

M. Remaz

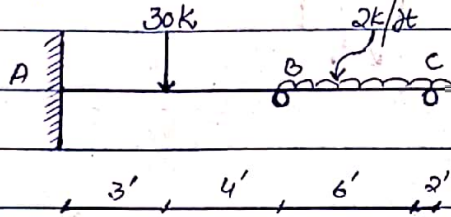
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①

Day: M T W T F S

Date: \_\_\_/\_\_\_/\_\_\_

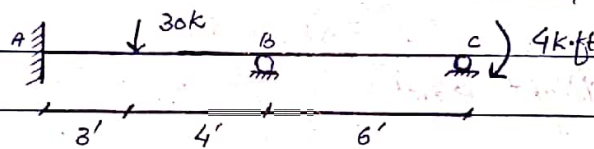
QNo 1) Analyze ----- EI is constant.



Sol:

Step ① Determining kinematic Indeterminacy.  
 $K \cdot I = 5^\circ$

We have to reduce the extended portion.



$$\Rightarrow \frac{2(2)}{1} \Rightarrow 4 \text{ k-ft}$$

Now:

$$K \cdot I = 2^\circ$$

Step ②

Determine unknow joint Displacement

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

Step ③

Compute  $[ADL]$  Matrix

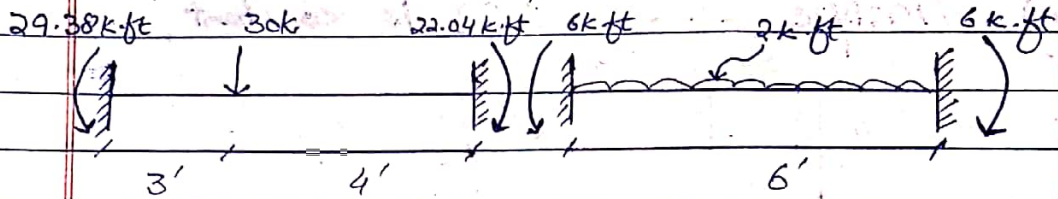
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⇒ for point load (Not at mid)  
⇒ for left end

$$\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{(7)^2} = 29.38 \text{ k}\cdot\text{ft}$$

for Right end

$$\frac{Pa^2b}{L^2} = \frac{(30)(3)^2(4)}{(7)^2} = 22.04 \text{ k}\cdot\text{ft}$$

⇒ for UDL

$$\frac{wL^2}{12} \Rightarrow \frac{(2)(6)^2}{12} = 6 \text{ k}\cdot\text{ft}$$

$$ADL_1 = +22.04 - 6 = 16.04 \text{ k}\cdot\text{ft}$$

$$ADL_2 = 6 \text{ k}\cdot\text{ft}$$

Step (4)

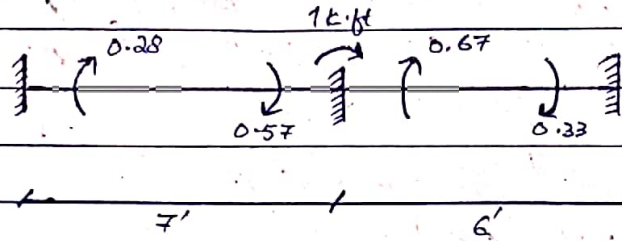
Compute [S] matrix

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

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a)  $D_1 = 1 \text{ k}$        $D_2 = 0$



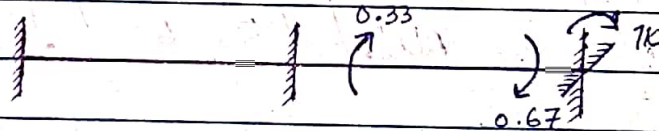
$$\frac{4EI}{7} = 0.57 \qquad \frac{2EI}{6} = 0.33$$

$$\frac{4EI}{6} = 0.67 \qquad \frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67 = 1.24 \text{ EA}$$

$$S_{21} = 0.33 \text{ EA}$$

b)  $D_1 = 0$        $D_2 = 1 \text{ k}$



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{pmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{pmatrix}$$

