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Subject : S E S

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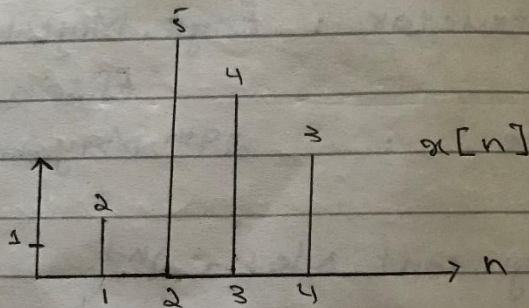
Date : 29th May, 2020

Assignment No: 2nd

Q: 1

Evaluate the even & odd components for the given function.

Given:



Required:

Even & odd components of the above signal.

Solution:

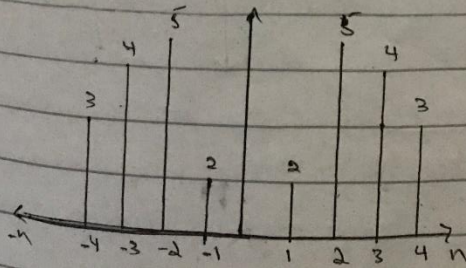
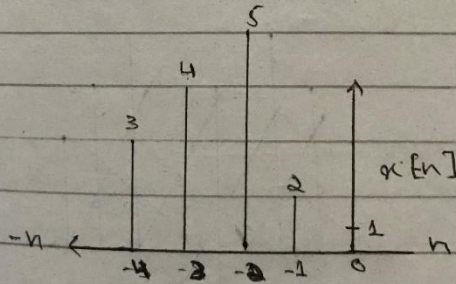
For Even :

As we know that even components can be written as ;

$$x_e[n] = \frac{x[n] + x[-n]}{2}$$

So,

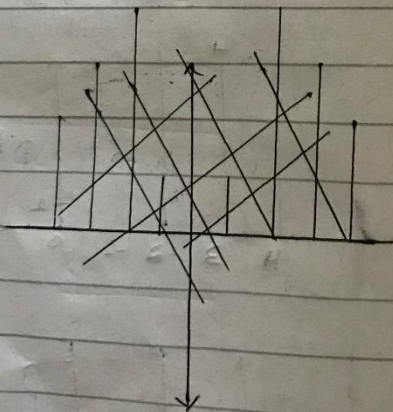
Reflect $x[n]$ to get $x[-n]$

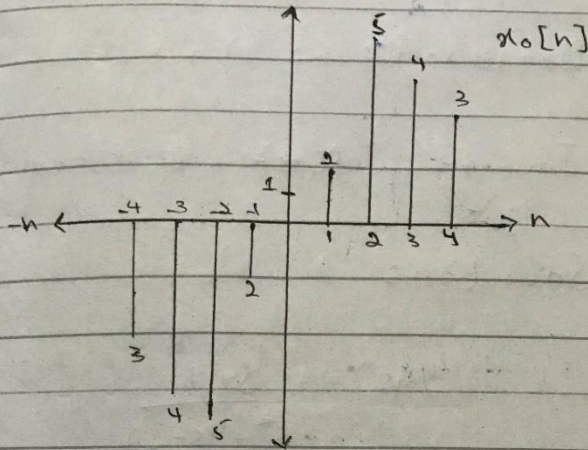


For odd:

As odd components can
be written as ax
we can find odd
component by this

$$x_o[n] = \frac{x[n] - x[-n]}{2}$$





Q:2

Calculate the inverse Laplace transform of the given equation

Given:

$$Y(s) = \frac{s+4}{s^2+4s-12}$$

Required:

Inverse Laplace transform

Solution:

$$Y(s) = \frac{s+4}{s^2+4s-12}$$

$$= \frac{s+4}{s^2+6s-12}$$

$$= \frac{s+4}{s(s+6)-2(s+6)}$$

$$= \frac{s+4}{(s+6)(s-2)}$$

$$\frac{s+4}{(s+6)(s-2)} = \frac{A}{s+6} + \frac{B}{s-2} \rightarrow (A)$$

$$s+4 = A(s-2) + B(s+2) \quad \text{--- (i)}$$

for B:

Let,

$$s = 2 \quad \text{in eq (i)}$$

$$2+4 = A(2-2) + B(2+2)$$

$$6 = A(0) + B(4)$$

$$6 = B(4)$$

$$\div \text{ing } 4 \text{ b/s}$$

$$\frac{6}{4} = \frac{B(4)}{4}$$

$$B = \frac{3}{2}$$

for A:

Let,

$$s = -2$$

put in eq (i).

