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## Formulas and Conversions

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## Formulas and Conversions

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## Foreword

IDC Technologies specializes in providing high quality state-of-the-art technical training workshops to engineers, scientists and technicians throughout the world. More than 50,000 engineers have attended IDC's workshops over the past 10 years. The tremendous success of the technical training workshops is based in part on the enormous investment IDC puts into constant review and updating of the workshops, an unwavering commitment to the highest quality standards and most importantly - enthusiastic, experienced IDC engineers who present the workshops and keep up-to-date with consultancy work.

The objective of this booklet is to provide today's engineer with useful technical information and as aide-memoir when you need to refresh your memory.

Conversions and formulas that are important and useful to the engineer, scientist and technician, independent of discipline, are covered in this useful booklet.

Although IDC Technologies was founded in Western Australia many years ago, it now draws engineers from all countries. IDC Technologies currently has offices in Australia, Canada, Ireland, Malaysia, New Zealand, Singapore, South Africa, UK and USA.

We have produced this booklet so that you will have important formulas and conversion at your fingertips. Information at an advanced level on engineering and technical topics can be gained from attendance at one of IDC Technologies Practical Training Workshops. Held across the globe, these workshops will sharpen your skills in today's competitive engineering environment.

Other books in this series

INSTRUMENTATION Automation using PLCs, SCADA and Telemetry, Process Control and Data Acquisition

COMMUNICATIONS Data Communications, Industrial Networking, TCP/IP and Fiber Optics

ELECTRICAL Power Quality, Power Systems Protection and Substation Automation

ELECTRONICS Personal Computers, Digital Signal Processing and Analog/Digital Conversions

## 1 Definition and Abbreviations for Physical Quantities

| Symbol | Unit | Quantity |
| :--- | :--- | :--- |
| m | meter | Length |
| kg | kilogram | Mass |
| s | second | Time |
| A | ampere | Electric current |
| K | kelvin | Thermodynamic temp |
| cd | candela | Luminous intensity |


| Quantity | Unit | Symbol | Equivalent |
| :--- | :--- | :--- | :--- |
| Plane angle | radian | rad | - |
| Force | newton | N | $\mathrm{kg} \cdot \mathrm{m} / \mathrm{s}^{2}$ |
| Work, energy | heat | joule | $\mathrm{J} \cdot \mathrm{N} \cdot \mathrm{m}$ |
| Power | watt | W | $\mathrm{J} / \mathrm{s}$ |
| Frequency | hertz | Hz | $\mathrm{s}^{-1}$ |
| Viscosity: kinematic | - | $\mathrm{m}^{2} / \mathrm{s}$ | 10 c St (Centistoke) |
| Viscosity: Dynamic | - | $\mathrm{Ns} / \mathrm{m}^{2}$ | $10^{3} \mathrm{cP}($ Centipoise $)$ |
| Pressure | - | Pa or $\mathrm{N} / \mathrm{m}^{2}$ | pascal, Pa |


| Symbol | Prefix | Factor by which unit is <br> multiplied |
| :--- | :--- | :--- |
| T | Tera | $10^{12}$ |
| G | Giga | $10^{9}$ |
| M | Mega | $10^{6}$ |
| k | Kilo | $10^{3}$ |
| h | Hecto | $10^{2}$ |
| da | Deca | 10 |
| d | Deci | $10^{-1}$ |
| c | Centi | $10^{-2}$ |
| m | Milli | $10^{-3}$ |
| m | Micro | $10^{-6}$ |
| n | Nano | $10^{-9}$ |
| p | Pico | $10^{-12}$ |
|  |  |  |


| Quantity | Electrical unit | Symbol | Derived unit |
| :--- | :--- | :--- | :--- |
| Potential | Volt | V | W/A |
| Resistance | Ohm | $\Omega$ | V/A |
| Charge | Coulomb | C | A•s |
| Capacitance | Farad | F | A•s/V |
| Electric field strength | - | $\mathrm{V} / \mathrm{m}$ | - |
| Electric flux density | - | $\mathrm{C} / \mathrm{m}^{2}$ | - |


| Quantity | Magnetic unit | Symbol | Derived unit |
| :--- | :--- | :--- | :--- |
| Magnetic flux | Weber | Wb | $\mathrm{V} \cdot \mathrm{s}=\mathrm{N} \cdot \mathrm{m} / \mathrm{A}$ |
| Inductance | Henry | H | $\mathrm{V} \cdot \mathrm{s} / \mathrm{A}=\mathrm{N} \cdot \mathrm{m} / \mathrm{A}^{2}$ |
| Magnetic field strength | - | $\mathrm{A} / \mathrm{m}$ | - |
| Magnetic flux density | Tesla | T | $\mathrm{Wb} / \mathrm{m}^{2}=(\mathrm{N}) /(\mathrm{Am})$ |

## 2 Units of Physical Quantities

| Conversion Factors (general): |
| :--- |
| 1 acre $=43,560$ square feet |
| 1 cubic foot $=7.5$ gallons |
| 1 foot $=0.305$ meters |
| 1 gallon $=3.79$ liters |
| 1 gallon $=8.34$ pounds |
| 1 grain per gallon $=17.1 \mathrm{mg} / \mathrm{L}$ |
| 1 horsepower $=0.746$ kilowatts |
| 1 million gallons per day $=694$ gallons per minute |
| 1 pound $=0.454$ kilograms |
| 1 pound per square inch $=2.31$ feet of water |
| Degrees Celsius $=($ Degrees Fahrenheit -32$)(5 / 9)$ |
| Degrees Fahrenheit $=($ Degrees Celsius $)(9 / 5)+32$ |
| $1 \%=10,000$ mg/L |


| Name | To convert from | To | Multiply by | Divide by |
| :---: | :---: | :---: | :---: | :---: |
| Acceleration | $\mathrm{ft} / \mathrm{sec}^{2}$ | $\mathrm{m} / \mathrm{s}^{2}$ | 0.3048 | 3.2810 |
| Area | acre | $\mathrm{m}^{2}$ | 4047 | $2.471 \mathrm{E}-04$ |
| Area | $\mathrm{ft}^{2}$ | $\mathrm{m}^{2}$ | $9.294 \mathrm{E}-02$ | 10.7600 |
| Area | hectare | $\mathrm{m}^{2}$ | $1.000 \mathrm{E}+04$ | $1.000 \mathrm{E}-04$ |
| Area | $i n^{2}$ | $\mathrm{m}^{2}$ | $6.452 \mathrm{E}-04$ | 1550 |
| Density | $\mathrm{g} / \mathrm{cm}^{3}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | 1000 | $1.000 \mathrm{E}-03$ |
| Density | $\mathrm{lbm} / \mathrm{ft}^{3}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | 16.02 | $6.243 \mathrm{E}-02$ |
| Density | $\mathrm{lbm} / \mathrm{in}^{3}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | $2.767 \mathrm{E}+04$ | $3.614 \mathrm{E}-05$ |
| Density | $\mathrm{lb} \cdot \mathrm{s}^{2} / \mathrm{in}^{4}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | $1.069 \mathrm{E}+07$ | $9.357 \mathrm{E}-08$ |
| Density | slug/ $\mathrm{ft}^{3}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | 515.40 | $1.940 \mathrm{E}-03$ |
| Energy | BTU | J | 1055 | $9.478 \mathrm{E}-04$ |
| Energy | cal | J | 4.1859 | 0.2389 |
| Energy | erg | J | $1.000 \mathrm{E}-07$ | $1.000 \mathrm{E}+07$ |
| Energy | eV | J | $1.602 \mathrm{E}-19$ | $6.242 \mathrm{E}+18$ |
| Energy | Ft.lbf | J | 1.3557 | 0.7376 |
| Energy | kiloton TNT | J | $4.187 \mathrm{E}+12$ | $2.388 \mathrm{E}-13$ |
| Energy | KW•hr | J | $3.600 \mathrm{E}+06$ | $2.778 \mathrm{E}-07$ |
| Energy | Megaton TNT | J | $4.187 \mathrm{E}+15$ | $2.388 \mathrm{E}-16$ |
| Force | Dyne | N | $1.000 \mathrm{E}-05$ | $1.000 \mathrm{E}+05$ |
| Force | Lbf | N | 4.4484 | 0.2248 |
| Force | Ozf | N | 0.2780 | 3.5968 |
| Heat capacity | BTU/lbm $\cdot{ }^{\circ} \mathrm{F}$ | $\mathrm{J} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$ | 4188 | $2.388 \mathrm{E}-04$ |
| Heat transfer coefficient | $\mathrm{BTU} / \mathrm{hr} \cdot \mathrm{ft}^{2} \cdot{ }^{\circ} \mathrm{F}$ | $\mathrm{W} / \mathrm{m}^{2} \cdot{ }^{\circ} \mathrm{C}$ | 5.6786 | 0.1761 |
| Length | AU | m | $1.496 \mathrm{E}+11$ | $6.685 \mathrm{E}-12$ |
| Length | ft | m | 0.3048 | 3.2810 |
| Length | in | m | $2.540 \mathrm{E}-02$ | 39.3700 |
| Length | mile | m | 1609 | $6.214 \mathrm{E}-04$ |
| Length | Nautical mile | m | 1853 | $5.397 \mathrm{E}-04$ |
| Length | parsec | m | $3.085 \mathrm{E}+16$ | $3.241 \mathrm{E}-17$ |
| Mass | amu | kg | $1.661 \mathrm{E}-27$ | $6.022 \mathrm{E}+26$ |
| Mass | lbm | kg | 0.4535 | 2.2050 |
| Mass | $\mathrm{lb} \cdot \mathrm{s}^{2} / \mathrm{in}$ | kg | 1200.00 | $5.711 \mathrm{E}-03$ |
| Mass | slug | kg | 14.59 | $6.853 \mathrm{E}-02$ |


| Name | To convert from | To | Multiply by | Divide by |
| :---: | :---: | :---: | :---: | :---: |
| Mass flow rate | $\mathrm{lbm} / \mathrm{hr}$ | kg/s | $1.260 \mathrm{E}-04$ | 7937 |
| Mass flow rate | $\mathrm{lbm} / \mathrm{sec}$ | kg/s | 0.4535 | 2.2050 |
| Moment of inertia | $\mathrm{ft} \cdot \mathrm{lb} \cdot \mathrm{s}^{2}$ | $\mathrm{kg} \cdot \mathrm{m}^{2}$ | 1.3557 | 0.7376 |
| Moment of inertia | $\mathrm{in} \cdot \mathrm{lb} \cdot \mathrm{s}^{2}$ | $\mathrm{kg} \cdot \mathrm{m}^{2}$ | 0.1130 | 8.8510 |
| Moment of inertia | $\mathrm{oz} \cdot \mathrm{in} \cdot \mathrm{s}^{2}$ | $\mathrm{kg} \cdot \mathrm{m}^{2}$ | 7.062E-03 | 141.60 |
| Power | BTU/hr | W | 0.2931 | 3.4120 |
| Power | hp | W | 745.71 | $1.341 \mathrm{E}-03$ |
| Power | tons of refrigeration | W | 3516 | $2.844 \mathrm{E}-04$ |
| Pressure | bar | Pa | $1.000 \mathrm{E}+05$ | $1.000 \mathrm{E}-05$ |
| Pressure | dyne/ $\mathrm{cm}^{2}$ | Pa | 0.1000 | 10.0000 |
| Pressure | in. mercury | Pa | 3377 | $2.961 \mathrm{E}-04$ |
| Pressure | in. water | Pa | 248.82 | $4.019 \mathrm{E}-03$ |
| Pressure | $\mathrm{kgf} / \mathrm{cm}^{2}$ | Pa | $9.807 \mathrm{E}+04$ | $1.020 \mathrm{E}-05$ |
| Pressure | $\mathrm{lbf} / \mathrm{ft}^{2}$ | Pa | 47.89 | $2.088 \mathrm{E}-02$ |
| Pressure | $\mathrm{lbf} / \mathrm{in}^{2}$ | Pa | 6897 | $1.450 \mathrm{E}-04$ |
| Pressure | mbar | Pa | 100.00 | $1.000 \mathrm{E}-02$ |
| Pressure | microns mercury | Pa | 0.1333 | 7.501 |
| Pressure | mm mercury | Pa | 133.3 | $7.501 \mathrm{E}-03$ |
| Pressure | std atm | Pa | $1.013 \mathrm{E}+05$ | $9.869 \mathrm{E}-06$ |
| Specific heat | BTU/lbm $\cdot{ }^{\circ} \mathrm{F}$ | $\mathrm{J} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$ | 4186 | $2.389 \mathrm{E}-04$ |
| Specific heat | $\mathrm{cal} / \mathrm{g} \cdot{ }^{\circ} \mathrm{C}$ | $\mathrm{J} / \mathrm{kg} \cdot{ }^{\circ} \mathrm{C}$ | 4186 | $2.389 \mathrm{E}-04$ |
| Temperature | ${ }^{\circ} \mathrm{F}$ | ${ }^{\circ} \mathrm{C}$ | 0.5556 | 1.8000 |
| Thermal conductivity | BTU/hr•ft ${ }^{\circ} \mathrm{F}$ | $\mathrm{W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$ | 1.7307 | 0.5778 |
| Thermal conductivity | BTU.in/hr.ft ${ }^{2} \cdot{ }^{\circ} \mathrm{F}$ | $\mathrm{W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$ | 0.1442 | 6.9340 |
| Thermal conductivity | $\mathrm{cal} / \mathrm{cm} \cdot \mathrm{s} \cdot{ }^{\circ} \mathrm{C}$ | $\mathrm{W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$ | 418.60 | $2.389 \mathrm{E}-03$ |
| Thermal conductivity | $\mathrm{cal} / \mathrm{ft} \cdot \mathrm{hr} \cdot{ }^{\circ} \mathrm{F}$ | $\mathrm{W} / \mathrm{m} \cdot{ }^{\circ} \mathrm{C}$ | $6.867 \mathrm{E}-03$ | 145.62 |


| Name | To convert from | To | Multiply by | Divide by |
| :--- | :--- | :--- | :--- | :--- |
| Time | day | S | $8.640 \mathrm{E}+04$ | $1.157 \mathrm{E}-05$ |
| Time | sidereal year | S | $3.156 \mathrm{E}+07$ | $3.169 \mathrm{E}-08$ |
| Torque | $\mathrm{ft} \cdot \mathrm{lbf}$ | $\mathrm{N} \cdot \mathrm{m}$ | 1.3557 | 0.7376 |
| Torque | in $\cdot \mathrm{lbf}$ | $\mathrm{N} \cdot \mathrm{m}$ | 0.1130 | 8.8504 |
| Torque | $\mathrm{In} \cdot \mathrm{ozf}$ | $\mathrm{N} \cdot \mathrm{m}$ | $7.062 \mathrm{E}-03$ | 141.61 |
| Velocity | $\mathrm{ft} / \mathrm{min}$ | $\mathrm{m} / \mathrm{s}$ | $5.079 \mathrm{E}-03$ | 196.90 |
| Velocity | $\mathrm{ft} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ | 0.3048 | 3.2810 |
| Velocity | $\mathrm{Km} / \mathrm{hr}$ | $\mathrm{m} / \mathrm{s}$ | 0.2778 | 3.6000 |
| Velocity | miles $/ \mathrm{hr}$ | $\mathrm{m} / \mathrm{s}$ | 0.4470 | 2.2370 |
| Viscosity - absolute | centipose | $\mathrm{N} \cdot \mathrm{s} / \mathrm{m}^{2}$ | $1.000 \mathrm{E}-03$ | 1000 |
| Viscosity - absolute | $\mathrm{g} / \mathrm{cm} \cdot \mathrm{s}$ | $\mathrm{N} \cdot \mathrm{s} / \mathrm{m}^{2}$ | 0.1000 | 10 |
| Viscosity - absolute | $\mathrm{lbf} / \mathrm{ft} \cdot \mathrm{s}$ | $\mathrm{N} \cdot \mathrm{s} / \mathrm{m}^{2}$ | 47.87 | $2.089 \mathrm{E}-02$ |
| Viscosity - absolute | $\mathrm{lbm} / \mathrm{ft} \cdot \mathrm{s}$ | $\mathrm{N} \cdot \mathrm{s} / \mathrm{m}^{2}$ | 1.4881 | 0.6720 |
| Viscosity - kinematic | centistoke | $\mathrm{m}^{2} / \mathrm{s}$ | $1.000 \mathrm{E}-06$ | $1.000 \mathrm{E}+06$ |
| Viscosity - kinematic | $\mathrm{ft} / \mathrm{sec}$ | $\mathrm{m}^{2} / \mathrm{s}$ | $9.294 \mathrm{E}-02$ | 10.7600 |
| Volume | $\mathrm{ft}^{3}$ | $\mathrm{~m}^{3}$ | $2.831 \mathrm{E}-02$ | 35.3200 |
| Volume | $\mathrm{in}^{3}$ | $\mathrm{~m}^{3}$ | $1.639 \mathrm{E}-05$ | $6.102 \mathrm{E}+04$ |
| Volume | Liters | $\mathrm{m}^{3}$ | $1.000 \mathrm{E}-03$ | 1000 |
| Volume | $\mathrm{U} . \mathrm{S}$. gallons | $\mathrm{m}^{3}$ | $3.785 \mathrm{E}-03$ | 264.20 |
| Volume flow rate | $\mathrm{ft}^{3} / \mathrm{min}$ | $\mathrm{m}^{3} / \mathrm{s}$ | $4.719 \mathrm{E}-04$ | 2119 |
| Volume flow rate | $\mathrm{U} . \mathrm{S}$. gallons $/ \mathrm{min}$ | $\mathrm{m}^{3} / \mathrm{s}$ | $6.309 \mathrm{E}-05$ | $1.585 \mathrm{E}+04$ |

