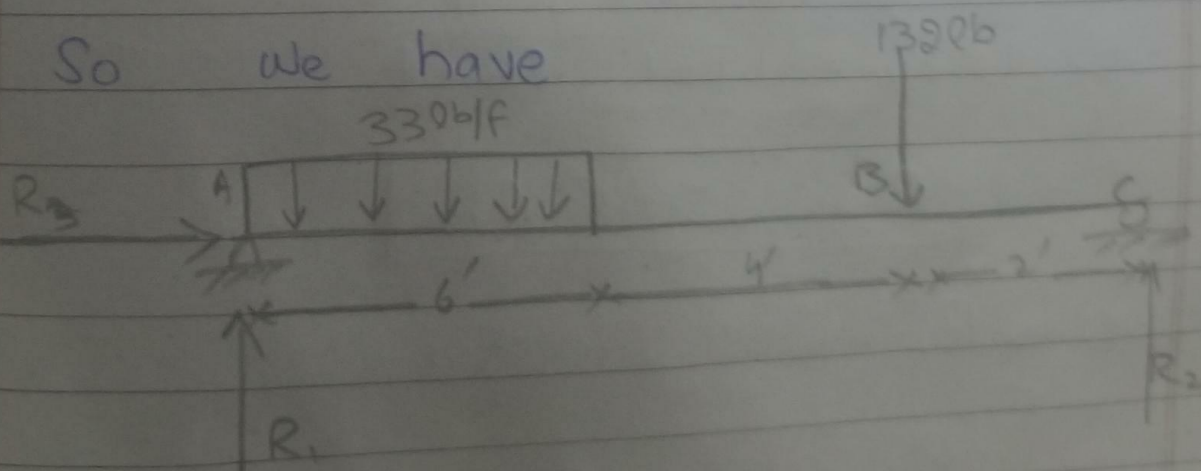
Q. Construct the Mohr's Circle diagram and find principal stress and maximum in plane shear stress for the stress state of a point C located at the centre of uniformly distributed load in pounds.

