

Name

Wajeehuddin

ID

7921

SUBJECT

MOS 2

Date

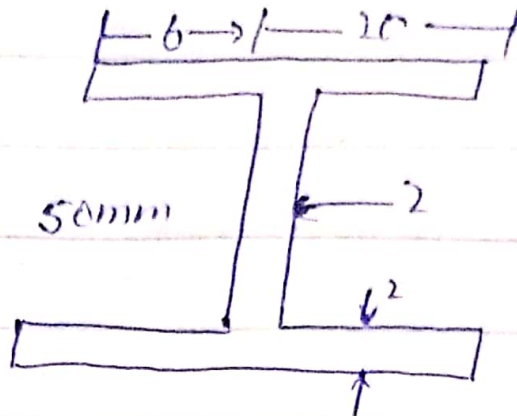
23 June 2020

Section

51

# Question 1 (LA)

(1)



Required of location of Shear Center

Solution As we know

$$e = \frac{I_2 h^2 b^2}{4I}$$

$$\text{and } I = 2 \left( \frac{bh^3}{12} + Ay^2 \right) + \left( \frac{b^3 h}{12} + Ay^2 \right)$$
$$= 2 \left[ \frac{20(2)^3}{12} + (20 \times 2)(25)^2 \right] + \left[ \frac{2(50)^3}{12} + 40 \right]$$

$$I = 50034.66 + 20833$$

$$I = 70867.99 \text{ mm}^4$$

$$e = \frac{2(50)^2(25)^2}{4(70867.99)} = 11.02 \text{ mm}$$

So shear center =  $e = 11.02 \text{ mm}$

# Question 1 (B) (2)

## Data

$$H = 26 \text{ ft}$$

I assume diameter

$$D = 22 \text{ ft}$$

$$\text{tangential stress} = 600 \text{ lb/ft}^2$$

specific weight of water

$$\text{tank} = 62.4 \text{ lb/ft}^3$$

we have to find the thickness = ?

## Solution

The pressure develop by water =  $p = \gamma h$

$$\delta t = \frac{PD}{2t}$$

(3)

$$bt = \frac{PD}{2t} = \frac{rKD}{2t}$$

$$2t \times bt = rKD$$

$$2t = \frac{rKD}{bt}$$

$$t = \frac{rKD}{bt \times 2}$$

$$t = \frac{(62.4) \times 2 (6 \times 12) \times (22 \times 12)}{(12)^3}$$

---

$$6000 \times 2$$

$$t = 0.24''$$

# Question 2 (A)

(4)

## Moment of inertia

$$I_z = \frac{bh^3}{12} = \frac{0.1 (0.15)^3}{12} = I_z = 2.8125 \times 10^{-5}$$

Now

$$I_y = \frac{b^3 h}{12} = 0.15 (0.1)^3$$

$$I_y = 1.25 \times 10^{-5}$$

$$I = \frac{M_z}{I_z} + \frac{M_y}{I_y}$$

$$I = \frac{M \cos \theta}{I_z} + \frac{M \sin \theta}{I_y}$$

where

$$M \cos \theta = p \cos \theta = M_z$$
$$= 18 \cos 30^\circ = M_z$$

$$M \sin \theta = p \sin \theta = M_y$$

$$M_y = 12 \sin 30$$

$$M_y = -11.8563$$

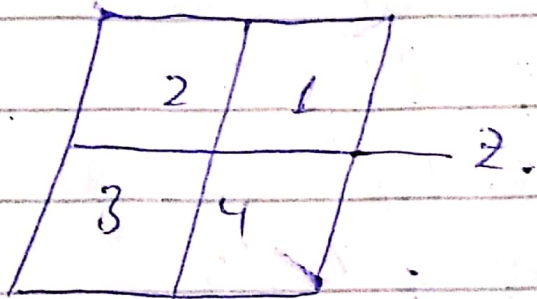
(5)