## A. DISTANCE (Length)

## Conversions

| Multiply |  | By |
| :--- | :--- | :--- |
| LENGTH |  |  |


| To Convert | To | Multiply By |
| :---: | :---: | :---: |
| Cables | Fathoms | 120 |
| Cables | Meters | 219.456 |
| Cables | Yards | 240 |
| Centimeters | Meters | 0.01 |
| Centimeters | Yards | 0.01093613 |
| Centimeters | Feet | 0.0328084 |
| Centimeters | Inches | 0.3937008 |
| Chains, (Surveyor's) | Rods | 4 |
| Chains, (Surveyor's) | Meters | 20.1168 |
| Chains, (Surveyor's) | Feet | 66 |
| Fathoms | Meters | 1.8288 |
| Fathoms | Feet | 6 |
| Feet | Statute Miles | 0.00018939 |
| Feet | Kilometers | 0.0003048 |
| Feet | Meters | 0.3048 |
| Feet | Yards | 0.3333333 |
| Feet | Inches | 12 |
| Feet | Centimeters | 30.48 |
| Furlongs | Statute Miles | 0.125 |
| Furlongs | Meters | 201.168 |
| Furlongs | Yards | 220 |
| Furlongs | Feet | 660 |
| Furlongs | Inches | 7920 |
| Hands (Height Of Horse) | Inches | 4 |
| Hands (Height Of Horse) | Centimeters | 10.16 |
| Inches | Meters | 0.0254 |
| Inches | Yards | 0.02777778 |
| Inches | Feet | 0.08333333 |
| Inches | Centimeters | 2.54 |
| Inches | Millimeters | 25.4 |
| Kilometers | Statute Miles | 0.621371192 |
| Kilometers | Meters | 1000 |
| Leagues, Nautical | Nautical Miles | 3 |
| Leagues, Nautical | Kilometers | 5.556 |
| Leagues, Statute | Statute Miles | 3 |
| Leagues, Statute | Kilometers | 4.828032 |
| Links, (Surveyor's) | Chains | 0.01 |
| Links, (Surveyor's) | Inches | 7.92 |
| Links, (Surveyor's) | Centimeters | 20.1168 |
| Meters | Statute Miles | 0.000621371 |
| Meters | Kilometers | 0.001 |
| Meters | Yards | 1.093613298 |
| Meters | Feet | 3.280839895 |
| Meters | Inches | 39.370079 |
| Meters | Centimeters | 100 |
| Meters | Millimeters | 1000 |
| Microns | Meters | 0.000001 |
| Microns | Inches | 0.0000394 |
| Miles, Nautical | Statute Miles | 1.1507794 |
| Miles, Nautical | Kilometers | 1.852 |
| Miles, Statute | Kilometers | 1.609344 |
| Miles, Statute | Furlongs | 8 |


| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Miles, Statute | Rods | 320 |
| Miles, Statute | Meters | 1609.344 |
| Miles, Statute | Yards | 1760 |
| Miles, Statute | Feet | 5280 |
| Miles, Statute | Inches | 63360 |
| Miles, Statute | Centimeters | 160934.4 |
| Millimeters | Inches | 0.039370079 |
| Mils | Inches | 0.001 |
| Mils | Millimeters | 0.0254 |
| Paces (US) | Inches | 30 |
| Paces (US) | Centimeters | 76.2 |
| Points (Typographical) | Inches | 0.013837 |
| Points (Typographical) | Millimeters | 0.3514598 |
| Rods | Meters | 5.0292 |
| Rods | Yards | 5.5 |
| Rods | Feet | 16.5 |
| Spans | Inches | 9 |
| Spans | Centimeters | 22.86 |
| Yards | Miles | 0.00056818 |
| Yards | Meters | 0.9144 |
| Yards | Feet | 3 |
| Yards | Inches | 36 |
| Yards | Centimeters | 91.44 |
|  |  |  |


| Conversion |  |
| :---: | :---: |
| Length |  |
| $1 \mathrm{ft}=12 \mathrm{in}$ | $1 \mathrm{yd}=3 \mathrm{ft}$ |
| $1 \mathrm{~cm}=0.3937 \mathrm{in}$ | $1 \mathrm{in}=2.5400 \mathrm{~cm}$ |
| $1 \mathrm{~m}=3.281 \mathrm{ft}$ | $1 \mathrm{ft}=0.3048 \mathrm{~m}$ |
| $1 \mathrm{~m}=1.0936 \mathrm{yd}$ | $1 \mathrm{yd}=0.9144 \mathrm{~m}$ |
| $1 \mathrm{~km}=0.6214$ mile | 1 mile $=1.6093 \mathrm{~km}$ |
| 1 furlong $=40$ rods | 1 fathom $=6 \mathrm{ft}$ |
| 1 statute mile $=8$ furlongs | $1 \mathrm{rod}=5.5 \mathrm{yd}$ |
| 1 statute mile $=5280 \mathrm{ft}$ | $1 \mathrm{in}=100 \mathrm{mils}$ |
| 1 nautical mile $=6076 \mathrm{ft}$ | 1 light year $=9.461 \times 10^{15} \mathrm{~m}$ |
| 1 league $=3$ miles | $1 \mathrm{mil}=2.540 \times 10^{-5} \mathrm{~m}$ |
| Area |  |
| $1 \mathrm{ft}^{2}=144 \mathrm{in}^{2}$ | 1 acre $=160 \mathrm{rod}^{2}$ |
| $1 \mathrm{yd}^{2}=9 \mathrm{ft}^{2}$ | 1 acre $=43,560 \mathrm{ft}^{2}$ |
| $1 \mathrm{rod}^{2}=30.25 \mathrm{yd}^{2}$ | 1 mile $^{2}=640$ acres |
| $1 \mathrm{~cm}^{2}=0.1550 \mathrm{in}^{2}$ | $1 \mathrm{in}^{2}=6.4516 \mathrm{~cm}^{2}$ |
| $1 \mathrm{~m}^{2}=10.764 \mathrm{ft}^{2}$ | $1 \mathrm{ft}^{2}=0.0929 \mathrm{~m}^{2}$ |
| $1 \mathrm{~km}^{2}=0.3861$ mile $^{2}$ | $1 \mathrm{mile}^{2}=2.590 \mathrm{~km}^{2}$ |
| Volume |  |
| $1 \mathrm{~cm}^{3}=0.06102 \mathrm{in}^{3}$ | $1 \mathrm{in}^{3}=16.387 \mathrm{~cm}^{3}$ |
| $1 \mathrm{~m}^{3}=35.31 \mathrm{ft}^{3}$ | $1 \mathrm{ft}^{3}=0.02832 \mathrm{~m}^{3}$ |
| 1 Litre $=61.024 \mathrm{in}^{3}$ | $1 \mathrm{in}^{3}=0.0164$ litre |
| 1 Litre $=0.0353 \mathrm{ft}^{3}$ | $1 \mathrm{ft}^{3}=28.32$ litres |
| 1 Litre $=0.2642$ gal. (U.S.) | $1 \mathrm{yd}^{3}=0.7646 \mathrm{~m}^{3}$ |
| 1 Litre $=0.0284$ bu (U.S.) | 1 gallon (US) $=3.785$ litres |
| 1 Litre $=1000.000 \mathrm{~cm}^{3}$ | 1 gallon (US) $=3.785 \times 10^{-3} \mathrm{~m}^{3}$ |
| 1 Litre $=1.0567$ qt. (liquid) or 0.9081 qt. (dry) | 1 bushel (US) = 35.24 litres |
| 1 oz (US fluid) $=2.957 \times 10^{-5} \mathrm{~m}^{3}$ | 1 stere $=1 \mathrm{~m}^{3}$ |
| Liquid Volume |  |
| 1 gill $=4$ fluid ounces | 1 barrel $=31.5$ gallons |
| 1 pint $=4$ gills | 1 hogshead $=2 \mathrm{bbl}$ ( 63 gal ) |
| 1 quart $=2$ pints | 1 tun $=252$ gallons |
| 1 gallon $=4$ quarts | 1 barrel (petrolum) $=42$ gallons |
| Dry Volume |  |
| 1 quart $=2$ pints | 1 quart $=67.2 \mathrm{in}^{3}$ |
| 1 peck $=8$ quarts | 1 peck $=537.6 \mathrm{in}^{3}$ |
| 1 bushel $=4$ pecks | 1 bushel $=2150.5 \mathrm{in}^{3}$ |

## B. Area

## Conversions

| Multiply | By | To obtain |
| :--- | :--- | :--- |
| AREA |  |  |
| acre | $4,046.856$ | meter $^{2}\left(\mathrm{~m}^{2}\right)$ |
| acre | 0.4046856 | hectare |
| centimeter |  |  |
| centimeter $^{2}$ | 0.1550003 | inch $^{2}$ |
| foot $^{2}$ | 0.001076391 | foot $^{2}$ |


| Multiply | By | To obtain |
| :--- | :--- | :--- |
| foot $^{2}$ | $929.0304^{2}$ | centimeter $^{2}\left(\mathrm{~cm}^{2}\right)$ |
| foot $^{2}$ | $92,903.04$ | millimeter ${ }^{2}\left(\mathrm{~mm}^{2}\right)$ |
| hectare $^{\text {inch }}$ 2 | 2.471054 | acre |
| inch $^{2}$ | 645.16 | millimeter ${ }^{2}\left(\mathrm{~mm}^{2}\right)$ |
| inch $^{2}$ | 6.4516 | centimeter $\left(\mathrm{cm}^{2}\right)$ |
| inch $^{2}$ | 0.00064516 | meter $^{2}\left(\mathrm{~m}^{2}\right)$ |
| meter $^{2}$ | $1,550.003$ | inch $^{2}$ |
| meter $^{2}$ | 10.763910 | foot $^{2}$ |
| meter $^{2}$ | 1.195990 | yard $^{2}$ |
| meter $^{2}$ | 0.0002471054 | acre $^{2}$ |
| millimeter $^{2}$ | 0.00001076391 | foot $^{2}$ |
| millimeter $^{2}$ | 0.001550003 | inch $^{2}$ |
| yard $^{2}$ | 0.8361274 | meter $^{2}\left(\mathrm{~m}^{2}\right)$ |

## C. Volume

## Conversions

## Metric Conversion Factors: Volume (including Capacity)

| Multiply | By | To obtain |
| :---: | :---: | :---: |
| VOLUME (including CAPACITY) |  |  |
| centimeter ${ }^{3}$ | 0.06102376 | inch ${ }^{3}$ |
| foot ${ }^{3}$ | 0.028311685 | meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$ |
| foot ${ }^{3}$ | 28.31685 | liter |
| gallon (UK liquid) | 0.004546092 | meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$ |
| gallon (UK liquid) | 4.546092 | litre |
| gallon (US liquid) | 0.003785412 | meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$ |
| gallon (US liquid) | 3.785412 | liter |
| inch $^{3}$ | 16,387.06 | millimeter ${ }^{3}\left(\mathrm{~mm}^{3}\right)$ |
| inch $^{3}$ | 16.38706 | centimeter ${ }^{3}\left(\mathrm{~cm}^{3}\right)$ |
| inch $^{3}$ | 0.00001638706 | meter ${ }^{3}$ ( $\mathrm{m}^{3}$ ) |
| Liter | $0.001 *$ | meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$ |
| Liter | 0.2199692 | gallon (UK liquid) |
| Liter | 0.2641720 | gallon (US liquid) |
| Liter | 0.03531466 | foot ${ }^{3}$ |
| meter $^{3}$ | 219.9692 | gallon (UK liquid) |
| meter $^{3}$ | 264.1720 | gallon (US liquid) |
| meter $^{3}$ | 35.31466 | foot ${ }^{3}$ |
| meter $^{3}$ | 1.307951 | yard ${ }^{3}$ |
| meter $^{3}$ | 1000.* | liter |
| meter $^{3}$ | 61,023.76 | inch $^{3}$ |
| millimeter ${ }^{3}$ | 0.00006102376 | inch ${ }^{3}$ |
| Yard ${ }^{3}$ | 0.7645549 | meter $^{3}\left(\mathrm{~m}^{3}\right)$ |

## D. Mass and Weight

## Conversions

| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Carat | Milligrams | 200 |
| Drams, Avoirdupois | Avoirdupois Ounces | 0.06255 |


| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Drams, Avoirdupois | Grams | 1.7718452 |
| Drams, Avoirdupois | Grains | 27.344 |
| Drams, Troy | Troy Ounces | 0.125 |
| Drams, Troy | Scruples | 3 |
| Drams, Troy | Grams | 3.8879346 |
| Drams, Troy | Grains | 60 |
| Grains | Kilograms | $6.47989 \mathrm{E}-05$ |
| Grains | Avoirdupois Pounds | 0.00014286 |
| Grains | Troy Pounds | 0.00017361 |
| Grains | Troy Ounces | 0.00208333 |
| Grains | Avoirdupois Ounces | 0.00228571 |
| Grains | Troy Drams | 0.0166 |
| Grains | Avoirdupois Drams | 0.03657143 |
| Grains | Pennyweights | 0.042 |
| Grains | Scruples | 0.05 |
| Grains | Grams | 0.06479891 |
| Grains | Milligrams | 64.79891 |
| Grams | Kilograms | 0.001 |
| Grams | Avoirdupois Pounds | 0.002204623 |
| Grams | Troy Pounds | 0.00267923 |
| Grams | Troy Ounces | 0.032150747 |
| Grams | Avoirdupois Ounces | 0.035273961 |
| Grams | Avoirdupois Drams | 0.56438339 |
| Grams | Grains | 15.432361 |
| Grams | Milligrams | 1000 |
| Hundredweights, Long | Long Tons | 0.05 |
|  |  |  |



| To Convert | To | Multiply By |
| :---: | :---: | :---: |
| Hundredweights, Long | Metric Tons | 0.050802345 |
| Hundredweights, Long | Short Tons | 0.056 |
| Hundredweights, Long | Kilograms | 50.802345 |
| Hundredweights, Long | Avoirdupois Pounds | 112 |
| Hundredweights, Short | Long Tons | 0.04464286 |
| Hundredweights, Short | Metric Tons | 0.045359237 |
| Hundredweights, Short | Short Tons | 0.05 |
| Hundredweights, Short | Kilograms | 45.359237 |
| Hundredweights, Short | Avoirdupois Pounds | 100 |
| Kilograms | Long Tons | 0.0009842 |
| Kilograms | Metric Tons | 0.001 |
| Kilograms | Short Tons | 0.00110231 |
| Kilograms | Short Hundredweights | 0.02204623 |
| Kilograms | Avoirdupois Pounds | 2.204622622 |
| Kilograms | Troy Pounds | 2.679229 |
| Kilograms | Troy Ounces | 32.15075 |
| Kilograms | Avoirdupois Ounces | 35.273962 |
| Kilograms | Avoirdupois Drams | 564.3834 |
| Kilograms | Grams | 1000 |
| Kilograms | Grains | 15432.36 |
| Milligrams | Grains | 0.015432358 |
| Ounces, Avoirdupois | Kilograms | 0.028349523 |
| Ounces, Avoirdupois | Avoirdupois Pounds | 0.0625 |
| Ounces, Avoirdupois | Troy Pounds | 0.07595486 |
| Ounces, Avoirdupois | Troy Ounces | 0.9114583 |
| Ounces, Avoirdupois | Avoirdupois Drams | 16 |
| Ounces, Avoirdupois | Grams | 28.34952313 |
| Ounces, Avoirdupois | Grains | 437.5 |
| Ounces, Troy | Avoirdupois Pounds | 0.06857143 |
| Ounces, Troy | Troy Pounds | 0.0833333 |
| Ounces, Troy | Avoirdupois Ounces | 1.097143 |
| Ounces, Troy | Troy Drams | 8 |
| Ounces, Troy | Avoirdupois Drams | 17.55429 |
| Ounces, Troy | Pennyweights | 20 |
| Ounces, Troy | Grams | 31.1034768 |
| Ounces, Troy | Grains | 480 |
| Pennyweights | Troy Ounces | 0.05 |
| Pennyweights | Grams | 1.55517384 |
| Pennyweights | Grains | 24 |
| Pounds, Avoirdupois | Long Tons | 0.000446429 |
| Pounds, Avoirdupois | Metric Tons | 0.000453592 |
| Pounds, Avoirdupois | Short Tons | 0.0005 |
| Pounds, Avoirdupois | Quintals | 0.00453592 |
| Pounds, Avoirdupois | Kilograms | 0.45359237 |
| Pounds, Avoirdupois | Troy Pounds | 1.215278 |
| Pounds, Avoirdupois | Troy Ounces | 14.58333 |
| Pounds, Avoirdupois | Avoirdupois Ounces | 16 |
| Pounds, Avoirdupois | Avoirdupois Drams | 256 |
| Pounds, Avoirdupois | Grams | 453.59237 |
| Pounds, Avoirdupois | Grains | 7000 |
| Pounds, Troy | Kilograms | 0.373241722 |
| Pounds, Troy | Avoirdupois Pounds | 0.8228571 |


| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Pounds, Troy | Troy Ounces | 12 |
| Pounds, Troy | Avoirdupois Ounces | 13.16571 |
| Pounds, Troy | Avoirdupois Drams | 210.6514 |
| Pounds, Troy | Pennyweights | 240 |
| Pounds, Troy | Grams | 373.2417216 |
| Pounds, Troy | Grains | 5760 |
| Quintals | Metric Tons | 0.1 |
| Quintals | Kilograms | 100 |
| Quintals | Avoirdupois Pounds | 220.46226 |
| Scruples | Troy Drams | 0.333 |
| Scruples | Grams | 1.2959782 |
| Scruples | Grains | 20 |
| Tons, Long (Deadweight) | Metric Tons | 1.016046909 |
| Tons, Long (Deadweight) | Short Tons | 1.12 |
| Tons, Long (Deadweight) | Long Hundredweights | 20 |
| Tons, Long (Deadweight) | Short Hundredweights | 22.4 |
| Tons, Long (Deadweight) | Kilograms | 1016.04691 |
| Tons, Long (Deadweight) | Avoirdupois Pounds | 2240 |
| Tons, Long (Deadweight) | Avoirdupois Ounces | 35840 |
| Tons, Metric | Long Tons | 0.9842065 |
| Tons, Metric | Short Tons | 1.1023113 |
| Tons, Metric | Quintals | 10 |
| Tons, Metric | Long Hundredweights | 19.68413072 |
| Tons, Metric | Short Hundredweights | 22.04623 |
| Tons, Metric | Kilograms | 1000 |
| Tons, Metric | Avoirdupois Pounds | 2204.623 |
| Tons, Metric | Troy Ounces | 32150.75 |
| Tons, Short | Long Tons | 0.8928571 |
| Tons, Short | Metric Tons | 0.90718474 |
| Tons, Short | Long Hundredweights | 17.85714 |
| Tons, Short | Short Hundredweights | 20 |
| Tons, Short | Kilograms | 907.18474 |
| Tons, Short |  | 2000 |
|  |  |  |

## E. Density

## Conversions

| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Grains/imp. Gallon | Parts/million | 14.286 |
| Grains/US gallon | Parts/million | 17.118 |
| Grains/US gallon | Pounds/million gal | 142.86 |
| Grams/cu. Cm | Pounds/mil-foot | $3.405 \mathrm{E}-07$ |
| Grams/cu. Cm | Pounds/cu. in | 0.03613 |
| Grams/cu. Cm | Pounds/cu. ft | 62.43 |
| Grams/liter | Pounds/cu. ft | 0.062427 |
| Grams/liter | Pounds/1000 gal | 8.345 |
| Grams/liter | Grains/gal | 58.417 |
| Grams/liter | Parts/million | 1000 |
| Kilograms/cu meter | Pounds/mil-foot | $3.405 \mathrm{E}-10$ |
| Kilograms/cu meter | Pounds/cu in | 0.00003613 |
| Kilograms/cu meter | Grams/cu cm | 0.001 |


| To Convert | To | Multiply By |
| :--- | :--- | :--- |
| Kilograms/cu meter | Pound/cu ft | 0.06243 |
| Milligrams/liter | Parts/million | 1 |
| Pounds/cu ft | Pounds/mil-foot | $5.456 \mathrm{E}-09$ |
| Pounds/cu ft | Pounds/cu in | 0.0005787 |
| Pounds/cu ft | Grams/cu cm | 0.01602 |
| Pounds/cu ft | Kgs/cu meter | 16.02 |
| Pounds/cu in | Pounds/mil-foot | 0.000009425 |
| Pounds/cu in | Gms/cu cm | 27.68 |
| Pounds/cu in | Pounds/cu ft | 1728 |
| Pounds/cu in | Kgs/cu meter | 27680 |

F. Relative Density (Specific Gravity) Of Various Substances

| Substance | Relative Density |
| :--- | :--- |
| Water (fresh) | 1.00 |
| Mica | 2.9 |
| Water (sea average) | 1.03 |
| Nickel | 8.6 |
| Aluminum | 2.56 |
| Oil (linseed) | 0.94 |
| Antimony | 6.70 |
| Oil (olive) | 0.92 |
| Bismuth | 9.80 |
| Oil (petroleum) | $0.76-0.86$ |
| Brass | 8.40 |
| Oil (turpentine) | 0.87 |

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| Substance | Relative Density |
| :---: | :---: |
| Brick | 2.1 |
| Paraffin | 0.86 |
| Calcium | 1.58 |
| Platinum | 21.5 |
| Carbon (diamond) | 3.4 |
| Sand (dry) | 1.42 |
| Carbon (graphite) | 2.3 |
| Silicon | 2.6 |
| Carbon (charcoal) | 1.8 |
| Silver | 10.57 |
| Chromium | 6.5 |
| Slate | 2.1-2.8 |
| Clay | 1.9 |
| Sodium | 0.97 |
| Coal | 1.36-1.4 |
| Steel (mild) | 7.87 |
| Cobalt | 8.6 |
| Sulphur | 2.07 |
| Copper | 8.77 |
| Tin | 7.3 |
| Cork | 0.24 |
| Tungsten | 19.1 |
| Glass (crown) | 2.5 |
| Wood (ash) | 0.75 |
| Glass (flint) | 3.5 |
| Wood (beech) | 0.7-0.8 |
| Gold | 19.3 |
| Wood (ebony) | 1.1-1.2 |
| Iron (cast) | 7.21 |
| Wood (elm) | 0.66 |
| Iron (wrought) | 7.78 |
| Wood (lignum-vitae) | 1.3 |
| Lead | 11.4 |
| Magnesium | 1.74 |
| Manganese | 8.0 |
| Mercury | 13.6 |
| Lead | 11.4 |
| Magnesium | 1.74 |
| Manganese | 8.0 |
| Wood (oak) | 0.7-1.0 |
| Wood (pine) | 0.56 |
| Wood (teak) | 0.8 |
| Zinc | 7.0 |
| Wood (oak) | 0.7-1.0 |
| Wood (pine) | 0.56 |
| Wood (teak) | 0.8 |
| Zinc | 7.0 |
| Mercury | 13.6 |

G. Greek Alphabet

| Name | Lower Case | Upper Case |
| :---: | :---: | :---: |
| Alpha | $\alpha$ | A |
| Beta | $\beta$ | B |
| Gamma | $\gamma$ | $\Gamma$ |
| Delta | $\delta$ | $\Delta$ |
| Epsilon | $\varepsilon$ | E |
| Zeta | $\zeta$ | Z |
| Eta | $\eta$ | H |
| Theta | $\theta$ | $\Theta$ |
| Iota | 1 | I |
| Kарра | $\kappa$ | K |
| Lambda | $\lambda$ | $\Lambda$ |
| Mu | $\mu$ | M |
| Nu | $v$ | N |
| Xi | $\xi$ | $\Xi$ |
| Omicron | o | O |
| Pi | $\pi$ | $\Pi$ |
| Rho | $\rho$ | P |
| Sigma | $\sigma$ and $\varsigma$ | $\Sigma$ |
| Tau | $\tau$ | T |
| Upsilon | $v$ | $\Upsilon$ |
| Phi | $\varphi$ | $\Phi$ |
| Chi | $\chi$ | X |
| Psi | $\psi$ | $\Psi$ |
| Omega | $\omega$ | $\Omega$ |



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## 3 System of Units

The two most commonly used systems of units are as follows:

- SI
- Imperial

SI: The International System of Units (abbreviated "SI") is a scientific method of expressing the magnitudes of physical quantities. This system was formerly called the meter-kilogram-second (MKS) system.

Imperial: A unit of measure for capacity officially adopted in the British Imperial System; British units are both dry and wet

## Metric System

|  | Exponent value | Numerical equivalent | Representation | Example |
| :--- | :--- | :--- | :--- | :--- |
| Tera | $10^{12}$ | 1000000000000 | 1000000000 | T |
| Giga | $10^{9}$ | 1000000 | G | Thz (Tera hertz) |
| Mega | $10^{6}$ | 1 | M | Mhz (Giga hertz) |
| Unit quantity | 1 | 0.001 |  | hz (hertz) <br> F (Farads) |
| Micro | $10^{-6}$ | 0.000001 | m | mF (Micro farads) |
| Nano | $10^{-9}$ | 0.000000000001 | p | nF (Nano farads) |
| Pico | $10^{-12}$ |  | pF (Pico farads) |  |

## Conversion Chart

| Multiply by | Into Milli | Into Centi | Into Deci | Into MGL* | Into Deca | Into Hecto | Into Kilo |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| To convert Kilo | $10^{6}$ | $10^{5}$ | $10^{4}$ | $10^{3}$ | $10^{2}$ | $10^{1}$ | 1 |
| To convert Hecto | $10^{5}$ | $10^{4}$ | $10^{3}$ | $10^{2}$ | $10^{1}$ | 1 | $10^{-1}$ |
| To convert Deca | $10^{4}$ | $10^{3}$ | $10^{2}$ | $10^{1}$ | 1 | $10^{-1}$ | $10^{-2}$ |
| To convert MGL* | $10^{3}$ | $10^{2}$ | $10^{1}$ | 1 | $10^{-1}$ | $10^{-2}$ | $10^{-3}$ |
| To convert Deci | $10^{2}$ | $10^{1}$ | 1 | $10^{-1}$ | $10^{-2}$ | $10^{-3}$ | $10^{-4}$ |
| To convert Centi | $10^{1}$ | 1 | $10^{-1}$ | $10^{-2}$ | $10^{-3}$ | $10^{-4}$ | $10^{-5}$ |
| To convert Milli | 1 | $10^{-1}$ | $10^{-2}$ | $10^{-3}$ | $10^{-4}$ | $10^{-5}$ | $10^{-6}$ |

## Example:

To convert Kilogram Into Milligram $\rightarrow\left(1\right.$ Kilo X $\left.10^{6}\right)$ Milligrams

## Physical constants

| Name | Symbolic Representation | Numerical Equivalent |
| :---: | :---: | :---: |
| Avogadro's number | N | $6.023 \times 10^{26} /(\mathrm{kg} \mathrm{mol})$ |
| Bohr magneton | B | $9.27 \times 10^{-24} \mathrm{Am} 25^{2}$ |
| Boltzmann's constant | k | $1.380 \times 10^{-23} \mathrm{~J} / \mathrm{k}$ |
| Stefan-Boltzmann constant | d | $5.67 \times 10^{-8} \mathrm{~W} /\left(\mathrm{m}^{2} \mathrm{~K}^{4}\right)$ |
| Characteristic impedance of free space | Zo | $\left(\mathrm{m}_{\mathrm{o}} / \mathrm{E}_{\mathrm{o}}\right)^{1 / 2}=120 \mathrm{PW}$ |
| Electron volt | eV | $1.602 \times 10^{-19} \mathrm{~J}$ |
| Electron charge | e | $1.602 \times 10^{-19} \mathrm{C}$ |
| Electronic rest mass | $\mathrm{m}_{\text {e }}$ | $9.109 \times 10^{-31} \mathrm{~kg}$ |
| Electronic charge to mass ratio | $\mathrm{e} / \mathrm{m}_{\mathrm{e}}$ | $1.759 \times 10^{11} \mathrm{C} / \mathrm{kg}$ |
| Faraday constant | F | $9.65 \times 10^{7} \mathrm{C} /(\mathrm{kg} \mathrm{mol})$ |
| Permeability of free space | $\mathrm{m}_{0}$ | $4 \mathrm{P} \times 10^{-7} \mathrm{H} / \mathrm{m}$ |
| Permittivity of free space | E | $8.85 \times 10^{-12} \mathrm{~F} / \mathrm{m}$ |
| Planck's constant | h | $6.626 \times 10^{-34} \mathrm{~J} \mathrm{~s}$ |
| Proton mass | $\mathrm{m}_{\mathrm{p}}$ | $1.672 \times 10^{-27} \mathrm{~kg}$ |
| Proton to electron mass ratio | $\mathrm{m}_{\mathrm{p}} / \mathrm{m}_{\mathrm{e}}$ | 1835.6 |
| Standard gravitational acceleration | g | $9.80665 \mathrm{~m} / \mathrm{s}^{2}, 9.80665 \mathrm{~N} / \mathrm{kg}$ |
| Universal constant of gravitation | G | $6.67 \times 10-11 \mathrm{~N} \mathrm{~m}^{2} / \mathrm{kg}^{2}$ |
| Universal gas constant | R。 | $8.314 \mathrm{~kJ} /(\mathrm{kg} \mathrm{mol} \mathrm{K})$ |
| Velocity of light in vacuum | C | $2.9979 \times 10^{8} \mathrm{~m} / \mathrm{s}$ |
| Temperature | ${ }^{\circ} \mathrm{C}$ | $5 / 9\left({ }^{\circ} \mathrm{F}-32\right)$ |
| Temperature | K | $\begin{aligned} & 5 / 9\left({ }^{\circ} \mathrm{F}+459.67\right), 5 / 9^{\circ} \mathrm{R},{ }^{\circ} \mathrm{C}+ \\ & 273.15 \end{aligned}$ |
| Speed of light in air | c | $3.00 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-1}$ |
| Electron charge | e | $-1.60 \times 10^{-19} \mathrm{C}$ |
| Mass of electron | $\mathrm{m}_{\mathrm{e}}$ | $9.11 \times 10^{-31} \mathrm{~kg}$ |
| Planck's constant | h | $6.63 \times 10^{-34} \mathrm{~J} \mathrm{~s}$ |


| Name | Symbolic Representation | Numerical Equivalent |
| :--- | :--- | :--- |
| Universal gravitational constant | G | $6.67 \times 10^{-11} \mathrm{~N} \mathrm{~m}^{2} \mathrm{~kg}^{-2}$ |
| Electron volt | 1 eV | $1.60 \times 10^{-19} \mathrm{~J}$ |
| Mass of proton | $\mathrm{m}_{\mathrm{p}}$ | $1.67 \times 10^{-27} \mathrm{~kg}$ |
| Acceleration due to gravity on Earth | g | $9.80 \mathrm{~m} \mathrm{~s}^{-2}$ |
| Acceleration due to gravity on the Moon | $\mathrm{g}_{\mathrm{M}}$ | $1.62 \mathrm{~m} \mathrm{~s}^{-2}$ |
| Radius of the Earth | $\mathrm{R}_{\mathrm{E}}$ | $6.37 \times 10^{6} \mathrm{~m}$ |
| Mass of the Earth | $\mathrm{M}_{\mathrm{E}}$ | $5.98 \times 10^{24} \mathrm{~kg}$ |
| Radius of the Sun | $\mathrm{R}_{\mathrm{S}}$ | $6.96 \times 10^{8} \mathrm{~m}$ |
| Mass of the Sun | $\mathrm{M}_{\mathrm{S}}$ | $1.99 \times 10^{30} \mathrm{~kg}$ |
| Radius of the Moon | $\mathrm{R}_{\mathrm{M}}$ | $1.74 \times 10^{6} \mathrm{~m}$ |
| Mass of the Moon | $\mathrm{M}_{\mathrm{M}}$ | $7.35 \times 10^{22} \mathrm{~kg}$ |
| Earth-Moon distance | - | $3.84 \times 10^{8} \mathrm{~m}$ |
| Earth-Sun distance | - | $1.50 \times 10^{11} \mathrm{~m}$ |
| Speed of light in air | $\mathrm{c}^{2}$ | $3.00 \times 10^{8} \mathrm{~m} \mathrm{~s}$ |

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| Name | Symbolic Representation | Numerical Equivalent |
| :--- | :--- | :--- |
| Electron charge | e | $-1.60 \times 10^{-19} \mathrm{C}$ |
| Mass of electron | $\mathrm{m}_{\mathrm{e}}$ | $9.11 \times 10^{-31} \mathrm{~kg}$ |
| Planck's constant | h | $6.63 \times 10^{-34} \mathrm{~J} \mathrm{~s}$ |
| Universal gravitational constant | G | $6.67 \times 10^{-11} \mathrm{~N} \mathrm{~m}^{2} \mathrm{~kg}^{-2}$ |
| Electron volt | 1 eV | $1.60 \times 10^{-19} \mathrm{~J}$ |
| Mass of proton | $\mathrm{m}_{\mathrm{p}}$ | $1.67 \times 10^{-27} \mathrm{~kg}$ |
| Acceleration due to gravity on Earth | g | $9.80 \mathrm{~m} \mathrm{~s}^{-2}$ |
| Acceleration due to gravity on the Moon | $\mathrm{g}_{\mathrm{M}}$ | $1.62 \mathrm{~m} \mathrm{~s}^{-2}$ |
| Ton | 1 ton | $1.00 \times 10^{3} \mathrm{~kg}$ |