Given Beam:-



Note Put the value of $P = 66$

So we have



To find the unknown reaction at the support apply equilibrium equation

Pg - 2

$$\sum f_x = 0 \quad \text{i.e.} \quad R_3 = 0$$

$$\sum f_y = 0 \quad \uparrow \downarrow$$

$$R_1 + R_2 = (33 \times 6) \text{ lb} + 139 \text{ lb}$$

$$R_1 + R_2 = 198 + 139$$

$$\Rightarrow 330$$

$$R_1 + R_2 = 330 \quad \text{--- (1)}$$

Next $\sum M_A = 0$ + -

$$R_2 \times 12 = 10 \times 139 - (33 \times 6) \times \frac{6}{2} = 0$$

$$12R_2 = 1390 + (198) \times 3$$

$$= 1390 + 594$$

$$\Rightarrow 12R_2 = 1914 \text{ lb-ft}$$

$$R_2 = 159.5 \text{ lb}$$

$$\text{(1)} \Rightarrow R_1 + R_2 = 330$$

$$R_1 = 330 - R_2$$

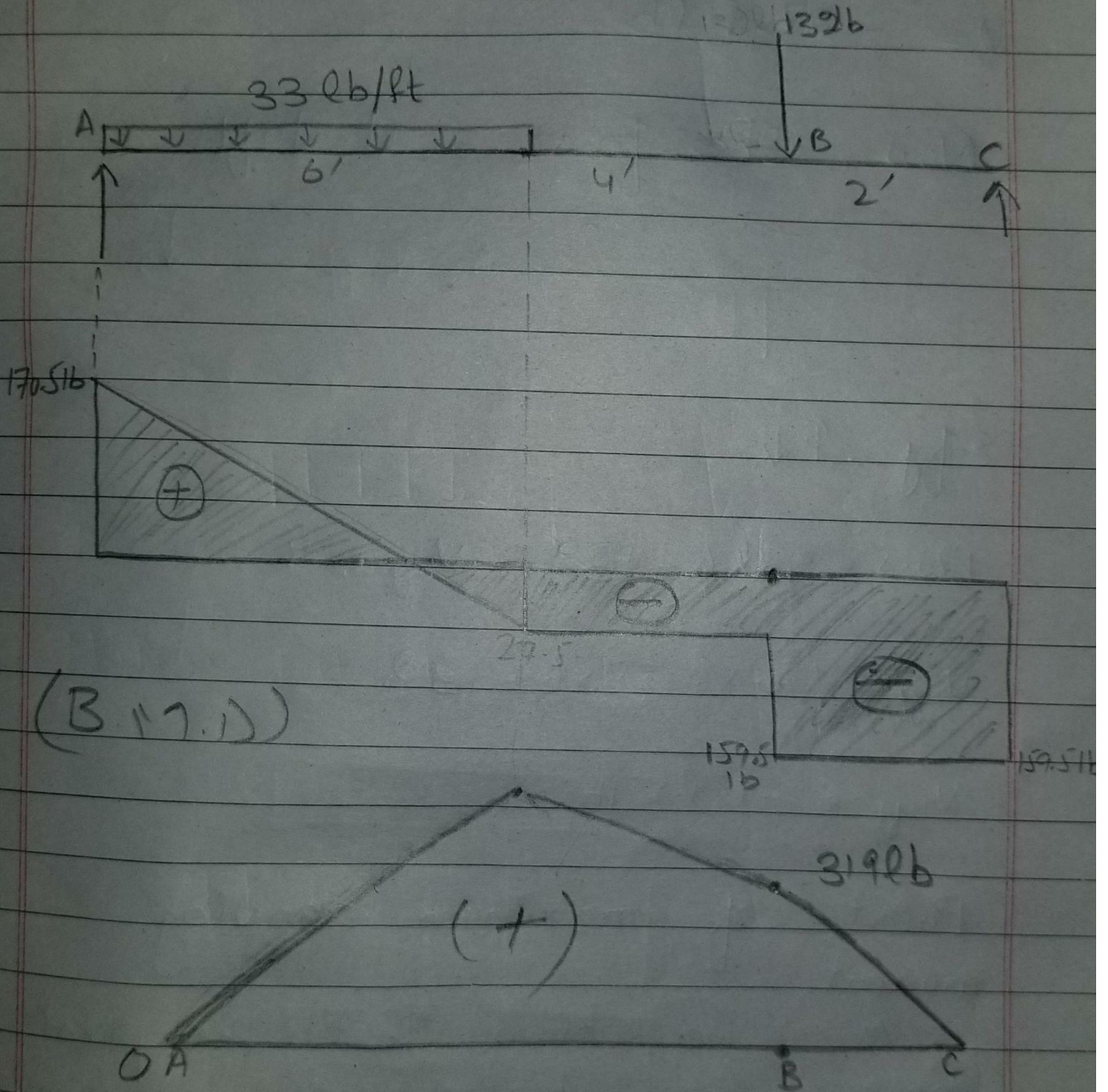
$$R_1 = 330 - 159.5$$

$$R_1 = 170.5$$

$$R_1 = 170.5 \text{ lb}$$

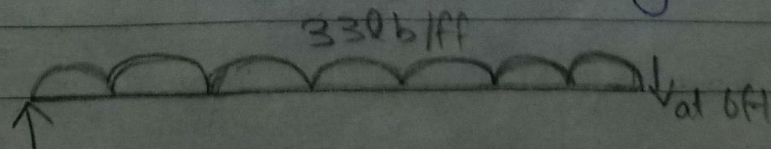
Now draw shear force and bending moment diagram

We have.



(B.M.D)

Now shear force at change point of beam



Shear stress at 6 ft from left support

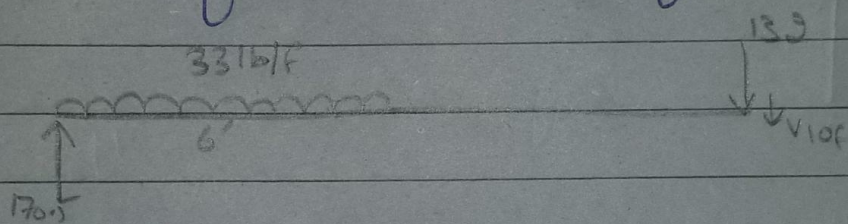
Pg-4

$$\sum F_y = 0 \uparrow + \downarrow -$$

$$170.5 - 33 \times 6 - V_{\text{left}} = 0$$

$$V_{\text{left}} = -27.5 \text{ lb}$$

Now Shear force at left



$$\sum F_y = \uparrow + \downarrow -$$

$$170.5 - 33 \times 6 - 132 - V_{\text{left}} = 0$$

$$V_{\text{left}} = 170.5 - 33 \times 6 - 132$$

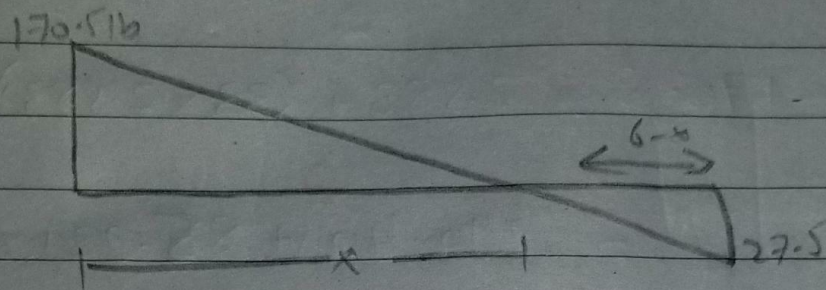
$$V_{\text{left}} = -159.5 \text{ lb}$$

Point of maximum bending moment

As we know that the point where shear force is minimum the bending moment is maximum. So from point of zero shear corresponding point will have maximum bending moment.