$$-2+4 = A(-2-2) + B(-2+2)$$

$$2 = A(-4) + B(0)$$

$$2 = A(-4)$$

$$\div \text{ing } -4 \text{ b/s}$$

$$\frac{2}{-4} = \frac{A(-4)}{-4}$$

$$A = \frac{1}{-2}$$

Now put values of
A & B in eq (A)

we get,

$$Y(s) = \frac{1}{s+6} + \frac{2}{s-2}$$

$$= \frac{1}{-2}$$

$$= \frac{1}{-2}$$

Q: 3

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$$= \frac{1}{-2} \mathcal{L}^{-1} \left[\frac{1}{s+6} + \frac{3}{2} \mathcal{L}^{-1} \left(\frac{1}{s-2} \right) \right]$$

$$= \frac{1}{-2} e^{-6t} + \frac{3}{2} e^{2t}$$

Q:3 (i)

Discuss the procedure of converting an analog signal into a digital one.

Answer:

To convert an ~~contin~~ analog signal to discrete signal it has to be passed from ~~two~~ ^{three} different stages which are;

- (i) Sampler
- (ii) Quantiser
- (iii) Coder.

All of the above stages are completed in two steps.

Step No 1:

Sampling converts a continuous time continuous amplitude signal to discrete time continuous amplitude (still real valued) signal. Only the time axis is discretised into the amplitude axis.

Step No 2:

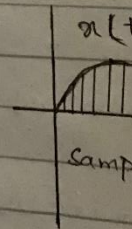
Quantization converts the discrete time continuous amplitude

signal to values, be represented by bits and stored

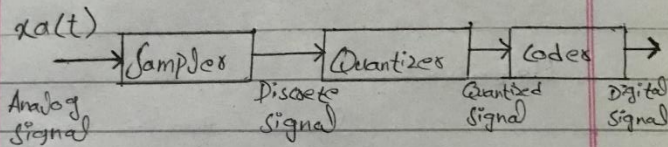
$x_a(t)$ → [Sam]

Analog signal

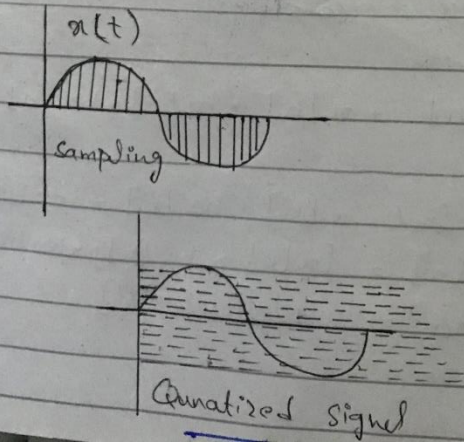
The de
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ADC (Ana



signal to set of finite values, so that it can be represented by finite bits and can be stored on computer.



The device used for converting the signals is called ADC (Analog to Digital converter).



Q: 4

~~Q: 4~~

Given:

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$

Required:

Show that they are equal.

Solution:

Let's consider

$$y[n] = x[n] * h_1[n] * h_2[n]$$

$$\text{Let } x[n] * h_1[n] = w_1[n]$$

$$y[n] = [x[n] * h_1[n]] * h_2[n] \rightarrow w_1[n]$$

$$y[n] = w_1[n] * h_2[n]$$

$$x[n] \rightarrow \boxed{h_1[n]} \xrightarrow{w_1[n]} \boxed{h_2[n]} \rightarrow y[n]$$

Now consider that.

$$w_2[n] = h_1[n] \times h_2[n]$$

$$\begin{aligned} y[n] &= x[n] \times [h_1[n] \times h_2[n]] \\ &= x[n] \times w_2[n] \end{aligned}$$

$$x[n] \rightarrow \boxed{w_2[n]} \rightarrow y[n]$$

Proved:

$$[x[n] \times h_1[n]] \times h_2[n] = x[n] \times [h_1[n] \times h_2[n]].$$

Q3 : (ii)

Solution:

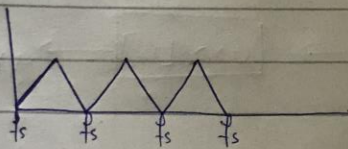
Nyquist criteria: $f = 60 \text{ Hz}$

$$f_s \geq 2 f_m \quad \uparrow \uparrow \uparrow \uparrow$$

f_m

$$f_s \geq 2 \times 60$$

$$f_s = 120$$



if $f_s = 120 \text{ Hz}$ there will be no aliasing occur as Nyquist Criteria proves it.