## 4 General Mathematical Formulae

### 4.1 Algebra

A. Expansion Formulae

Square of summation

- $(x+y)^{2}=x^{2}+2 x y+y^{2}$


## Square of difference

- $(x-y)^{2}=x^{2}-2 x y+y^{2}$

Difference of squares

- $x^{2}-y^{2}=(x+y)(x-y)$


## Cube of summation

- $(x+y)^{3}=x^{3}+3 x^{2} y+3 x y^{2}+y^{3}$

Summation of two cubes

- $x^{3}+y^{3}=(x+y)\left(x^{2}-x y+y^{2}\right)$

Cube of difference

- $(x-y)^{3}=x^{3}-3 x^{2} y+3 x y^{2}-y^{3}$

Difference of two cubes

- $x^{3}-y^{3}=(x-y)\left(x^{2}+x y+y^{2}\right)$


## B. Quadratic Equation

- If $a x^{2}+b x+c=0$,

Then $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

The basic algebraic properties of real numbers $\mathrm{a}, \mathrm{b}$ and c are:

| Property | Description |
| :--- | :--- |
| Closure | $\mathrm{a}+\mathrm{b}$ and ab are real numbers |
| Commutative | $\mathrm{a}+\mathrm{b}=\mathrm{b}+\mathrm{a}, \mathrm{ab}=\mathrm{ba}$ |
| Associative | $(a+b)+c=a+(b+c),(a b) c=a(b c)$ |
| Distributive | $(\mathrm{a}+\mathrm{b}) \mathrm{c}=\mathrm{ac}+\mathrm{bc}$ |
| Identity | $\mathrm{a}+0=0+\mathrm{a}=\mathrm{a}$ |
| Inverse | $\mathrm{a}+(-\mathrm{a})=0, \mathrm{a}(1 / \mathrm{a})=1$ |
| Cancellation | If $\mathrm{a}+\mathrm{x}=\mathrm{a}+\mathrm{y}$, then $\mathrm{x}=\mathrm{y}$ |
| Zero-factor | $\mathrm{a} 0=0 \mathrm{a}=0$ |
| Negation | $-(-\mathrm{a})=\mathrm{a},(-\mathrm{a}) \mathrm{b}=\mathrm{a}(-\mathrm{b})=-(\mathrm{ab}),(-\mathrm{a})(-\mathrm{b})=\mathrm{ab}$ |

Algebraic Combinations
Factors with a common denominator can be expanded:

$$
\frac{a+b}{c}=\frac{a}{c}+\frac{b}{c}
$$

Fractions can be added by finding a common denominator:
$\frac{a}{c}+\frac{b}{d}=\frac{a d+b c}{c d}$


Products of fractions can be carried out directly:
$\frac{a}{c} \times \frac{b}{d}=\frac{a b}{c d}$
Quotients of fractions can be evaluated by inverting and multiplying:

$$
\frac{a / b}{c / d}=\frac{a}{b} \times \frac{d}{c}=\frac{a d}{b c}
$$

## Radical Combinations

$$
\begin{aligned}
& \sqrt[n]{a b}=\sqrt[n]{a} \sqrt[n]{b} \\
& \sqrt[n]{a}=a^{1 / n} \\
& \sqrt[n]{\frac{a}{b}}=\frac{\sqrt[n]{a}}{\sqrt[n]{b}} \\
& \sqrt[n]{a^{m}}=a^{\frac{m}{n}} \\
& \sqrt[n]{\sqrt[m]{a}}=\sqrt[m n]{a}
\end{aligned}
$$

### 4.2 Geometry

| Item | Circumference / <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| Square | 4 s |  | NA |  |  |


| Item | Circumference <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rectangle | 2(L + B) |  |  |  |  |


| Item | Circumference / <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Equilateral triangle | 3s <br> where $s$ is the length of each side | $A=\frac{1}{2} b h$ | NA | NA |  |
| Trapezoid | $a+b+h\left(\frac{1}{\sin \theta}+\frac{1}{\sin \phi}\right)$ <br> where $\theta$ and $\Phi$ are the 2 base angles | $A=\left(\frac{a+b}{2}\right) h$ | NA | NA |  |

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| Item | Circumference / <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Circle | $\begin{aligned} & \mathrm{C}=2 \mathrm{pr} \\ & \mathrm{C}=\mathrm{pd} \end{aligned}$ | $\mathrm{A}=\mathrm{pr}^{2}$ | NA | NA |  |
| Circle <br> Sector | $2 \mathrm{r}+($ arc length $)$ | $\begin{gathered} A=\frac{\operatorname{arc} \times r}{2} \\ A=\frac{\theta^{\circ}}{360} \times \pi r^{2} \\ A=\frac{\theta^{\circ} r^{2}}{2} \end{gathered}$ | NA | NA |  |
| Ellipse | $(1 / 4) \cdot D \cdot d \cdot \Pi$ <br> where D and d are the two axis | $A=\frac{\pi}{4} D d$ <br> D is the larger radius and d is the smaller radius | NA | NA |  |
| Trapezoid | Sum of all sides | $A=\frac{1}{2}\left(b_{1}+b_{2}\right) h$ | NA | NA |  |



| Item | Circumference / <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Sphere | NA | NA | $S=4 \pi r^{2}$ | $\frac{4}{3} \pi r^{3}$ |  |
| Pyramid | NA | NA | $1 / 2$.perimeter. <br> slant height $+\mathrm{B}$ | $\begin{gathered} \frac{1}{3} \text { base area. } \\ \text { perpendicular } \\ \text { height } \end{gathered}$ |  |

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| Item | Circumference / <br> Perimeter | Area | Surface Area | Volume | Figure |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rectangular <br> prism | NA |  |  |  |  |
| Cone |  | NA | $2 l \mathrm{~h}+21 \mathrm{w}+2 \mathrm{wh}$ | $\mathrm{V}=1 \mathrm{wh}$ |  |

### 4.3 Trigonometry

## A. Pythagoras' Law

$$
c^{2}=a^{2}+b^{2}
$$

## B. Basic Ratios

- $\operatorname{Sin} \theta=\mathrm{a} / \mathrm{c}$
- $\operatorname{Cos} \theta=b / c$

b
- $\operatorname{Tan} \theta=\mathrm{a} / \mathrm{b}$
- $\operatorname{Cosec} \theta=c / a$
- $\operatorname{Sec} \theta=c / b$
- $\operatorname{Cot} \theta=\mathrm{b} / \mathrm{a}$


## Degrees versus Radians

- A circle in degree contains 360 degrees
- A circle in radians contains $2 \pi$ radians


Sine, Cosine and Tangent

$$
\sin \theta=\frac{\text { opposite }}{\text { hypotenus }} \quad \cos \theta=\frac{\text { adjacent }}{\text { hypotenus }} \quad \tan \theta=\frac{\text { opposite }}{\text { adjacent }}
$$

Sine, Cosine and the Pythagorean Triangle

$$
[\sin \theta]^{2}+[\cos \theta]^{2}=\sin ^{2} \theta+\cos ^{2} \theta=1
$$

Tangent, Secant and Co-Secant

$$
\begin{aligned}
& \tan \theta=\frac{\sin \theta}{\cos \theta} \\
& \sec \theta=\frac{1}{\cos \theta} \\
& \csc \theta=\frac{1}{\sin \theta}
\end{aligned}
$$

C. Trigonometric Function Values

Euler's Representation

$$
\begin{aligned}
& e^{j \theta}=\cos (\theta)+j \sin (\theta) \\
& e^{-j \theta}=\cos (\theta)-j \sin (\theta)
\end{aligned}
$$

$$
\begin{aligned}
& e^{j n \theta}=\cos (n \theta)+j \sin (n \theta) \\
& \cos \theta=\frac{e^{j \theta}+e^{-j \theta}}{2} \\
& \sin \theta=\frac{e^{j \theta}-e^{-j \theta}}{2 j} \\
& \text { 4.4 Logarithm }
\end{aligned}
$$

## Definition

The logarithm of a number to a particular base is the power (or index) to which that base must be raised to obtain the number.

The number 8 written in index form as $\mathbf{8}=\mathbf{2}^{\mathbf{3}}$

The equation can be rewritten in logarithm form as $\boldsymbol{\operatorname { l o g }}_{2} \mathbf{8}=\mathbf{3}$

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## Logarithm laws

The logarithm laws are obtained from the index laws and are:

- $\log _{a} x+\log _{a} y=\log _{a} x y$
- $\log _{a} x-\log _{a} y=\log _{a}(x / y)$
- $\log _{a} x y=y \log _{a} x$
- $\log _{a}(1 / x)=-\log _{a} x$
- $\log _{\mathrm{a}} 1=0$
- $\log _{\mathrm{a}} \mathrm{a}=1$
- $a^{\left(\log _{a} x\right)}=x$

Note: It is not possible to have the logarithm of a negative number. All logarithms must have the same base.

## Euler Relationship

The trigonometric functions are related to a complex exponential by the Euler relationship:
$e^{j x}=\cos x+j \sin x$
$e^{-j x}=\cos x-j \sin x$

From these relationships the trig functions can be expressed in terms of the complex exponential:

$$
\begin{aligned}
& \cos x=\frac{e^{j x}+e^{-j x}}{2} \\
& \sin x=\frac{e^{j x}-e^{-j x}}{2}
\end{aligned}
$$

## Hyperbolic Functions

The hyperbolic functions can be defined in terms of exponentials.

Hyperbolic sine $=\sinh \mathrm{x}=\frac{\frac{e^{x}-e^{-x}}{2}}{2}$

Hyperbolic cosine $=\cosh \mathrm{x}=\frac{\frac{e^{x}+e^{-x}}{2}}{2}$

Hyperbolic tangent $=\tanh \mathrm{x}=\frac{\sinh x}{\cosh x}=\frac{e^{x}-e^{-x}}{e^{x}+e^{x}}$

### 4.5 Exponents

## Summary of the Laws of Exponents

Let $c, d, r$, and $s$ be any real numbers.

| $c^{r} \cdot c^{s}=c^{r+s}$ | $(c \cdot d)^{r}=c^{r} \cdot d^{r}$ |
| :---: | :---: |
| $\frac{c^{r}}{c^{s}}=c^{r-s}, c \neq 0$ | $\left(\frac{c}{d}\right)^{r}=\frac{c^{r}}{d^{r}}, d \neq 0$ |
| $\left(c^{r}\right)^{s}=c^{r \cdot s}$ | $c^{-r}=\frac{1}{c^{r}}$ |

## Basic Combinations

Since the raising of a number $n$ to a power $p$ may be defined as multiplying $n$ times itself $p$ times, it follows that $n^{p_{1}+p_{2}}=n^{p_{1}} n^{p_{2}}$

The rule for raising a power to a power can also be deduced
$\left(n^{a}\right)^{b}=n^{a b}$
$(a b)^{n}=a^{n} b^{n}$
$\mathrm{a}^{\mathrm{m} / \mathrm{a}^{\mathrm{n}}}=\mathrm{a}^{\mathrm{m}-\mathrm{n}}$
where a not equal to zero

### 4.6 Complex Numbers

A complex number is a number with a real and an imaginary part, usually expressed in Cartesian form
$a+j b$ where $\mathbf{j}=\sqrt{ }-1$ and $\mathbf{j} \cdot \mathbf{j}=-\mathbf{1}$

Complex numbers can also be expressed in polar form
$\mathrm{Ae}^{\mathrm{j} \theta}$ where $\mathrm{A}=\sqrt{ } \mathrm{a}^{2}+\mathbf{b}^{2}$ and $\theta=\boldsymbol{\operatorname { t a n }}^{-1}(\mathbf{b} / \mathbf{a})$

The polar form can also be expressed in terms of trigonometric functions using the Euler relationship $\mathrm{e}^{\mathrm{j} \theta}=\cos \theta+\mathrm{j} \sin \theta$

## Euler Relationship

The trigonometric functions are related to a complex exponential by the Euler relationship

$$
e^{j x}=\cos x+j \sin x
$$

$e^{-j \theta}=\cos x-j \sin x$

From these relationships the trigonometric functions can be expressed in terms of the complex exponential:

$$
\begin{aligned}
& \cos x=\frac{e^{j x}+e^{-j x}}{2} \\
& \sin x=\frac{e^{j x}-e^{-j x}}{2}
\end{aligned}
$$

This relationship is useful for expressing complex numbers in polar form, as well as many other applications.

## Polar Form, Complex Numbers

The standard form of a complex number is
$a+j b$ where $j=\sqrt{ }-1$


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But this can be shown to be equivalent to the form
$A e^{i \theta}$ where $A=\sqrt{ } \mathbf{a}^{2}+b^{2}$ and $\theta=\tan ^{-1}(b / a)$
which is called the polar form of a complex number. The equivalence can be shown by using the Euler relationship for complex exponentials.

$$
\begin{aligned}
& A e^{j \theta}=\sqrt{a^{2}+b^{2}}\left(\cos \left[\tan ^{-1} \frac{b}{a}\right]+j \sin \left[\tan ^{-1} \frac{b}{a}\right]\right) \\
& A e^{j \theta}=\sqrt{a^{2}+b^{2}}\left(\frac{a}{\sqrt{a^{2}+b^{2}}}+j \frac{b}{\sqrt{a^{2}+b^{2}}}\right)=a+j b
\end{aligned}
$$

## 5 Engineering Concepts and Formulae

### 5.1 Electricity

Ohm's Law
$I=\frac{V}{R}$

Or
$V=I R$

Where
$\mathrm{I}=$ current (amperes)
$\mathrm{E}=$ electromotive force (volts)
$\mathrm{R}=$ resistance (ohms)

## Temperature correction

$R_{t}=R o(1+\alpha t)$

Where

Ro $=$ resistance at $0^{\circ} \mathrm{C}($.
$\mathrm{R}_{\mathrm{t}}=$ resistance at $\mathrm{t}^{\circ} \mathrm{C}$ (.)
$\alpha=$ temperature coefficient which has an average value for copper of $0.00428\left(\Omega / \Omega^{\circ} \mathrm{C}\right)$
$R_{2}=R_{1} \frac{\left(1+\alpha t_{2}\right)}{\left(1+\alpha t_{1}\right)}$

Where $\mathrm{R}_{1}=$ resistance at $\mathrm{t}_{1}$
$\mathrm{R}_{2}=$ resistance at $\mathrm{t}_{2}$

| Values of alpha | $\mathbf{\Omega} / \mathbf{\Omega}^{\circ} \mathbf{C}$ |
| :--- | :--- |
| Copper | 0.00428 |
| Platinum | 0.00358 |
| Nickel | 0.00672 |
| Tungsten | 0.00450 |
| Aluminum | 0.0040 |

Current, $I=\frac{n q v t A}{t}=n q v A$

## Conductor Resistivity

$$
R=\frac{\rho L}{a}
$$

Where

$$
\begin{aligned}
& \rho=\text { specific resistance (or resistivity) (ohm meters, } \Omega \mathrm{m} \text { ) } \\
& \mathrm{L}=\text { length (meters) } \\
& \mathrm{a}=\text { area of cross-section (square meters) }
\end{aligned}
$$

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| Quantity | Equation |
| :--- | :--- |
| Resistance R of a uniform conductor | $R=\rho \frac{L}{A}$ |
| Resistors in series, $R_{s}$ | $R_{s}=\mathrm{R}_{1}+\mathrm{R}_{2}+\mathrm{R}_{3}$ |
|  | $\frac{1}{R_{p}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}$ |
| Resistors in parallel, $R_{p}$ | $P=V=I^{2} R=\frac{V^{2}}{R}$ |
| Power dissipated in resistor: | $\mathrm{V}=\mathrm{I} \mathrm{R}$ |
| Potential drop across R |  |

## Dynamo Formulae

Average e.m.f. generated in each conductor $=\frac{2 \varphi N p Z}{60 c}$
Where
$\mathrm{Z}=$ total number of armature conductors
$c=$ number of parallel paths through winding between positive and negative brushes
Where $\mathrm{c}=2$ (wave winding), $\mathrm{c}=2 \mathrm{p}$ (lap winding)
$\Phi=$ useful flux per pole (webers), entering or leaving the armature
$\mathrm{p}=$ number of pairs of poles
$\mathrm{N}=$ speed (revolutions per minute)

Generator Terminal volts $=$ EG - IaRa
Motor Terminal volts $=\mathrm{EB}+\mathrm{IaRa}$
Where $E G=$ generated e.m.f.
$E B=$ generated back e.m.f.
Ia $=$ armature current
$\mathrm{Ra}=$ armature resistance