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Step 5

Compute [D] matrix

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$= \frac{1}{|S|} \times \text{Adj } A$$

$$\begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

$$|S| = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$= 0.8308 - 0.1089$$

$$|S| = 0.7219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

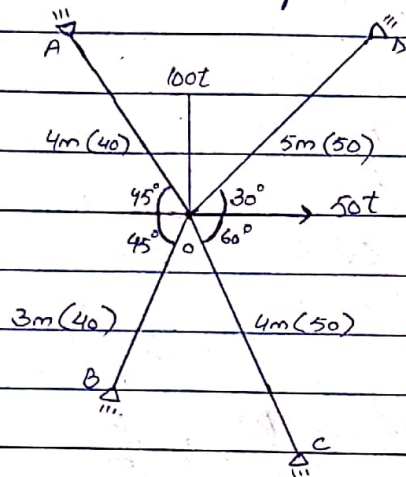
$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} E$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

0.7219

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.9711 \\ 3.8902 \end{bmatrix}$$

Q2 Analyze the pin-jointed frame .....  
 ....  $E = 2000 \text{ t/cm}^2$



Sol:

point "A"

$$\sin 45^\circ = \frac{P}{h} = \frac{P}{4}$$

$$\Rightarrow P = 2.828 \text{ m}$$

$$\cos 45^\circ = \frac{b}{4}$$

$$b = 2.825 \text{ m}$$

point "B"

$$\sin 45^\circ = \frac{P}{3}$$

$$\Rightarrow P = 2.12 \text{ m}$$

$$\cos 45^\circ = \frac{b}{h}$$

$$b = 2.12 \text{ m}$$

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point "C"

$$\sin 60^\circ = \frac{p}{h} = \frac{p}{5}$$

$$= p = 4.330 \text{ m}$$

$$\cos 60^\circ = \frac{b}{h}$$

$$b = 2.5 \text{ m}$$

point "D"

$$\sin 30^\circ = \frac{p}{h} = \frac{p}{5}$$

$$\Rightarrow p = 2.5$$

$$\cos 30^\circ = \frac{b}{5}$$

$$b = 4.33$$

"30"

$$EA_{(a)} = 2000 \times 40 = 80,000 \text{ t}$$

$$EA_{(b)} = 2000 \times 40 = 80,000 \text{ t}$$

$$EA_{(c)} = 2000 \times 50 = 100,000 \text{ t}$$

$$EA_{(d)} = 2000 \times 50 = 100,000 \text{ t}$$

Step 1

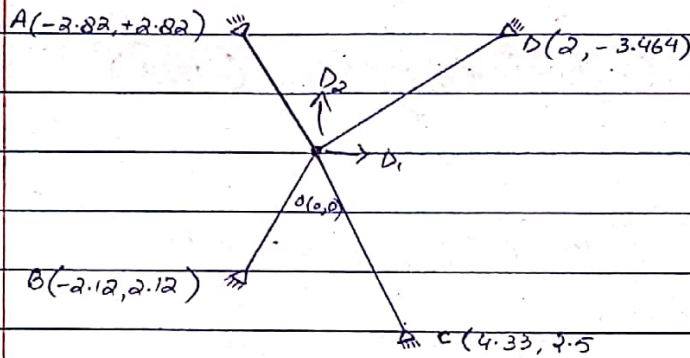
K.I

$$K.I = 2j - \gamma$$

$$= 2(5) - 8 = 2^\circ$$

Step ②

Unknown joint displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

Step ③

$[AMD]_{4 \times 2}$  and  $[S]_{2 \times 2}$

i)  $D_1 = 1, D_2 = 0$

$$AMD = EA \frac{(X_k - X_j)}{L^2}$$

$$AMD_{11} = \frac{80,000 \times (0 + 282)}{(400)^2} = 141$$

$$AMD_{21} = \frac{80,000 \times (0 + 212)}{(300)^2} = 188.44$$

$$AMD_{31} = \frac{100,000 \times (0 - 200)}{(400)^2} = 125$$

$$AMD_{41} = \frac{100,000 \times (0 - 433)}{(500)^2} = -173.2$$

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$$\text{Now } S_{11} = \sum_{k=1}^m \frac{EA}{L^3} (X_k - X_j)^2$$

$$= \frac{80,000}{400^3} \times (282)^2 + \frac{80,000}{(300)^3} \times (212)^2$$

$$+ \frac{100,000}{(400)^3} \times (-200)^2 + \frac{100,000}{(500)^3} \times (-433)^2$$