$$S = \left( \frac{M_x}{I_x} \right) + \left( \frac{M_y}{I_y} \right)$$

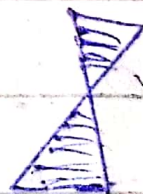
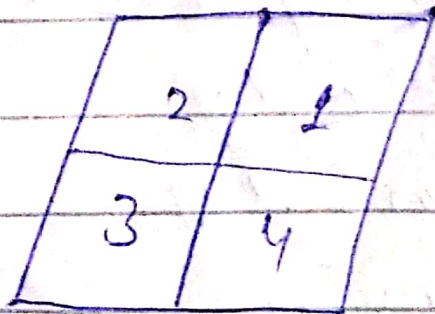
$$S = \frac{1.852}{2.812 \times 10^{-5}} + \left( \frac{-11.0563}{1.25 \times 10^{-5}} \right)$$

$$= 882678 \text{ Nm}^2$$

S convention

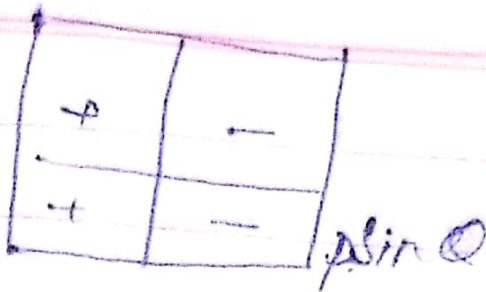


if we have compression as negative and tension as positive and the beam is a simply supported.

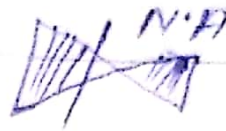


Quadrant 1, 2 -ive

Quadrant 3, 4 +ive



(6)



Quardant 1, 4 -ive

Quardant 2, 3 +ive

In case of unsymmetrical loading the neutral axis lies at an angle of  $\alpha$  to the principle axis and the algebraic sum of stress at N.A. is zero.

$$\sigma = \frac{M \cos \theta}{I_z} y + \frac{M \sin \theta}{I_y} z \rightarrow \text{①}$$

in this case N.A. passes through 2, 4

$$\sigma = \frac{M \cos \theta}{I_z} y + \frac{M \sin \theta}{I_y} z$$

let consider a point A on N.A. lies in Quardant 2.

(7)

Bending stress due to  
 plane is compressive  
 and

Bending stress due to  
 plane is tensile.

Equation (1)

$$\sigma = \frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow \sigma = \frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\frac{y_A}{z_A} = \frac{I_z}{I_y} \frac{\sin \theta}{\cos \theta} = \tan \theta \frac{I_z}{I_y} \quad \text{--- (ii)}$$



(8)

Now put the value of  $I_x$ ,  $I_y$  and (i) and eq (ii)

$$\tan \alpha = \frac{I_x \tan 30}{I_y}$$

$$\Rightarrow \tan \alpha = \frac{2.8125 \times 10^{-5} (\tan 30^\circ)}{1.25 \times 10^{-5}}$$

$$\tan \alpha = -14.4229$$

$$\alpha = \tan^{-1} (-14.4229)$$

$$\alpha = 1.5^\circ$$

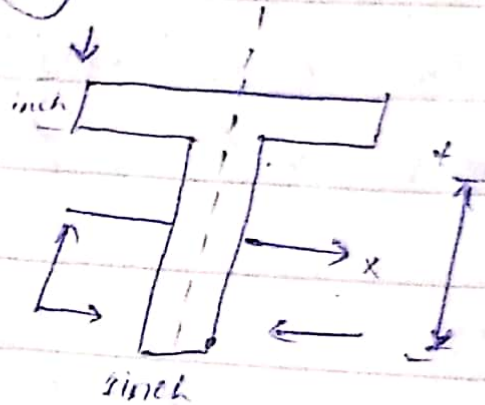
$$\alpha = 1^\circ 30' 5''$$

(9)