## Alternating Current

RMS value of sine curve $=0.707$ of maximum value
Mean Value of Sine wave $=0.637$ of maximum value
Form factor $=$ RMS value $/$ Mean Value $=1.11$
Frequency of Alternator $=\frac{p N}{60}$ cycles per second
Where $p$ is number of pairs of poles
N is the rotational speed in $\mathrm{r} / \mathrm{min}$

## Slip of Induction Motor

[(Slip speed of the field - Speed of the rotor) / Speed of the Field] $\times 100$

Inductors and Inductive Reactance

| Physical Quantity | Equation |
| :---: | :---: |
| Inductors and Inductance | $\mathrm{V}_{\mathrm{L}}=\mathrm{L} \frac{\mathrm{di}}{\mathrm{dt}}$ |
| Inductors in Series: | $\mathrm{L}_{\mathrm{T}}=\mathrm{L}_{1}+\mathrm{L}_{2}+\mathrm{L}_{3}+\ldots$. |
| Inductor in Parallel: | $\frac{1}{\mathrm{~L}_{\mathrm{T}}}=\frac{1}{\mathrm{~L}_{1}}+\frac{1}{\mathrm{~L}_{2}}+\frac{1}{\mathrm{~L}_{3}}+\ldots .$ |
| Current build up <br> (switch initially closed after having been opened) | $\begin{aligned} & \text { At } v_{L}(t)=E e^{-\frac{t}{\tau}} \\ & v_{R}(t)=E\left(1-e^{-\frac{t}{\tau}}\right) \\ & i(t)=\frac{E}{R}\left(1-e^{-\frac{t}{\tau}}\right) \\ & \tau=\frac{L}{R} \end{aligned}$ |
| Current decay <br> (switch moved to a new position) | $\begin{aligned} & i(t)=I_{o} e^{-\frac{t}{\tau^{\prime}}} \\ & \mathrm{V}_{\mathrm{R}}(\mathrm{t})=\mathrm{Ri}(\mathrm{t}) \\ & \mathrm{V}_{\mathrm{L}}(\mathrm{t})=-\mathrm{R}_{\mathrm{T}} \mathrm{i}(\mathrm{t}) \\ & \tau^{\prime}=\frac{\mathrm{L}}{\mathrm{R}_{\mathrm{T}}} \end{aligned}$ |
| Alternating Current | $\begin{aligned} & f=1 / T \\ & \omega=2 \pi f \end{aligned}$ |
| Complex Numbers: | $\begin{aligned} & C=a+j b \\ & C=M \cos \theta+j M \sin \theta \\ & M=\sqrt{a^{2}+b^{2}} \\ & \theta=\tan ^{-1}\left(\frac{b}{a}\right) \end{aligned}$ |
| Polar form: | $C=M \angle \theta$ |
| Inductive Reactance | $\left\|X_{L}\right\|=\omega L$ |
| Capacitive Reactance | $\left\|X_{C}\right\|=1 /(\omega \mathrm{C})$ ) |
| Resistance | R |


| Physical Quantity | Equation |
| :--- | :--- |
|  |  |
|  | Resistance: $Z_{R}=R \angle 0^{\circ}$ <br> Impedance <br> Inductance: $Z_{L}=X_{L} \angle 90^{\circ}=\omega \mathrm{L} \angle 90^{\circ}$ <br>  <br>  <br>  <br>  <br>  <br> $\angle-90^{\circ}$ <br>  |


| Quantity | Equation |
| :--- | :--- |
| Ohm's Law for AC | $\mathrm{V}=\mathrm{I} \mathrm{Z}$ |
| Time Domain | $\mathrm{V}(\mathrm{t})=\mathrm{V}_{\mathrm{m}} \sin (\omega \mathrm{t} \pm \phi)$ <br> $\mathrm{i}(\mathrm{t})=\mathrm{I}_{\mathrm{m}} \sin (\omega \mathrm{t} \pm \phi)$ |
| Phasor Notation | $\mathrm{V}=\mathrm{V}_{\mathrm{rms}} \angle \phi$ <br> $\mathrm{V}=\mathrm{V}_{\mathrm{m}} \angle \phi$ |
| Components in Series | $\mathrm{Z}_{\mathrm{T}}=\mathrm{Z}_{1}+\mathrm{Z}_{2}+\mathrm{Z}_{3}+\ldots$ |
| Voltage Divider Rule | $\mathrm{V}_{\mathrm{x}}=\mathrm{V}_{\mathrm{T}} \frac{\mathrm{Z}_{\mathrm{x}}}{\mathrm{Z}_{\mathrm{T}}}$ |

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| Quantity | Equation |
| :--- | :--- |
| Components in Parallel | $\frac{1}{\mathrm{Z}_{\mathrm{T}}}=\frac{1}{\mathrm{Z}_{1}}+\frac{1}{\mathrm{Z}_{2}}+\frac{1}{\mathrm{Z}_{3}}+\ldots$ |
| Current Divider Rule | $\mathrm{I}_{\mathrm{x}}=\mathrm{I}_{\mathrm{T}} \frac{\mathrm{Z}_{\mathrm{T}}}{\mathrm{Z}_{\mathrm{x}}}$ |
| Two impedance values in parallel | $\mathrm{Z}_{\mathrm{T}}=\frac{Z_{1} Z_{2}}{Z_{1}+Z_{2}}$ |

## Capacitance

| Capacitors | $\mathrm{C}=\frac{\mathrm{Q}}{\mathrm{~V}}[\mathrm{~F}] \text { (Farads) }$ |
| :---: | :---: |
| Capacitor in Series | $\frac{1}{\mathrm{C}_{\mathrm{T}}}=\frac{1}{\mathrm{C}_{1}}+\frac{1}{\mathrm{C}_{2}}+\frac{1}{\mathrm{C}_{3}}+\ldots$. |
| Capacitors in Parallel | $\mathrm{C}_{\mathrm{T}}=\mathrm{C}_{1}+\mathrm{C}_{2}+\mathrm{C}_{3}+\ldots \ldots$ |
| Charging a Capacitor | $\begin{aligned} & i(t)=\frac{E}{R} e^{-\frac{t}{R C}} \\ & v_{R}(t)=E e^{-\frac{t}{R C}} \\ & v_{C}(t)=E\left(1-e^{-\frac{t}{R C}}\right) \\ & \tau=R C \end{aligned}$ |
| Discharging a Capacitor | $\begin{aligned} & i(t)=-\frac{V_{o}}{R} e^{-\frac{t}{\tau^{\prime}}} \\ & \mathrm{V}_{\mathrm{R}}(\mathrm{t})=-\mathrm{V}_{\mathrm{o}} \mathrm{e}^{-\frac{\mathrm{t}}{\tau^{\prime}}} \\ & \mathrm{V}_{\mathrm{C}}(\mathrm{t})=\mathrm{V}_{\mathrm{o}} \mathrm{e}^{-\frac{\mathrm{t}}{\tau^{\prime}}} \\ & \tau^{\prime}=\mathrm{R}_{\mathrm{T}} \mathrm{C} \end{aligned}$ |


| Quantity | Equation |
| :--- | :--- |
| Capacitance | $C=\frac{Q}{V}$ |
| Capacitance of a Parallel-plate <br> Capacitor | $C=\frac{\varepsilon A}{d}$ |


| Quantity | Equation |
| :--- | :--- |
| Isolated Sphere | $\mathrm{C}=4 \pi \varepsilon \mathrm{r}$ |
| Capacitors in parallel | $\mathrm{C}=\mathrm{C}_{1}+\mathrm{C}_{2}+\mathrm{C}_{3}$ |
| Capacitors in series | $\frac{1}{C}=\frac{1}{C_{1}}+\frac{1}{C_{2}}+\frac{1}{C_{3}}$ |
| Energy stored in a charged capacitor | $W=\frac{Q^{2}}{2 C}=\frac{1}{2} C V^{2}=\frac{1}{2} Q V$ |
| If the capacitor is isolated | $W=\frac{Q^{2}}{2 C}$ |
| If the capacitor is connected to a |  |
| battery | $W=\frac{1}{2} C V^{2}$ |
| For R C circuits | $Q=Q_{o}\left(1-e^{-t / R C}\right) ;$ <br> $V=V_{o}$ <br> $\left(1-e^{-t / R C}\right)$ |
| Charging a capacitor | $Q=Q_{o} e^{-t / R C}$ <br> $V=V_{o} e^{-t / R C}$ |
| Discharging a capacitor |  |

- If the capacitor is isolated, the presence of the dielectric decreases the potential difference between the plates
- If the capacitor is connected to a battery, the presence of the dielectric increases the charge stored in the capacitor.
- The introduction of the dielectric increases the capacitance of the capacitor


## Current in AC Circuit

## RMS Current

| In Cartesian <br> form | $I=\frac{V}{\left[R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}\right]^{2}} \cdot\left[R-j\left(\omega L-\frac{1}{\omega C}\right)\right]$ |
| :--- | :--- |
|  | $I=\frac{V}{\sqrt{\left[R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}\right]}} \angle-\phi_{s}$ |
| In polar form $\quad$ Amperes |  |
|  | $\phi_{s}=\tan ^{-1}\left[\frac{\omega L-\frac{1}{\omega C}}{R}\right]$ |
| where |  |


| Modulus | $\|I\|={\frac{V}{\sqrt{R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}}}}_{\text {Amperes }}$ |
| :--- | :--- |

## Complex Impedance

| In Cartesian form | $Z=R+j\left(\omega L-\frac{1}{\omega C}\right)_{\text {Ohms }}$ |
| :--- | :--- |
| In polar form | $Z=\sqrt{R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}} \angle \phi_{s}$ |
| Ohms |  |
|  | $\phi_{s}=\tan ^{-1}\left[\frac{\omega L \frac{-}{\omega C}}{R}\right]$ |
| Modulus | $\left.\|Z\|=\sqrt{\left[R^{2}+\left(\omega L-\frac{1}{\omega C}\right)^{2}\right.}\right]$ Ohms |

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## Power dissipation

| Average power, | $P=V I \cos \phi$ Watts |
| :--- | :--- |
| Power dissipation in a resistor | $P=\|I\|^{2} R$ Watts |

## Rectification

| Controlled half wave rectifier | Average DC voltage $=\frac{V_{m}}{2 \pi}(1+\cos \alpha)$ Volts |
| :--- | :--- |
| Controlled full wave rectifier | Average DC voltage $=\frac{V_{m}}{\pi}(1+\cos \alpha)$ Volts |

## Power Factor

| DC Power | $P_{d c}=V I=I^{2} R=\frac{V^{2}}{R}$ |
| :--- | :--- |
| AC Power | $P a c=\operatorname{Re}(V . I)=V \cos \phi$ |

## Power in ac circuits

| Quantity | Equation |
| :---: | :---: |
| Resistance | The mean power $=\bar{P}=\mathrm{I}_{\mathrm{rms}} \mathrm{V}_{\mathrm{rms}}=\mathrm{I}_{\mathrm{rms}}{ }^{2} \mathrm{R}$ |
| Inductance | The instantaneous power $=(\mathrm{Io} \sin \mathrm{wt})(\mathrm{Vosin}(\mathrm{wt}+\pi)$ |
| The mean power | $\bar{P}=0$ |
| Capacitance | The instantaneous power $=(\mathrm{Io} \sin (\mathrm{wt}+\pi / 2))\left(\mathrm{V}_{\mathrm{o}} \sin \right.$ wt) |
| The mean power | $\bar{P}=0$ |
| Formula for a.c. power | The mean power $=\bar{P}=I_{\text {rms }} \mathrm{V}_{\mathrm{rms}} \cos \phi$ |

## Three Phase Alternators

Star connected

$$
\begin{aligned}
& \text { Line voltage }=\sqrt{3} \bullet \text { Phase Voltage } \\
& \text { Line current }=\text { phase current }
\end{aligned}
$$

Delta connected

Line voltage $=$ phase voltage
Line current $=\sqrt{3} \bullet$ Phase Current

Three phase power

$$
\mathrm{P}=\sqrt{3} \bullet E_{L} \bullet I_{L} \bullet \operatorname{Cos} \phi
$$

Where:
$P$ is the active power in Watts
$\mathrm{E}_{\mathrm{L}}$ is the Line Voltage in Volts
$\mathrm{I}_{\mathrm{L}}$ is the line current in Amperes
Cos $f$ is the power factor

## Electrostatics

| Quantity | Equation |
| :--- | :--- |
| Instantaneous current, | $I=\frac{d q}{d t}=C \frac{d v}{d t} \quad$ Amperes |
| Permittivity of free space | $\varepsilon_{0}=\frac{10^{-9}}{36 \pi}=8.85 \times 10^{-12} \quad$ Farads (meters) ${ }^{-1}$ |
| Energy stored in a capacitor | $=\frac{1}{2} C V^{2} \quad$ Joules |


| Quantity | Equation |
| :--- | :--- |
| Coulomb's law | $F=k \frac{Q_{1} Q_{2}}{r^{2}}$ |
| Electric fields | $E=\frac{F}{q}$ |
| Due to a point charge | $E=\frac{Q}{4 \pi \varepsilon_{o} r^{2}}$ |
| Due to a conducting sphere carrying charge Q Inside the sphere | $\mathrm{E}=0$ |
| Outside the sphere | $E=\frac{Q}{4 \pi \varepsilon_{o} r^{2}}$ |
| Just outside a uniformly charged conducting sphere or plate | $E=\frac{\sigma}{\varepsilon_{o}}$ |

- An electric field E is a vector
- The electric field strength is directly proportional to the number of electric field lines per unit cross-sectional area,
- The electric field at the surface of a conductor is perpendicular to the surface.
- The electric field is zero inside a conductor.

| Quantity | Equation |
| :---: | :---: |
| Suppose a point charge Q is at A . The work done in bringing a charge q from infinity to some point a distance r from A is | $W=\frac{Q q}{4 \pi \varepsilon_{o} r}$ |
| Electric potential | $V=\frac{W}{q}$ |
| Due to a point charge | $V=\frac{Q}{4 \pi \varepsilon_{o} r}$ |
| Due to a conducting sphere, of radius a , carrying charge Q : <br> Inside the sphere | $V=\frac{Q}{4 \pi \varepsilon_{o} a}$ |
| Outside the sphere | $V=\frac{Q}{4 \pi \varepsilon_{o} r}$ |
| If the potential at a point is $V$, then the potential energy of a charge q at that point is | $\mathrm{U}=\mathrm{qV}$ |
| Work done in bringing charge $q$ from $A$ of potential $V_{A}$ to point $B$ of potential $V_{B}$ | $\mathrm{W}=\mathrm{q}\left(\mathrm{V}_{\mathrm{B}}-\mathrm{V}_{\mathrm{A}}\right)$ |



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| Quantity | Equation |
| :--- | :--- |
| Relation between E and V | $E=-\frac{d V}{d x}$ |
| For uniform electric field | $E=\frac{V}{d}$ |

## Magnetostatics

| Physical Quantity | Equation |
| :--- | :--- |
| Magnetic flux density (also called the B-field) is defined as the <br> force acting per unit current length. | $B=\frac{F}{I \ell}$ |
| Force on a current-carrying conductor in a magnetic field | $\mathrm{F}=\mathrm{I} \ell \mathrm{B} \vec{F}=\mathrm{I} \vec{\ell} \cdot \vec{B}$ <br> And Magnitude of <br> $\vec{F}=\mathrm{F}=\mathrm{I} \ell \mathrm{B}$ <br> $\sin \theta$ |
| Force on a moving charged particle in a magnetic field | $\mathrm{F}=\mathrm{q} \vec{v} \cdot \vec{B}$ |
| Circulating Charges | $q v B=\frac{m v^{2}}{r}$ |

## Calculation of magnetic flux density

| Physical Quantity | Equation |
| :---: | :---: |
| Magnetic fields around a long straight wire carrying current I | $B=\frac{\mu_{o} I}{2 \pi a}$ <br> where $\mathrm{a}=$ perp. distance from a very long straight wire |
| Magnetic fields inside a long solenoid, carrying current | $\mathrm{I}: \mathrm{B}=\mu_{\mathrm{o}} \mathrm{n}$, where $\mathrm{n}=$ number of turns per unit length. |
| Hall effect <br> At equilibrium | $\begin{aligned} & Q \frac{V_{H}}{d}=Q v B \\ & \mathrm{~V}_{\mathrm{H}}=\mathrm{B} \mathrm{v} \mathrm{~d} \end{aligned}$ |
| The current in a material is given by | $\mathrm{I}=\mathrm{nQAv}$ |
| The forces between two current-carrying conductors | $F_{2}=\frac{\mu_{o} I_{1} I_{2} \ell}{2 \pi a}$ |


| Physical Quantity | Equation |
| :---: | :---: |
| The torque on a rectangular coil in a magnetic field | $\begin{aligned} & \mathrm{T}=\mathrm{Fb} \sin \theta \\ & =\mathrm{N} \text { I } \ell \mathrm{Bb} \sin \theta \\ & =\mathrm{N} \text { I A B } \sin \theta \end{aligned}$ |
| If the coil is in a radial field and the plane of the coil is always parallel to the field, then | $\begin{aligned} & \mathrm{T}=\mathrm{N} \text { I A B } \sin \theta \\ & =\text { N I A B } \sin 90^{\circ} \\ & =\text { N I A B } \end{aligned}$ |
| Magnetic flux f | $\phi=\mathrm{B} \mathrm{~A} \cos \theta$ <br> and $\text { Flux-linkage }=N \phi$ |
| Current Sensitivity | $S_{I}=\frac{\theta}{I}=\frac{N A B}{c}$ |

## Lenz's law

The direction of the induced e.m.f. is such that it tends to oppose the flux-change causing it, $\varepsilon=-N \frac{d}{d t} \phi$ and does oppose it if induced current flows.