$$S_{11} = 99.405 + 133.107 + 62.5 + 149.991$$

$$S_{11} = 445.062$$

$$S_{12} = S_{21} = \sum_{k=1}^m \frac{EA}{L^3} \times (X_k - X_j) (Y_k - Y_j)$$

$$= \frac{80,000}{(400)^3} \times (282) (-282) + \frac{80,000}{(300)^3} \times (212) (212)$$

$$+ \frac{100,000}{(400)^3} \times (-200) (0 + 346) + \frac{100,000}{(500)^3} \times (433) (0 - 250)$$

$$S_{12} = S_{21} = 12.237$$

$$(ii) D_1 = 0$$

$$D_1 = 1k'$$

$$AMD = \frac{EA}{L^2} (Y_k - Y_j)$$

$$AMD_{12} = \frac{80,000}{(400)^2} \times (-282) = -141$$

$$AMD_{22} = \frac{80,000}{(300)^2} \times (212) = 188.44$$

$$AMD_{32} = \frac{100,000}{(400)^2} \times (346) = 216.25$$

$$AMD_{42} = \frac{100,000}{(500)^2} \times (-250) = -100$$

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$$\text{Now, } S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (y_k - y_j)^2$$

$$= \frac{80,000}{(400)^3} (-282)^2 + \frac{80,000}{(300)^3} (-212)^2$$

$$+ \frac{100,000}{(400)^3} (346)^2 + \frac{100,000}{(500)^3} (-250)^2$$

$$S_{22} = 469.628$$

Step ④

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.063 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$


$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step ⑤

[AM]

$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -125 & 216.25 \\ -173.2 & -100 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + 188.44 \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

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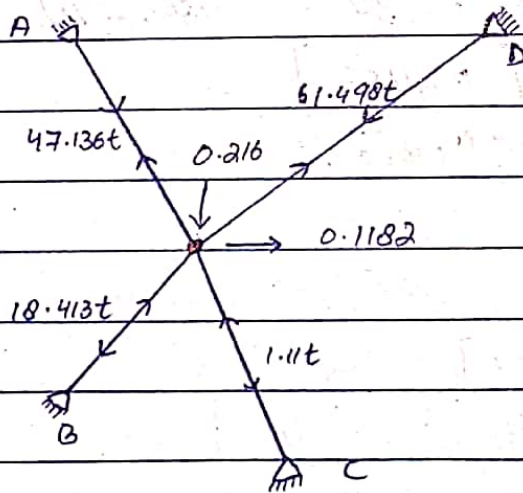
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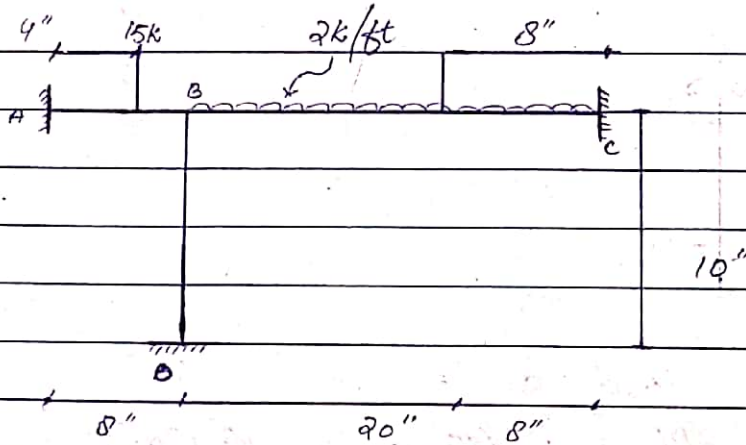
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AM <sub>1</sub>	=	16.68 + 30.46
AM <sub>2</sub>	=	22.29 - 40.70
AM <sub>3</sub>	=	-14.79 - 46.71
AM <sub>4</sub>	=	-20.49 + 21.6

AM <sub>1</sub>	=	47.136t
AM <sub>2</sub>	=	-18.413t
AM <sub>3</sub>	=	-61.49t
AM <sub>4</sub>	=	1.11t



Qno3) Analyze the rigid-joint constant



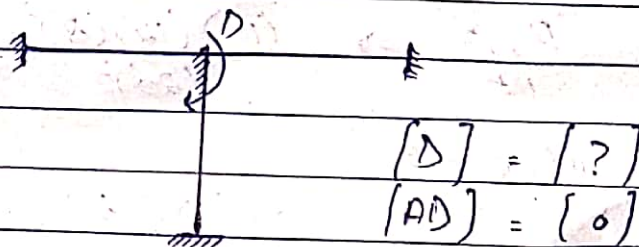
Solution:

Step ①

Determine kinematic indeterminacy.  
 $K \cdot I = 1^{\circ}$

Step ②

Unknown joint Displacement

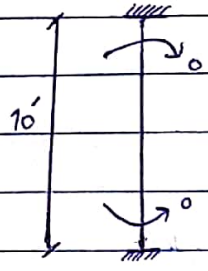
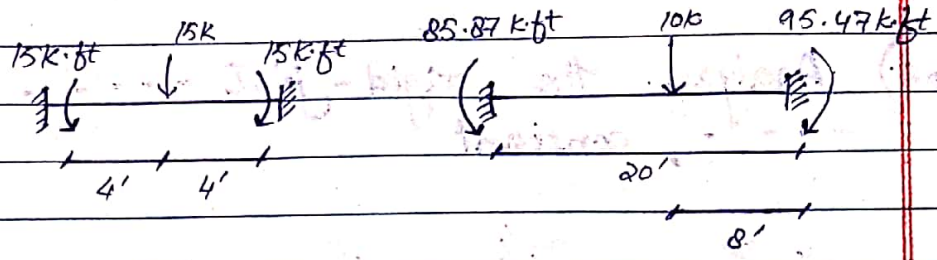


$$[D] = [?]$$

$$[AD] = [0]$$

Step ③

Compute  $[ADL]$  Matrix



⇒ Point load at center :-

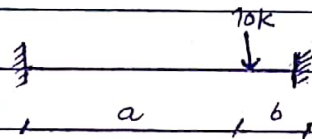
$$\frac{PL}{8} \Rightarrow \frac{(15)(8)}{8} = 15 \text{ kip}\cdot\text{ft}$$

⇒ Uniformly distributed load :-

$$\frac{wL^2}{12} \Rightarrow \frac{(2)(20)^2}{12} = 66.67 \text{ k}\cdot\text{ft}$$

⇒ Point load (not at mid) :-

∴



for left end :-

$$\frac{Pab^2}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ k}\cdot\text{ft}$$

for right end :-

$$\frac{Pa^2b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = 28.8 \text{ k}\cdot\text{ft}$$

So total moment at left end :-

$$19.2 + 66.67 = 85.87 \text{ k}\cdot\text{ft}$$

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Similarly at right ends-

$$28.8 + 66.67 = 95.47 \text{ k-ft}$$

So:

$$[ADL] = -85.87 + 15 = -70.87 \text{ k-ft}$$

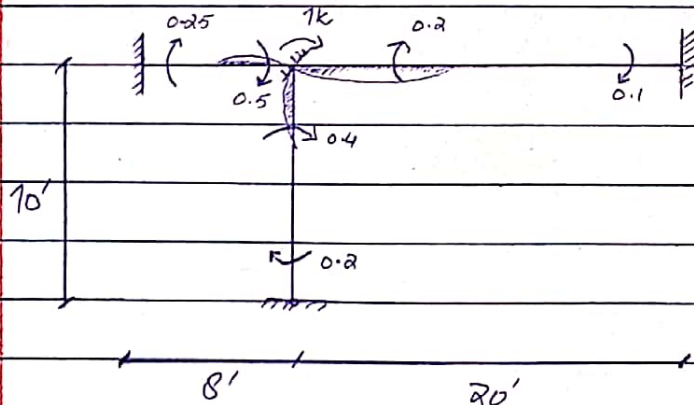
Step (4)

Determine  $[S]$  Matrix

$$[S] = [S_{ii}]$$

Now

$$D = 1 \text{ k}$$



$$\Rightarrow \frac{4EI}{8} = 0.5$$

$$\frac{2EI}{8} = 0.25$$

$$= \frac{4EI}{20} = 0.2$$

$$\frac{2EI}{20} = 0.1$$

$$= \frac{4EI}{10} = 0.4$$

$$\frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$

$$[S] = 1.1 \cdot EI$$

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Step 5

Compute D matrix

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87]$$

$$= \frac{70.87}{1.1}$$

$$[D] = [64.42] \frac{1}{EI}$$