Pg-5

From shear force diagram
on page (2) we have



We know that

$$\frac{170.5}{x} = \frac{27.5}{6-x}$$

$$(6-x) \cdot 170.5 = 27.5x$$

$$511.5 - 170.5x = 27.5x$$

$$511.5 = 27.5x + 170.5x$$

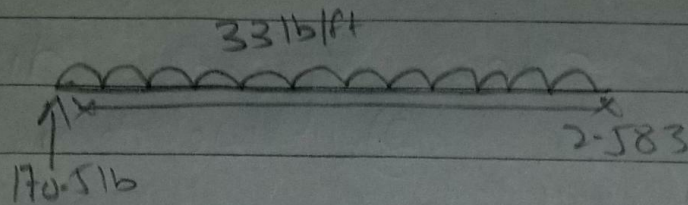
$$511.5 = 198x$$

$$198x = 511.5$$

$$x = \frac{511.5}{198}$$

$$x = 2.583 \text{ ft}$$

Now determine the value of
Moment at 2.583



$$17 \cdot \frac{1}{2.583} - 170.5 \times 2.583 + (33 \times 2.583) \times \frac{2.583}{2} = 0$$

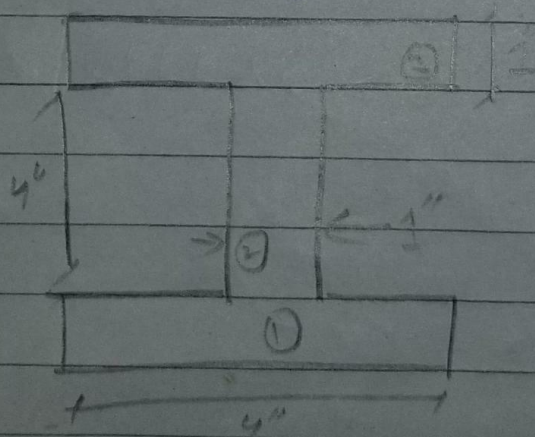
$$\Rightarrow 17 \cdot 2.583 \text{ ft} - 440.4015 + 88.239 \times 1.291 = 0$$

$$17 \cdot 2.583 \text{ ft} = 550.445 \text{ lb-ft}$$

For shear stress we have

$$I = \frac{VQ}{I_b}$$

So first we determine moment of Inertia I for the given section of Beam



As the given figure is symmetrical along both the axes
So

$$\bar{x} = \frac{4}{2} = 2 \text{ in}, \quad \bar{y} = \frac{6}{2} = 3 \text{ in}$$

i.e. $(\bar{x}, \bar{y}) = (2, 3)$ (Centre of gravity)

From extrem left and Bottom
Area of point ① = $4 \times 1 = 4 \text{ in}^2$
Area of point ② = $4 \times 1 = 4 \text{ in}^2$
Area of point ③ = $4 \times 1 = 4 \text{ in}^2$

Moment of inertia about x-axis
(Centroidal) I_{xx}

Determine distance between
C-G of the whole section
and the corresponding parts.

Let G_1, G_2, G_3 be the centre
of gravity of point ① ② and ③
and K_1, K_2, K_3 be the distance
between \bar{y} and y_1, y_2, y_3 respectively

So

$$K_1 = \bar{y} - y_1 = 3 - 0.5 = 2.5 \text{ in}$$

$$K_2 = \bar{y} - y_2 = 3 - 3 = 0 \text{ in}$$

$$K_3 = \bar{y} - y_3 = 3 - 0.5 = 2.5 \text{ in}$$

$$\text{So } I_{xx} = \frac{b_1 h_1^3}{12} + a_1 K_1^2 + \frac{b_2 h_2^3}{12} + a_2 K_2^2 + \frac{b_3 h_3^3}{12}$$

$$I_{xx} = \frac{(4)(1)^3}{12} + 4(2.5)^2 + \frac{(1)(4)^3}{12} + 4(0) + \frac{4(1)^3}{12} + 4(2.5)^2$$

$$I_{xx} = \frac{4}{12} + 95 + \frac{64}{12} + \frac{4}{12} + 25$$

$$\Rightarrow \frac{4 + 12(25) + 64 + 4 + 12(25)}{12}$$

$$\boxed{\bar{I}_{xx} = 56 \text{ in}^4}$$

Now

$$\bar{I}_{yy} = \frac{(4)^3(1)}{12} + \frac{(1)^3(4)}{12} + \frac{(4)^3(1)}{12}$$

$$= \frac{64}{12} + \frac{4}{12} + \frac{64}{12}$$

$$\bar{I}_{yy} = \frac{64 + 4 + 64}{12}$$

$$\boxed{\bar{I}_{yy} = 11 \text{ in}^4}$$