## EMF Equations

| E.m.f. induced in a straight conductor | $\varepsilon=$ B L v |
| :--- | :--- |
| E.m.f. induced between the center and the rim of a spinning disc | $\varepsilon=\mathrm{B} \pi \mathrm{r}^{2} \mathrm{f}$ |
| E.m.f. induced in a rotating coil | $\mathrm{E}=\mathrm{N}$ A B w sin wt |


| Quantity | Equation |
| :--- | :--- |
| Self-induction | $L=-\frac{\varepsilon}{d I / d t}$ |
| Energy stored in an inductor: | N <br> Transformers: <br> The L R (d.c.) circuit: |
|  | $U=\frac{1}{2} L I^{2}$ |
|  | $I=\frac{E}{R}\left(1-e^{-R t / L}\right)$ |

## Quantity $\quad$ Equation

When a great load (or smaller resistance) is connected to the secondary coil, the flux in the core decreases. The e.m.f., $\varepsilon_{\text {p }}$, in the $\mathrm{V}_{\mathrm{p}}-\varepsilon_{\mathrm{p}=\mathrm{IR} ;} I=\frac{V_{P}-\varepsilon_{p}}{R}$ primary coil falls.

## Kirchoff's laws

## Kirchoff's first law (Junction Theorem)

At a junction, the total current entering the junction is equal to the total current leaving the junction.

## Kirchoff's second law (Loop Theorem)

The net e.m.f. round a circuit is equal to the sum of the p.d.s round the loop.

| Physical Quantity | Equation |
| :--- | :--- |
| Power | $\mathrm{P}=\frac{\mathrm{W}}{\mathrm{t}}=\mathrm{VI}$ |
| Electric current | $\mathrm{I}=\frac{\mathrm{q}}{\mathrm{t}}$ |



| Work | $\mathrm{W}=\mathrm{qV}$ |
| :--- | :--- |
| Ohm's Law | $\mathrm{V}=\mathrm{IR}$ |
| Resistances in Series | $\mathrm{R}_{\mathrm{T}}=\mathrm{R}_{1}+\mathrm{R}_{2} \ldots$ |
| Resistances in Parallel | $\frac{1}{\mathrm{R}_{\mathrm{T}}}=\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}} \cdots$ |
| Magnetic flux | $\Phi=\mathrm{BA}$ |
| Electromagnetic induction | $\mathrm{Emf}=-\mathrm{N} \frac{\left(\Phi_{2}-\Phi_{1}\right)}{\mathrm{t}}$ <br> emf $=\mathrm{IVB}$ |
| Magnetic force | $\mathrm{F}=\mathrm{I} \mathbf{I} \mathrm{B}$ |

Electromagnetic spectrum


Note: 1. Shaded areas represent regions of overlap.
2. Gamma rays and X-rays occupy a common region.

### 5.2 Applied Mechanics

### 5.2.1 Newton's laws of motion

## Newton' first law of motion

The inertia of a body is the reluctance of the body to change its state of rest or motion.
Mass is a measure of inertia.

## Newton's second law of motion

$$
\mathrm{F}=\frac{\mathrm{mv}-\mathrm{mu}}{\Delta \mathrm{t}}
$$

$\mathrm{F}=\mathrm{ma}$

Impulse $=$ force $\cdot$ time $=$ change of momentum
$\mathrm{Ft}=\mathrm{mv}-\mathrm{mu}$

## Newton's third law of motion

When two objects interact, they exert equal and opposite forces on one another.
"Third-law pair" of forces act on two different bodies.

## Universal Law

$\mathrm{F}=\mathrm{Gm} \mathrm{m}_{\mathrm{p}} / \mathrm{d}^{2}$
$m_{s}$ is the mass of the sun.
$m_{p}$ is the mass of the planet.

The Universal law and the second law must be consistent

## Newton's Laws of Motion and Their Applications

| Physical Quantity | Equations |
| :--- | :--- |
| Average velocity | $\mathrm{v}_{\mathrm{av}}=\frac{\mathrm{s}}{\mathrm{t}}=\frac{\mathrm{v}+\mathrm{u}}{2}$ |
| Acceleration | $\mathrm{a}=\frac{\mathrm{v}-\mathrm{u}}{\mathrm{t}}$ |
| Momentum | $\mathrm{p}=\mathrm{mv}$ |
| Force | $\mathrm{F}=\mathrm{ma}$ |
| Weight | $\mathrm{weight}=\mathrm{mg}$ |
| Work done | $\mathrm{W}=\mathrm{Fs}$ |
| Kinetic energy | $\mathrm{E}_{\mathrm{k}}=\frac{1}{2} \mathrm{mv}{ }^{2}$ |
| Gravitational potential energy | $\mathrm{E}_{\mathrm{p}}=\mathrm{mgh}$ |
| Equations of motion | $\mathrm{a}=\frac{\mathrm{v}-\mathrm{u}}{\mathrm{t}} ;$ |


| Physical Quantity | Equations |
| :--- | :--- |
| Centripetal acceleration | $\mathrm{a}=\frac{\mathrm{v}^{2}}{\mathrm{r}}$ |
| Centripetal force | $\mathrm{F}=\mathrm{ma}=\frac{\mathrm{mv}^{2}}{\mathrm{r}}$ |
| Newton's Law of Universal Gravitation | $\mathrm{F}=\mathrm{G} \frac{\mathrm{m}_{1} \mathrm{~m}_{2}}{\mathrm{r}^{2}}$ |
| Gravitational field strength | $\mathrm{g}=\mathrm{G} \frac{\mathrm{M}}{\mathrm{r}^{2}}$ |


| Physical Quantity | Equations |
| :--- | :--- |
| Moment of a force | $\mathrm{M}=\mathrm{rF}$ |
| Principle of moments | $\sum \mathrm{M}=0$ |
| Stress | Stress $=\frac{\mathrm{F}}{\mathrm{A}}$ |

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| Strain | Strain $=\frac{\Delta \mathbf{I}}{\mathbf{I}}$ |
| :--- | :--- |
| Young's Modulus | $\mathrm{Y}=\frac{\mathrm{F} / \mathrm{A}}{\Delta \mathbf{I} / \mathbf{I}}$ |

Scalar: a property described by a magnitude only
Vector: a property described by a magnitude and a direction
Velocity: vector property equal to displacement / time

The magnitude of velocity may be referred to as speed
In SI the basic unit is $\mathrm{m} / \mathrm{s}$, in Imperial $\mathrm{ft} / \mathrm{s}$
Other common units are $\mathrm{km} / \mathrm{h}, \mathrm{mi} / \mathrm{h}$
Conversions:
$1 \mathrm{~m} / \mathrm{s}=3.28 \mathrm{ft} / \mathrm{s}$
$1 \mathrm{~km} / \mathrm{h}=0.621 \mathrm{mi} / \mathrm{h}$

Speed of sound in dry air is $331 \mathrm{~m} / \mathrm{s}$ at $0^{\circ} \mathrm{C}$ and increases by about $0.61 \mathrm{~m} / \mathrm{s}$ for each ${ }^{\circ} \mathrm{C}$ rise.

Speed of light in vacuum equals $3 \times 10^{8} \mathrm{~m} / \mathrm{s}$

Acceleration: vector property equal to change in velocity time.

In SI the basic unit is $\mathrm{m} / \mathrm{s}^{2}$
In Imperial $\mathrm{ft} / \mathrm{s}^{2}$

## Conversion:

$1 \frac{m}{s^{2}}=3.28 \frac{f t}{s^{2}}$
Acceleration due to gravity, g is $9.81 \mathrm{~m} / \mathrm{s}^{2}$

### 5.2.2 Linear Velocity and Acceleration

| Quantity | Equations |
| :--- | :--- |
| If u initial velocity and v final velocity, then displacement $s$, | $s=\left(\frac{v+u}{2}\right)$ |
| If t is the elapsed time | $s=u t+\frac{1}{2} a t^{2}$ |
| If a is the acceleration | $v^{2}=u^{2}+2 a s$ |

## Angular Velocity and Acceleration

| Quantity | Equations |
| :--- | :--- |
| $\theta$ angular displacement (radians) | $\theta=\frac{\omega_{1}+\omega_{2}}{2} \times t$ |
| $\omega$ angular velocity (radians/s); | $\theta=\omega_{1} t+\frac{1}{2} \alpha t^{2}$ |
| $\omega_{1}=$ initial, $\omega_{2}=$ final | $\omega_{2}{ }^{2}=\omega_{1}{ }^{2}+2 \alpha \theta$ |
| $\alpha$ angular acceleration (radians/s ${ }^{2}$ ) | $\mathrm{s}=\mathrm{r} \theta$ |
| Linear displacement | $\mathrm{v}=\mathrm{r} \omega$ |
| Linear velocity | $\mathrm{aT}=\mathrm{r} \alpha$ |
| Linear, or tangential acceleration |  |

## Tangential, Centripetal and Total Acceleration

| Quantity | Equations |
| :--- | :--- |
| Tangential acceleration aT is due to angular acceleration $\alpha$ | $\mathrm{aT}=\mathrm{ra}$ |
| Centripetal (Centrifugal) acceleration ac is due to change in direction only | $\mathrm{ac}=\mathrm{v}^{2} / \mathrm{r}=\mathrm{r} \omega^{2}$ |
| Total acceleration, a, of a rotating point experiencing angular acceleration <br> is the vector sum of aT and ac | $\mathrm{a}=\mathrm{aT}+\mathrm{ac}$ |

### 5.2.3 Force

Vector quantity, a push or pull which changes the shape and/or motion of an object
In SI the unit of force is the newton, N , defined as a kg m
In Imperial the unit of force is the pound lb
Conversion: $9.81 \mathrm{~N}=2.2 \mathrm{lb}$

## Weight

The gravitational force of attraction between a mass, m, and the mass of the Earth
In SI weight can be calculated from Weight $=\mathrm{F}=\mathrm{mg}$, where $\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}$
In Imperial, the mass of an object (rarely used), in slugs, can be calculated from the known weight in pounds
$m=\frac{w e i g h t}{g}$
$g=32.2 \frac{f t}{s^{2}}$

## Torque Equation

$\mathrm{T}=\mathrm{I} \alpha$ where T is the acceleration torque in $\mathrm{Nm}, \mathrm{I}$ is the moment of inertia in $\mathrm{kg} \mathrm{m}^{2}$ and $\alpha$ is the angular acceleration in radians $/ \mathrm{s}^{2}$

## Momentum

Vector quantity, symbol p ,
$\mathrm{p}=\mathrm{mv}$ [Imperial $\mathrm{p}=(\mathrm{w} / \mathrm{g}) \mathrm{v}$, where w is weight]
in SI unit is $\mathrm{kgm} / \mathrm{s}$

## Work

Scalar quantity, equal to the (vector) product of a force and the displacement of an object. In simple systems, where W is work, F force and $s$ distance
$\mathrm{W}=\mathrm{F}$ s
In SI the unit of work is the joule, J, or kilojoule, kJ
$1 \mathrm{~J}=1 \mathrm{Nm}$
In Imperial the unit of work is the $\mathrm{ft}-\mathrm{lb}$

## Energy

Energy is the ability to do work, the units are the same as for work; $\mathrm{J}, \mathrm{kJ}$, and $\mathrm{ft}-\mathrm{lb}$

## Kinetic Energy

$$
E_{R}=\frac{1}{2} m k^{2} \omega^{2}
$$

Where k is radius of gyration, $\omega$ is angular velocity in $\mathrm{rad} / \mathrm{s}$


## Kinetic Energy of Rotation

$E r=\frac{1}{2} I \omega^{2}$
Where $\mathrm{I}=\mathrm{mk}^{2}$ is the moment of inertia

### 5.2.4 Centripetal (Centrifugal) Force

$$
F_{c}=\frac{m v^{2}}{r}
$$

Where r is the radius
Where $\omega$ is angular velocity in rad/s

## Potential Energy

| Quantity | Equation |
| :--- | :--- |
| Energy due to position in a force field, such as gravity | Ep $=\mathrm{m} \mathrm{g} \mathrm{h}$ |
|  | Ep = w h |
| In Imperial this is usually expressed | Where w is weight, and h is height above <br> some specified datum |

## Thermal Energy

In SI the common units of thermal energy are J , and kJ , (and $\mathrm{kJ} / \mathrm{kg}$ for specific quantities)
In Imperial, the units of thermal energy are British Thermal Units (Btu)

## Conversions

$1 \mathrm{Btu}=1055 \mathrm{~J}$
$1 \mathrm{Btu}=778 \mathrm{ft}-\mathrm{lb}$

## Electrical Energy

In SI the units of electrical energy are J, kJ and kilowatt hours kWh . In Imperial, the unit of electrical energy is the kWh

## Conversions

$1 \mathrm{kWh}=3600 \mathrm{~kJ}$
$1 \mathrm{kWh}=3412 \mathrm{Btu}=2.66 \times 10^{6} \mathrm{ft}-\mathrm{lb}$

## Power

A scalar quantity, equal to the rate of doing work
In SI the unit is the Watt W (or kW )
$1 W=1 \frac{J}{s}$
In Imperial, the units are:
Mechanical Power - $(\mathrm{ft}-\mathrm{lb}) / \mathrm{s}$, horsepower h.p.
Thermal Power - Btu / s
Electrical Power - W, kW, or h.p.

## Conversions

$746 W=1 h . p$.

1h.p. $=550 \frac{f t-l b}{s}$
$1 k W=0.948 \frac{B t u}{s}$

## Pressure

A vector quantity, force per unit area
In SI the basic units of pressure are pascals Pa and kPa
$1 P a=1 \frac{N}{m^{2}}$
In Imperial, the basic unit is the pound per square inch, psi

## Atmospheric Pressure

At sea level atmospheric pressure equals 101.3 kPa or 14.7 psi

## Pressure Conversions

$1 \mathrm{psi}=6.895 \mathrm{kPa}$

Pressure may be expressed in standard units, or in units of static fluid head, in both SI and Imperial systems

Common equivalencies are:

- $1 \mathrm{kPa}=0.294 \mathrm{in}$. mercury $=7.5 \mathrm{~mm}$ mercury
- $1 \mathrm{kPa}=4.02 \mathrm{in}$. water $=102 \mathrm{~mm}$ water
- $1 \mathrm{psi}=2.03 \mathrm{in}$. mercury $=51.7 \mathrm{~mm}$ mercury
- $1 \mathrm{psi}=27.7 \mathrm{in}$. water $=703 \mathrm{~mm}$ water
- $1 \mathrm{~m} \mathrm{H}_{2} \mathrm{O}=9.81 \mathrm{kPa}$

Other pressure unit conversions:

- 1 bar $=14.5 \mathrm{psi}=100 \mathrm{kPa}$
- $1 \mathrm{~kg} / \mathrm{cm}^{2}=98.1 \mathrm{kPa}=14.2 \mathrm{psi}=0.981 \mathrm{bar}$
- 1 atmosphere $(\mathrm{atm})=101.3 \mathrm{kPa}=14.7 \mathrm{psi}$


## Simple Harmonic Motion

Velocity of $\mathrm{P}=\omega \sqrt{R^{2}-x^{2}} \frac{m}{s}$

### 5.2.5 Stress, Strain And Modulus Of Elasticity

Young's modulus and the breaking stress for selected materials


| Material | Young modulus | Breaking <br> stress |
| :---: | :---: | :---: |
| x 10 |  |  |
| Aluminium $\mathbf{P a}$ | $\mathbf{x ~ 1 0 ^ { 8 }} \mathbf{~ P a ~}$ |  |
| Copper | 0.70 | 2.4 |
| Brass | 1.16 | 4.9 |
| Iron (wrought) | 0.90 | 4.7 |
| Mild steel | 1.93 | 3.0 |
| Glass | 2.10 | 11.0 |
| Tungsten | 0.55 | 10 |
| Bone | 4.10 | 20 |