## Question 2

## part B

## Given Data



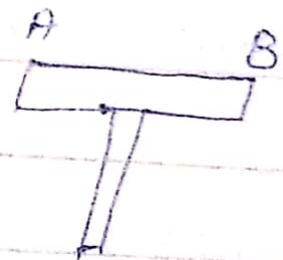
$$L = 16 \text{ ft}$$

$$I_x = 112 \text{ in}^4$$

$$I_y = 18.7 \text{ in}^4$$

$$S_c = 12000 \text{ psi}$$

$$S_t = 5000 \text{ psi}$$



## Solution

By looking figure we can judge that maximum compression would occur on  $a$  and maximum tension

(10)

C at B. These will  
tension as well a compression  
which will reduce that  
effect of each other.

So we will calculate  
stress at A and C

So

$$\sigma_A = \frac{M_{xy}}{I_x} + \frac{m_{yx}}{I_y} \text{ comp}$$

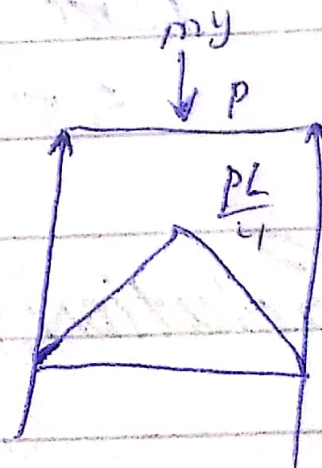
$$\sigma_C = \frac{m_{xy}}{I_x} + \frac{M_{yx}}{I_y} \text{ (Tension)}$$

Now  $M_x$  and

So

$$M_x = \frac{p \cos 60^\circ (16 \times 12)}{4}$$

$$M_x = 48 p \cos 60^\circ$$



$$M_y = \frac{p \sin 60^\circ (16 \times 12)}{4}$$

(11)

$$M_y = 48p \sin 60$$

NOW

$$S_A = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$\Rightarrow 1200 = \frac{48p \cos 60^\circ \times 3.07}{112.6}$$

Solving the equation  
 $48p \sin 60 \times 3$

$$p = 1638.6 \text{ lb}$$

NOW

$$S_C = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$5000 = 48p \cos 60 \times (5.93)$$

$$\frac{48p \sin 60 \times 0.5}{112.6}$$

Solving the equation

$$18.7$$

(12)

$$P = 2104.915$$

(13)

Q no 3

Given data

Length "L" = 10 ft

As: both sides are good

So  $L_e = L$

$E = 10.3 \times 10^6$

Factor of safety = 2

$b = 0.75$  inch

$h = 2$  inch

Required data

Determine safe load?

(14)

Solution

AS

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

As we know that  $I = Ar^2$

$$I = Ar^2$$

$$r = \sqrt{I/A}$$

$$r = \frac{\sqrt{\frac{hb^3}{12}}}{bh} \Rightarrow \sqrt{\frac{b^2}{12}}$$

$$r = 0.216 \text{ inch}$$

$$P_{cr} = \frac{\pi^2 EA}{(L_e/r)^2}$$

$$\Rightarrow \frac{(3.14)^2 (10.3 \times 10^6) (1.5)}{(10/0.216)^2}$$

$$P_{cr} = 853.8343$$

(15)

$$\text{Safe load} = \frac{\text{Crippling load}}{\text{Factor of safety}}$$

$$\Rightarrow \frac{853.8343}{2}$$

$$\text{Safe Load} \Rightarrow 426.917$$

(\*) For Fixed ended column

$$L_e = L/2 = 10/2$$

$$L_e = 5\text{m}$$

$$P_{cr} = \frac{\pi^2 EA}{(L_e/r)^2} \Rightarrow \frac{(3.14)^2 \times 10 \cdot 3 \times 10^6 (0.9)}{(60/2 \cdot 16)^2}$$

$$P_{cr} = 1974.207$$

$$\text{Safe load} = \frac{P_{cr}}{\text{Factor of safety}}$$

$$\frac{1974.207}{2} = 987.103$$