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Section B

Program BS. SE

Class Time Wednesday 8:00 to 11:00

Mid Assignment Operation Research.

Q No#1:

There are total of 5 machines and five employment are to be relegated and the related cost network is as per the following. Located the best possible task.

Sol^o =>

Machines.

	A	B	C	D	E
1	6	12	3	11	15
2	4	2	7	1	10
3	8	11	10	7	11
4	16	19	122	23	21
5	9	5	7	6	10

This is

Balanced assignment problem

$$5 = 5$$

Hungarian method: \Rightarrow

Phase I: Row and Column reduction ^{each}.

Step (1): Subtract the minimum value of row from the entries of that row.

Step (2): Subtract the minimum value of each Column from the entries of that column.

Phase 2: \Rightarrow optimization of the Problem.

(a) Row Scanning.

(b) Column Scanning.

	Machines					Row minimum
	A	B	C	D	E	
1	6	12	3	11	15	3
2	4	2	7	1	10	1
3	8	11	10	7	11	7
4	16	19	12	23	21	16
5	9	5	7	6	10	5

D
O
B
S

J O B S

	Machines				
	A	B	C	D	E
1	3	9	0	8	12
2	3	1	6	0	9
3	1	4	3	0	4
4	0	3	106	7	15
5	4	0	2	1	5
	0	0	0	0	4

Column minimum

	Machines					Row Scoring	Column Scoring
	A	B	C	D	E		
1	3	9	0	8	12	8	0
2	3	1	6	0	9	5	0
3	1	4	3	0	4	0	0
4	0	3	106	7	15	7	0
5	4	0	2	1	5	1	0

P#4

	Machines				
	A	B	C	D	E
1	6	12	<u>3</u>	11	15
2	4	2	7	<u>11</u>	10
3	8	11	10	7	<u>11</u>
4	<u>16</u>	19	122	23	21
5	9	<u>5</u>	7	6	10

Optimal Solution

Jobs Machines Time

1 B 5

2 C 3

3 D 1

4 E 11

5 A 16

Total hours.

Total Processing time = 36

Question No # 2

$$\min z = 2x_1 + 3x_2$$

$$\text{s.t. } (1/2)x_1 + (1/4)x_2 \leq 4$$

$$x_1 + 3x_2 \geq 20$$

$$x_1 + x_2 = 10$$

$$x_1, x_2 \geq 0$$

Solve \Rightarrow

By minimization method:

$$Z = -2x_1 - 3x_2$$

$$Z = -2x_1 - 3x_2 + m_1 - m_2$$

$$Z + 2x_1 + 3x_2 + m_1 + m_2 = 0$$

$$2x_1 + 3x_2 + m_1 + m_2 + Z = 0$$

$$\frac{1}{2}x_1 + \frac{1}{4}x_2 + S_1 = 4$$

$$x_1 + x_2 - S_2 + a_1 = 20$$

$$x_1 + x_2 + a_2 = 10$$

P₂

	x_1	x_2	S_1	S_2	a_{11}	a_{12}	Z
S_1	$1/2$	$1/4$	1	0	0	0	4
a_{11}	1	1	0	-1	1	0	20
a_{12}	1	1	0	0	0	1	10
Z	2	3	0	0	m	m	0

	m_1	m_2	S_1	S_2	a_{11}	a_{12}	Z
	$1/2$	$1/4$	1	0	0	0	0
	1	1	0	-1	1	0	0
	1	1	0	0	0	1	0
	$-m+2$	$-m+3$	0	m	0	m	1

$$R_4: \begin{matrix} 2 & 3 & 0 & 0 & 0 & m & m & 1 & 0 \end{matrix}$$

$$\begin{matrix} -mR_2 & -m & -m & 0 & m & -m & 0 & 0 & -20m \\ \hline -m+2 & -m+3 & 0 & m & 0 & m & 0 & m & -20m \end{matrix}$$

P₃ 9 P₄

x_1	x_2	s_1	s_2	a_1	a_2	Z
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
1	0	0	1	0	0	20
1	0	0	0	1	0	10
$-2m+2$	$-2m+3$	0	m	0	0	$-30m$

$R_4 : -m+2 \quad -m+3 \quad 0 \quad m \quad 0 \quad m \quad -20m$

$-mR_3 : -m \quad -m \quad 0 \quad 0 \quad 0 \quad -m \quad 0 \quad -10m$

$-2m+2 \quad -2m+3 \quad 0 \quad m \quad 0 \quad 0 \quad -30m$

x_1	x_2	s_1	s_2	a_1	a_2	Z
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	4
1	1	0	-1	1	0	0
1	1	0	0	0	1	0
$-2m+2$	$-2m+3$	0	m	0	0	1