### 5.3 Thermodynamics

### 5.3.1 Laws of Thermodynamics

- $\mathrm{W}=\mathrm{P} \Delta \mathrm{V}$
- $\Delta \mathrm{U}=\mathrm{Q}-\mathrm{W}$
- $\mathrm{W}=\mathrm{nRT} \ln V_{\mathrm{f}} / \mathrm{V}_{\mathrm{i}}$
- $\mathrm{Q}=\mathrm{Cn} \Delta \mathrm{T}$
- $\mathrm{C}_{\mathrm{v}}=3 / 2 \mathrm{R}$
- $\mathrm{C}_{\mathrm{p}}=5 / 2 \mathrm{R}$
- $C_{p} / C_{v}=\gamma=5 / 3$
- $\mathrm{e}=1-\mathrm{Qc} / \mathrm{Q}_{\mathrm{h}}=\mathrm{W} / \mathrm{Q}_{\mathrm{h}}$
- $\mathrm{e}_{\mathrm{c}}=1-\mathrm{T}_{\mathrm{c}} / \mathrm{T}_{\mathrm{h}}$
- $\mathrm{COP}=\mathrm{Q}_{\mathrm{c}} / \mathrm{W}$ (refrigerators)
- $\mathrm{COP}=\mathrm{Q}_{\mathrm{h}} / \mathrm{W}$ (heat pumps)
- $\mathrm{Wmax}=\left(1-\mathrm{T}_{\mathrm{c}} / \mathrm{T}_{\mathrm{h}}\right) \mathrm{Q}_{\mathrm{h}}$
- $\Delta \mathrm{S}=\mathrm{Q} / \mathrm{T}$


### 5.3.2 Momentum

- $\mathrm{p}=\mathrm{mv}$
- $\Sigma \mathrm{F}=\Delta \mathrm{p} / \Delta \mathrm{t}$


### 5.3.3 Impulse

$\mathrm{I}=\mathrm{F}_{\mathrm{av}} \Delta \mathrm{t}=\mathrm{mv}_{\mathrm{f}}-\mathrm{mv}_{\mathrm{i}}$
5.3.4 Elastic and Inelastic collision

- $\mathrm{m}_{\mathrm{i}} \mathrm{v}_{1 \mathrm{i}}+\mathrm{m}_{2} \mathrm{v}_{2 \mathrm{i}}=\mathrm{m}_{1} \mathrm{v}_{1 \mathrm{f}}+\mathrm{m}_{2} \mathrm{v}_{2 \mathrm{f}}$
- $(1 / 2) \mathrm{m}_{\mathrm{i}} \mathrm{v}_{1 \mathrm{i}}{ }^{2}+(1 / 2) \mathrm{m}_{2} \mathrm{v}_{2 \mathrm{i}}{ }^{2}=1 / 2 \mathrm{~m}_{1} \mathrm{v}_{1 \mathrm{f}}{ }^{2}+1 / 2 \mathrm{~m}_{2} \mathrm{v}_{2 \mathrm{f}}{ }^{2}$
- $\mathrm{m}_{\mathrm{i}} \mathrm{v}_{1 \mathrm{i}}+\mathrm{m}_{2} \mathrm{v}_{2 \mathrm{i}}=\left(\mathrm{m}_{1}+\mathrm{m}_{2}\right) \mathrm{v}_{\mathrm{f}}$


### 5.3.5 Center of Mass

- $\mathrm{X}_{\mathrm{cm}}=\sum \mathrm{mx} / \mathrm{M}$
- $\mathrm{V}_{\mathrm{cm}}=\Sigma \mathrm{mv} / \mathrm{M}$
- $\mathrm{A}_{\mathrm{cm}}=\sum \mathrm{ma} / \mathrm{M}$
- $\mathrm{MA}_{\mathrm{cm}}=\mathrm{F}_{\text {net }}$


### 5.3.6 Angular Motion

- $\mathrm{s}=\mathrm{r} \theta$
- $\mathrm{V}_{\mathrm{t}}=\mathrm{r} \omega$
- $a_{t}=r a$
- $\mathrm{a}_{\mathrm{c}}=\mathrm{v}_{\mathrm{t}}^{2} / \mathrm{r}=\mathrm{r} \omega^{2}$
- $\omega=2 \pi / \mathrm{T}$
- $1 \mathrm{rev}=2 \pi \mathrm{rad}=360^{\circ}$

For constant $\alpha$

- $\omega=\omega_{\mathrm{o}}+\alpha \mathrm{t}$
- $\omega^{2}=\omega_{\mathrm{o}}^{2}+2 \alpha \theta$
- $\theta=\omega_{0} t+1 / 2 \alpha t^{2}$
- $\theta=\left(\omega_{\mathrm{o}}+\omega\right) \cdot \mathrm{t} / 2$
- $\mathrm{I}=\sum \mathrm{mr}^{2}$
- $\mathrm{KE}_{\mathrm{R}}=1 / 2 \mathrm{I} \omega^{2}$
- $\tau=\mathrm{rF}$
- $\quad \sum \tau=\mathrm{I} \alpha$
- $\mathrm{W}_{\mathrm{R}}=\tau \theta$
- $\mathrm{L}=\mathrm{I} \omega$
- $\Sigma \tau=\mathrm{I} \alpha$
- $\mathrm{W}_{\mathrm{R}}=\tau \theta$
- $\mathrm{L}=\mathrm{I} \omega$
- $\mathrm{L}_{\mathrm{i}}=\mathrm{L}_{\mathrm{f}}$


### 5.3.7 Conditions of Equilibrium

- $\sum \mathrm{F}_{\mathrm{x}}=0$
- $\sum \mathrm{F}_{\mathrm{y}}=0$
- $\quad \Sigma \tau=0$ (any axis)


### 5.3.8 Gravity

- $\mathrm{F}=\mathrm{Gm}_{1} \mathrm{~m}_{2} / \mathrm{r}^{2}$
- $\mathrm{T}=2 \pi / \sqrt{ } \mathrm{r}^{3} / \mathrm{GM}_{\mathrm{s}}$
- $\mathrm{G}=6.67 \times 10^{-11} \mathrm{~N}-\mathrm{m}^{2} / \mathrm{kg}^{2}$
- $g=G M_{E} / R_{E}^{2}$
- $\mathrm{PE}=-\mathrm{Gm}_{1} \mathrm{~m}_{2} / \mathrm{r}$
- $\mathrm{v}_{\mathrm{e}}=\sqrt{ } 2 \mathrm{GM}_{\mathrm{E}} / \mathrm{R}_{\mathrm{E}}$
- $\mathrm{v}_{\mathrm{s}}=\sqrt{ } \mathrm{GM}_{\mathrm{E}} / \mathrm{r}$
- $\mathrm{M}_{\mathrm{E}}=5.97 \times 10^{24} \mathrm{~kg}$
- $\mathrm{R}_{\mathrm{E}}=6.37 \times 10^{6} \mathrm{~m}$


### 5.3.9 Vibrations \& Waves

- $\mathrm{F}=-\mathrm{kx}$
- $\mathrm{PE}_{\mathrm{s}}=1 / 2 \mathrm{kx}^{2}$
- $\mathrm{x}=\mathrm{A} \cos \theta=\mathrm{A} \cos (\omega \mathrm{t})$
- $\mathrm{v}=-\mathrm{A} \omega \sin (\omega \mathrm{t})$
- $\mathrm{a}=-\mathrm{A} \omega^{2} \cos (\omega \mathrm{t})$
- $\omega=\sqrt{ } \mathrm{k} / \mathrm{m}$
- $\mathrm{f}=1 / \mathrm{T}$
- $\mathrm{T}=2 \pi \sqrt{ } \mathrm{~m} / \mathrm{k}$
- $\mathrm{E}=1 / 2 \mathrm{kA}^{2}$

- $\mathrm{T}=2 \pi \sqrt{ } \mathrm{~L} / \mathrm{g}$
- $\mathrm{v}_{\max }=\mathrm{A} \omega$
- $a_{\text {max }}=A \omega^{2}$
- $\mathrm{v}=\lambda \mathrm{fv}=\sqrt{ } \mathrm{F}_{\mathrm{T}} / \mu$
- $\mu=m / L$
- $\mathrm{I}=\mathrm{P} / \mathrm{A}$
- $\beta=10 \log \left(\mathrm{I} / \mathrm{I}_{0}\right)$
- $\mathrm{I}_{\mathrm{o}}=1 \times 10^{-12} \mathrm{~W} / \mathrm{m}^{2}$
- $\mathrm{f}^{\prime}=\mathrm{f}\left[\left(1 \pm \mathrm{v}_{0} / \mathrm{v}\right) /\left(1 \overline{\mathrm{~F}}_{\mathrm{s}} / \mathrm{v}\right)\right]$
- Surface area of the sphere $=4 \pi \mathrm{r}^{2}$
- Speed of sound waves $=343 \mathrm{~m} / \mathrm{s}$


### 5.3.10 Standing Waves

- $\mathrm{f}_{\mathrm{n}}=\mathrm{nf}_{1}$
- $\mathrm{f}_{\mathrm{n}}=\mathrm{nv} / 2 \mathrm{~L}$ (air column, string fixed both ends) $\mathrm{n}=1,2,3,4 \ldots \ldots$.
- $f_{n}=n v / 4 L$ (open at one end) $n=1,3,5,7$.


### 5.3.11 Beats

- $\mathrm{f}_{\text {beats }}=\left|\mathrm{f}_{1}-\mathrm{f}_{2}\right|$
- Fluids
- $\rho=m / V$
- $P=F / A$
- $P_{2}=P_{1}+\rho g h$
- $P_{\text {atm }}=1.01 \times 10^{5} \mathrm{~Pa}=14.7 \mathrm{lb} / \mathrm{in}^{2}$
- $\mathrm{F}_{\mathrm{B}}=\rho_{\mathrm{f}} \mathrm{Vg}=\mathrm{W}_{\mathrm{f}}$ (weight of the displaced fluid)
- $\rho_{\mathrm{o}} / \rho_{\mathrm{f}}=\mathrm{V}_{\mathrm{f}} / \mathrm{V}_{\mathrm{o}}$ (floating object)
- $\rho_{\text {water }}=1000 \mathrm{~kg} / \mathrm{m}^{3}$
- $\mathrm{W}_{\mathrm{a}}=\mathrm{W}-\mathrm{F}_{\mathrm{B}}$

Equation of Continuity: Av = constant
Bernoulli's equation: $P+1 / 2 \rho v^{2}+\rho g y=0$

### 5.3.12 Temperature and Heat

- $\mathrm{T}_{\mathrm{F}}=(9 / 5) \mathrm{T}_{\mathrm{C}}+32$
- $\mathrm{T}_{\mathrm{C}}=5 / 9\left(\mathrm{~T}_{\mathrm{F}}-32\right)$
- $\Delta \mathrm{T}_{\mathrm{F}}=(9 / 5) \Delta \mathrm{T}_{\mathrm{C}}$
- $\mathrm{T}=\mathrm{T}_{\mathrm{C}}+273.15$
- $\rho=m / v$
- $\Delta \mathrm{L}=\alpha \mathrm{L}_{0} \Delta \mathrm{~T}$
- $\Delta \mathrm{A}=\gamma \mathrm{A}_{0} \Delta \mathrm{~T}$
- $\Delta \mathrm{V}=\beta \mathrm{V}_{\mathrm{o}} \Delta \mathrm{T} \quad \beta=3 \alpha$
- $\mathrm{Q}=\mathrm{mc} \Delta \mathrm{T}$
- $\mathrm{Q}=\mathrm{mL}$
- $1 \mathrm{kcal}=4186 \mathrm{~J}$
- Heat Loss = Heat Gain
- $\mathrm{Q}=(\mathrm{kA} \Delta \mathrm{T}) \mathrm{t} / \mathrm{L}$,
- $\mathrm{H}=\mathrm{Q} / \mathrm{t}=(\mathrm{kA} \Delta \mathrm{T}) / \mathrm{L}$
- $\mathrm{Q}=e \sigma \mathrm{~T}^{4} \mathrm{At}$
- $\mathrm{P}=\mathrm{Q} / \mathrm{t}$
- $P=\sigma A e T^{4}$
- $\mathrm{P}_{\text {net }}=\sigma \operatorname{Ae}\left(\mathrm{T}^{4}-\mathrm{T}_{\mathrm{s}}{ }^{4}\right)$
- $\sigma=5.67 \times 10^{-8} \mathrm{~W} / \mathrm{m}^{2} \mathrm{~K}^{4}$


### 5.3.13 Ideal Gases

- $\mathrm{PV}=\mathrm{nRT}$
- $\mathrm{R}=8.31 \mathrm{~J} / \mathrm{mol} \mathrm{K}$
- $\mathrm{PV}=\mathrm{NkT}$
- $\mathrm{N}_{\mathrm{A}}=6.02 \times 10^{23}$ molecules $/ \mathrm{mol}$
- $\mathrm{k}=1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}$
- $\mathrm{M}=\mathrm{N}_{\mathrm{A}} \mathrm{m}$
- $(\mathrm{KE})_{\mathrm{av}}=\left(1 / 2 \mathrm{mv}^{2}\right)_{\mathrm{av}}=3 / 2 \mathrm{kT}$
- $\mathrm{U}=3 / 2 \mathrm{NkT}=3 / 2 \mathrm{nRT}$


### 5.3.14 Elastic Deformation

- $P=F / A$
- $\mathrm{Y}=\mathrm{FL}_{\mathrm{o}} / \mathrm{A} \Delta \mathrm{L}$
- $\mathrm{S}=\mathrm{Fh} / \mathrm{A} \Delta \mathrm{x}$
- $B=-V_{0} \Delta F / A \Delta V$
- Volume of the sphere $=4 \pi r^{3} / 3$
- $1 \mathrm{~atm}=1.01 \times 10^{5} \mathrm{~Pa}$


### 5.3.15 Temperature Scales

- ${ }^{\circ} \mathrm{C}=5 / 9\left({ }^{\circ} \mathrm{F}-32\right)$
- ${ }^{\circ} \mathrm{F}=(9 / 5){ }^{\circ} \mathrm{C}+32$
- ${ }^{\circ} \mathrm{R}={ }^{\circ} \mathrm{F}+460$ ( R Rankine)
- $\mathrm{K}={ }^{\circ} \mathrm{C}+273$ (K Kelvin)


### 5.3.16 Sensible Heat Equation

- $\mathrm{Q}=\mathrm{mc} \Delta \mathrm{T}$
- $\mathrm{M}=$ mass
- $\mathrm{C}=$ specific heat
- $\Delta \mathrm{T}=$ temperature chance


### 5.3.17 Latent Heat

- Latent heat of fusion of ice $=335 \mathrm{~kJ} / \mathrm{kg}$
- Latent heat of steam from and at $100^{\circ} \mathrm{C}=2257 \mathrm{~kJ} / \mathrm{kg}$
- 1 tonne of refrigeration $=335000 \mathrm{~kJ} /$ day $=233 \mathrm{~kJ} / \mathrm{min}$


### 5.3.18 Gas Laws

## Boyle's Law

When gas temperature is constant
$\mathrm{PV}=$ constant or
$\mathrm{P}_{1} \mathrm{~V}_{1}=\mathrm{P}_{2} \mathrm{~V}_{2}$
Where P is absolute pressure and V is volume

## Charles' Law

When gas pressure is constant,
$\frac{V}{T}=$ cons .
or


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$\frac{V_{1}}{T_{1}}=\frac{V_{2}}{T_{2}}$
where V is volume and T is absolute temperature

## Gay-Lussac's Law

When gas volume is constant,
$\frac{P}{T}=$ const.
or
$\frac{P_{1}}{T_{1}}=\frac{P_{2}}{T_{2}}$
where P is absolute pressure and T is absolute temperature

## General Gas Law

$\frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}}=$ const .
$\mathrm{P} V=\mathrm{m} R \mathrm{~T}$ where $\mathrm{P}=$ absolute pressure $(\mathrm{kPa})$
$\mathrm{V}=$ volume $\left(\mathrm{m}^{3}\right)$
$\mathrm{T}=$ absolute temp $(\mathrm{K})$
$\mathrm{m}=$ mass (kg)
$\mathrm{R}=$ characteristic constant $(\mathrm{kJ} / \mathrm{kgK})$

Also
$\mathrm{PV}=\mathrm{nRoT}$ where $\mathrm{P}=$ absolute pressure $(\mathrm{kPa})$
$\mathrm{V}=$ volume $\left(\mathrm{m}^{3}\right)$
$\mathrm{T}=$ absolute temperature K
$\mathrm{N}=$ the number of kmoles of gas
Ro $=$ the universal gas constant $8.314 \mathrm{~kJ} / \mathrm{kmol} / \mathrm{K}$

### 5.3.19 Specific Heats Of Gases

| GAS | Specific Heat at Constant Pressure $\mathrm{kJ} / \mathrm{kgK} \text { or } \mathrm{kJ} / \mathrm{kg}^{\circ} \mathrm{C}$ | Specific Heat at Constant Volume <br> $\mathrm{kJ} / \mathrm{kgK}$ or $\mathrm{kJ} / \mathrm{kg}{ }^{\circ} \mathrm{C}$ | Ratio of Specific $\gamma=c p / c v$ |
| :---: | :---: | :---: | :---: |
| Air | 1.005 | 0.718 | 1.40 |
| Ammonia | 2.060 | 1.561 | 1.32 |
| Carbon Dioxide | 0.825 | 0.630 | 1.31 |
| Carbon Monoxide | 1.051 | 0.751 | 1.40 |
| Helium | 5.234 | 3.153 | 1.66 |
| Hydrogen | 14.235 | 10.096 | 1.41 |
| Hydrogen Sulphide | 1.105 | 0.85 | 1.30 |
| Methane | 2.177 | 1.675 | 1.30 |
| Nitrogen | 1.043 | 0.745 | 1.40 |
| Oxygen | 0.913 | 0.652 | 1.40 |
| Sulphur Dioxide | 0.632 | 0.451 | 1.40 |