P4

$$4R_1: \begin{pmatrix} 4/2 & 4/4 & 4 & 0 & 0 & 0 & 0 & 16 \end{pmatrix}$$

$$R_2: \begin{pmatrix} 2 & 1 & 4 & 0 & 0 & 0 & 0 & 16 \end{pmatrix}$$

x_1	x_2	s_1	s_2	a_1	a_2	z	
2	1	4	0	0	0	0	16
1	1	0	1	0	0	0	20
1	1	0	0	1	0	0	10
$-2m+2$	$-2m+3$	m	0	0	0	1	$-30m$

$R_2 - R_1$

$$R_2: \begin{pmatrix} 1 & 0 & -4 & 1 & 0 & 0 & 20 \end{pmatrix}$$

$$-R_1: \begin{pmatrix} -4 & -4 & 0 & 0 & 0 & 0 & -16 \end{pmatrix}$$

$$\begin{pmatrix} -4 & 0 & -4 & -1 & 0 & 0 & 4 \end{pmatrix}$$

P 5

	$-m_1$	m_2	S_1	S_2	a_1	a_2	Z
x_2	2	1	4	0	0	0	16
a_{11}	-1	0	-4	-1	1	0	4
a_2	1	1	0	0	0	1	10
Z	$-2m+2$	$-2m+3$	0	m	0	0	$-30m$

$R_3 - R_1$

$$R_3: 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 10$$

$$-R_1: -2 \quad -1 \quad -4 \quad 0 \quad 0 \quad 0 \quad -16$$

$$1 \quad 0 \quad -4 \quad 0 \quad 0 \quad 1 \quad 0 \quad -6$$

x_1	x_2	S_1	S_2	a_1	a_2	Z
2	1	4	0	0	0	16
-1	0	-4	-1	1	0	4
-1	0	-4	0	0	1	-6
$-2m+2$	$-2m+3$	0	m	0	0	$-30m$

$$R_4 + (2m-3)R_1$$

$$R_4 : \quad -2m+2 \quad -2m+3 \quad 0 \quad m \quad 0 \quad 0 \quad 1 \quad -3m$$

$$2m-3R_1 : \quad 4m-6 \quad 2m+3 \quad 8m-12 \quad 0 \quad 0 \quad 0 \quad 0 \quad 32m-48$$

$$2m-4 \quad 0 \quad 8m-12 \quad m \quad 0 \quad 0 \quad 1 \quad 2m-48$$

	x_1	x_2	S_1	S_2	a_1	a_2	$\frac{R_i}{b_i}$
x_2	2	1	4	0	0	0	16
a_1	-1	0	-4	-1	1	0	4
a_2	-1	0	-4	0	1	0	-6
Z	$2m-4$	0	$8m-12$	m	0	0	$2m-48$

P7

	x_1	x_2	s_1	s_2	a_1	a_2	Z
x_2	2	1	4	0	0	0	16
a_1	-1	0	-4	-1	1	0	4
a_2	-1	0	-4	0	0	1	-6
Z	$2m-4$	0	$8m-12$	m	0	0	$2m-48$

$$x_2 = 16$$

$$a_1 = 4$$

$$a_2 = -6$$

$$Z = 2m - 48$$

$$x_1 = 0$$

$$s_1 = 0$$

$$s_2 = 0$$

Question No # 3

Use Vogel's Approximation Method to obtain the initial feasible solution of

Origin	Destination			Supply
	1	2	3	
1	20	22	17	4
2	24	37	9	7
3	32	37	20	15
Demand	60	40	30	110
				<u>240</u>

Demand = Supply.

So it is

(Balanced transportation Problem)

P-2

Origin	Destination				Supply
	1	2	3	4	
2	X ₂₀	40	X ₁₇	4	120
2	10	22	30	4	180
3	24	X ₃₇	9	7	70
	50				20
	32	X ₃₇	X ₂₀	X ₁₅	50
Demand	60	40	30	10	240
	50	0	0	30	240
	0	0	0	0	

4	(15)	8	3
4	-	8	3
8	-	(11)	8
8	-	-	8

$$= 40 \times 22 + 80 \times 4 + 10 \times 24 + 30 \times 9 + 30 \times 7$$

$$+ 50 \times 32$$

3520