### 5.3.20 Efficiency of Heat Engines

## Carnot Cycle

$\eta=\frac{T_{1}-T_{2}}{T_{1}}$
where $T_{1}$ and $T_{2}$ are absolute temperatures of heat source and sink

## Air Standard Efficiencies

Spark Ignition Gas and Oil Engines (Constant Volume Cycle)
$\eta=1-\frac{1}{r_{v}{ }^{(\gamma-1)}}$
$\mathrm{r}_{\mathrm{v}}=$ compression ratio
$\gamma=$ specific heat (constant pressure) / Specific heat (constant volume)

## Diesel Cycle

$$
\eta=1-\frac{R \gamma-1)}{{r_{v}}^{\gamma-1} \gamma(R-1)}
$$

Where $\mathrm{r}=$ ratio of compression
$R=$ ratio of cut-off volume to clearance volume

## High Speed Diesel (Dual-Combustion) Cycle

$\eta=1 \frac{k \beta^{\gamma}-1}{r_{v}^{\gamma-1}[(k-1)+\gamma k(\beta-1)]}$
Where $\mathrm{r}_{\mathrm{v}}=$ cylinder volume / clearance volume
$\mathrm{k}=$ absolute pressure at the end of constant V heating (combustion) / absolute pressure at the beginning of constant
V combustion
$\beta=$ volume at the end of constant $P$ heating (combustion) / clearance volume

## Gas Turbines (Constant Pressure or Brayton Cycle)

$$
\eta=1-\frac{1}{r_{p}\left(\frac{\gamma-1}{\gamma}\right)}
$$

where $\mathrm{r}_{\mathrm{p}}=$ pressure ratio $=$ compressor discharge pressure $/$ compressor intake pressure

### 5.3.21 Heat Transfer by Conduction

| Material | Coefficient of Thermal <br> Conductivity <br> $\mathbf{W} / \mathbf{m}{ }^{\circ} \mathrm{C}$ |
| :---: | :---: |
| Air | 0.025 |
| Brass | 104 |

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| Material | Coefficient of Thermal <br> Conductivity <br> W/m |
| :---: | :---: |
| ${ }^{\circ} \mathbf{C}$ |  |$|$| Concrete | 0.85 |
| :---: | :---: |
| Cork | 0.043 |
| Glass | 70 |
| Iron, cast | 60 |
| Steel | 0.076 |
| Wallboard, paper | 206 |
| Aluminum | 0.6 |
| Brick | 380 |
| Copper | 0.038 |
| Felt | 0.04 |
| Glass, fibre | 0.04 |
| Plastic, cellular | 0.15 |
| Wood |  |
|  |  |
|  |  |
|  |  |

### 5.3.22 Thermal Expansion of Solids

Increase in length $=\mathrm{L} \alpha\left(\mathrm{T}_{2}-\mathrm{T}_{1}\right)$
Where $\mathrm{L}=$ original length
$\alpha=$ coefficient of linear expansion
$\left(\mathrm{T}_{2}-\mathrm{T}_{1}\right)=$ rise in temperature
Increase in volume $=\mathrm{V} \beta\left(\mathrm{T}_{2}-\mathrm{T}_{1}\right)$
Where $\mathrm{V}=$ original volume
$\beta=$ coefficient of volumetric expansion
$\left(\mathrm{T}_{2}-\mathrm{T}_{1}\right)=$ rise in temperature
Coefficient of volumetric expansion $=$ Coefficient of linear expansion $\times 3$
$\beta=3 \alpha$

### 5.3.23 Chemical Heating Value of a Fuel

Chemical Heating Value MJ per kg of fuel $=33.7 \mathrm{C}+144\left(\mathrm{H}_{2}-\frac{\mathrm{O}_{2}}{8}\right)+9.3 \mathrm{~S}$
C is the mass of carbon per kg of fuel
$\mathrm{H}_{2}$ is the mass of hydrogen per kg of fuel
$\mathrm{O}_{2}$ is the mass of oxygen per kg of fuel
S is the mass of sulphur per kg of fuel

## Theoretical Air Required to Burn Fuel

$$
\text { Air }(\mathrm{kg} \text { per kg of fuel })=\left[\frac{8}{3} C+8\left(H_{2}-O_{2}\right)+S\right] \frac{100}{23}
$$

## Air Supplied from Analysis of Flue Gases

$$
\text { Air in kg per kg of fuel }=\frac{N_{2}}{33\left(\mathrm{CO}_{2}+\mathrm{CO}\right)} \times C
$$

## Boiler Formulae

$$
\text { Equivalent evaporation } \frac{m_{s}\left(h_{1}-h_{2}\right)}{2257 \mathrm{kj} / \mathrm{kg}}
$$

$$
\text { Factor of evaporation } \frac{\left(h_{1}-h_{2}\right)}{2257 \mathrm{kj} / \mathrm{kg}}
$$

## Boiler Efficiency

$$
\frac{m_{s}\left(h_{1}-h_{2}\right)}{m f \times(\text { calorificvalue })}
$$

Where
$\mathrm{m}_{\mathrm{s}}=$ mass flow rate of steam
$h_{1}=$ enthalpy of steam produced in boiler
$h_{2}=$ enthalpy of feedwater to boiler
$m_{f}=$ mass flow rate of fuel

| Name of process | Value of $n$ | P-V-T Relationships |  |  | Heat added | Work done | Change in <br> Internal <br> Energy | Change in <br> Enthalpy | Change in <br> Entropy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | P-V | T-P | T-V |  |  |  |  |  |
| Constant Volume | $\infty$ | -- | $\frac{T_{1}}{T_{2}}=\frac{P_{1}}{P_{2}}$ | -- | $m c_{v}\left(T_{2}-T_{1}\right)$ | 0 | $m c_{v}\left(T_{2}-T_{1}\right)$ | $m c_{p}\left(T_{2}-T_{1}\right)$ | $m c_{v} \log _{e}\left(\frac{T_{2}}{T_{1}}\right)$ |
| Constant pressure | 0 | -- | -- | $\frac{T_{1}}{T_{2}}=\frac{V_{1}}{V_{2}}$ | $m c_{p}\left(T_{2}-T_{1}\right)$ | $\mathrm{P}\left(\mathrm{V}_{2}-\mathrm{V}_{1}\right)$ | $m c_{v}\left(T_{2}-T_{1}\right)$ | $m c_{p}\left(T_{2}-T_{1}\right)$ | $m R \log _{e}\left(\frac{P_{1}}{P_{2}}\right)$ |
| $\mathrm{P}=$ Pressure |  |  |  |  |  |  |  |  |  |


| Isothermal <br> T=Constant | 1 | $\frac{P_{1}}{P_{2}}=\frac{V_{2}}{V_{1}}$ | -- | -- | $m R T \log _{e}\left(\frac{P_{1}}{P_{2}}\right)$ | ${ }^{2} R T \log _{e}\left(\frac{P_{1}}{P_{2}}\right)$ | 0 | 0 | $m R \log _{e}\left(\frac{P_{1}}{P_{2}}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Isentropic S=Constant | $\gamma$ | $\frac{P_{1}}{P_{2}}=\left[\frac{V_{2}}{V_{1}}\right]^{*}$ | $\frac{T_{1}}{T_{2}}=\left[\frac{P_{1}}{P_{2}}\right]^{\frac{\gamma-1}{\gamma}}$ | $\frac{T_{1}}{T_{2}}=\left[\frac{V_{2}}{V_{1}}\right]^{\gamma-1}$ | 0 | $m c_{v}\left(T_{1}-T_{2}\right)$ | $m c_{v}\left(T_{2}-T_{1}\right)$ | $m c_{p}\left(T_{2}-T_{1}\right)$ | 0 |
| Polytropic $P V^{\mathrm{n}}=$ <br> Constant | n | $\frac{P_{1}}{P_{2}}=\left[\frac{V_{2}}{V_{1}}\right]^{n}$ | $\frac{T_{1}}{T_{2}}=\left[\frac{P_{1}}{P_{2}}\right]^{\frac{n-1}{n}}$ | $\frac{T_{1}}{T_{2}}=\left[\frac{V_{2}}{V_{1}}\right]^{n-1}$ | $m c_{n}\left(T_{2}-T_{1}\right)$ | $\frac{m R}{n-1}\left(T_{1}-T_{2}\right)$ | $m c_{v}\left(T_{2}-T_{1}\right)$ | $m c_{p}\left(T_{2}-T_{1}\right)$ | $m c_{n} \log _{e}\left(\frac{T_{2}}{T_{1}}\right)$ |

Thermodynamic Equations for perfect gases
*Can be used for reversible adiabatic processes
$c_{v}=$ Specific heat at constant volume, $\mathrm{kJ} / \mathrm{kgK}$
$c_{p}=$ Specific heat at constant pressure, $\mathrm{kJ} / \mathrm{kgK}$
$\mathrm{c}_{\mathrm{m}}=$ Specific heat for polytropic process $=c_{v}\left(\frac{\gamma-n}{1-n}\right) k J / k g K$
H = Enthalpy, kJ
$\gamma=$ Isentropic Exponent, $\mathrm{c}_{\mathrm{p}} / \mathrm{c}_{\mathrm{v}}$
$\mathrm{n}=$ polytropic exponent
$\mathrm{P}=$ Pressure, kPa

$\mathrm{R}=$ Gas content, $\mathrm{kJ} / \mathrm{kgK}$
S = Entropy, kJ/K
$\mathrm{T}=$ Absolute Temperature, $\mathrm{K}=273+{ }^{\circ} \mathrm{C}$
$\mathrm{U}=$ Internal Energy, kJ
$\mathrm{V}=$ Volume, $\mathrm{m}^{3}$
$\mathrm{m}=$ Mass of gas, kg

| Specific Heat and Linear <br> Expansion of Solids | $\begin{aligned} & \text { Mean Specific Heat between } 0 \\ & { }^{\circ} \mathrm{C} \\ & \text { and } 100{ }^{\circ} \mathrm{C} \mathrm{~kJ} / \mathrm{kgK} \text { or } \mathrm{kJ} / \mathrm{kg}{ }^{\circ} \mathrm{C} \end{aligned}$ | Coefficient of Linear Expansion between $\begin{aligned} & 0^{\circ} \mathrm{C} \text { and } 100{ }^{\circ} \mathrm{C} \\ & \left(\text { multiply by } 10^{-6}\right. \text { ) } \end{aligned}$ |
| :---: | :---: | :---: |
| Aluminum | 0.909 | 23.8 |
| Antimony | 0.209 | 17.5 |
| Bismuth | 0.125 | 12.4 |
| Brass | 0.383 | 18.4 |
| Carbon | 0.795 | 7.9 |
| Cobalt | 0.402 | 12.3 |
| Copper | 0.388 | 16.5 |
| Glass | 0.896 | 9.0 |
| Gold | 0.130 | 14.2 |
| $\text { Ice (between }-20{ }^{\circ} \mathrm{C} \text { \& } 0{ }^{\circ} \mathrm{C} \text { ) }$ | 2.135 | 50.4 |
| Iron (cast) | 0.544 | 10.4 |
| Iron (wrought) | 0.465 | 12.0 |
| Lead | 0.131 | 29.0 |
| Nickel | 0.452 | 13.0 |
| Platinum | 0.134 | 8.6 |
| Silicon | 0.741 | 7.8 |
| Silver | 0.235 | 19.5 |
| Steel (mild) | 0.494 | 12.0 |
| Tin | 0.230 | 26.7 |
| Zinc | 0.389 | 16.5 |

## Specific Heat and Volume Expansion for Liquids

| Liquid | Specific Heat $\begin{aligned} & \text { (at } 20{ }^{\circ} \mathrm{C} \text { ) } \\ & \text { KJ/kgK or } \mathrm{kJ} / \mathrm{kg}{ }^{\circ} \mathrm{C} \end{aligned}$ | Coefficient of Volume Expansion <br> (Multiply by $10^{-4}$ ) |
| :---: | :---: | :---: |
| Alcohal | 2.470 | 11.0 |
| Ammonia | 0.473 |  |
| Benzine | 1.138 | 12.4 |
| Carbon Dioxide | 3.643 | 1.82 |
| Mercury | 0.139 | 1.80 |
| Olive oil | 1.633 |  |
| Petroleum | 2.135 |  |
| Gasoline | 2.093 | 12.0 |
| Turpentine | 1.800 | 9.4 |
| Water | 4.183 | 3.7 |

### 5.4 Fluid Mechanics

### 5.4.1 Discharge from an Orifice

| Let $\mathrm{A}=$ cross-sectional area of the orifice $=$ | $\frac{\pi}{4} d^{2}$ |
| :--- | :--- |
| And $\mathrm{Ac}=$ cross-sectional area of the jet at the vena conrtacta | $\frac{\pi}{4} d_{c}{ }^{2}$ |
| Then $\mathrm{Ac}=\mathrm{CcA}$ | $C_{c}=\frac{A_{c}}{A}=\left(\frac{d_{c}}{d}\right)^{2}$ |

Where $C_{c}$ is the coefficient of contraction


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At the vena contracta, the volumetric flow rate Q of the fluid is given by

- $\mathrm{Q}=$ area of the jet at the vena contracta $\cdot$ actual velocity $=\mathrm{A}_{\mathrm{c}} \mathrm{V}$
- Or $Q=C_{c} A C_{v} \sqrt{2 g h}$
- Typically, values for Cd vary between 0.6 and 0.65
- Circular orifice: $\mathrm{Q}=0.62 \mathrm{~A} \sqrt{ } 2 \mathrm{gh}$
- Where $\mathrm{Q}=$ flow $\left(\mathrm{m}^{3} / \mathrm{s}\right) \mathrm{A}=\operatorname{area}\left(\mathrm{m}^{2}\right) \mathrm{h}=$ head $(\mathrm{m})$
- Rectangular notch: $\mathrm{Q}=0.62(\mathrm{~B} \cdot \mathrm{H}) 2 / 3 \sqrt{ } 2 \mathrm{gh}$

Where B = breadth (m)
$\mathrm{H}=$ head (m above sill)
Triangular Right Angled Notch: $\mathrm{Q}=2.635 \mathrm{H}^{5 / 2}$
Where $\mathrm{H}=$ head ( m above sill)

### 5.4.2 Bernoulli's Theory

$H=h+\frac{P}{w}+\frac{v^{2}}{2 g}$
$\mathrm{H}=$ total head (meters)
$\mathrm{w}=$ force of gravity on $1 \mathrm{~m}^{3}$ of fluid $(\mathrm{N})$
$\mathrm{h}=$ height above datum level (meters)
$\mathrm{v}=$ velocity of water (meters per second)
$\mathrm{P}=$ pressure ( $\mathrm{N} / \mathrm{m}^{2}$ or Pa )
Loss of Head in Pipes Due to Friction

Loss of head in meters $=f \frac{L}{d} \frac{v^{2}}{2 g}$
$\mathrm{L}=$ length in meters
$\mathrm{v}=$ velocity of flow in meters per second
$\mathrm{d}=$ diameter in meters
$\mathrm{f}=$ constant value of 0.01 in large pipes to 0.02 in small pipes

### 5.4.3 Actual pipe dimensions

| Nominal pipe size <br> $(\mathrm{in})$ | Outside diameter <br> $(\mathbf{m m})$ | Inside diameter <br> $(\mathbf{m m})$ | Wall thickness <br> $(\mathbf{m m})$ | Flow area ( $\left.\mathbf{m}^{2}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $1 / 8$ | 10.3 | 6.8 | 1.73 | $3.660 \times 10^{-5}$ |
| $1 / 4$ | 13.7 | 9.2 | 2.24 | $6717 \times 10^{-5}$ |
| $3 / 8$ | 17.1 | 12.5 | 2.31 | $1.236 \times 10^{-4}$ |
| $1 / 2$ | 21.3 | 15.8 | 2.77 | $1.960 \times 10^{-4}$ |


| Nominal pipe size (in) | Outside diameter (mm) | Inside diameter (mm) | Wall thickness (mm) | Flow area ( $\mathrm{m}^{2}$ ) |
| :---: | :---: | :---: | :---: | :---: |
| 3/4 | 26.7 | 20.9 | 2.87 | $3.437 \times 10^{-4}$ |
| 1 | 33.4 | 26.6 | 3.38 | $5.574 \times 10^{-4}$ |
| $11 / 4$ | 42.2 | 35.1 | 3.56 | $9.653 \times 10^{-4}$ |
| $11 / 2$ | 48.3 | 40.9 | 3.68 | $1.314 \times 10^{-3}$ |
| 2 | 60.3 | 52.5 | 3.91 | $2.168 \times 10^{-3}$ |
| $2^{1 / 2}$ | 73.0 | 62.7 | 5.16 | $3.090 \times 10^{-3}$ |
| 3 | 88.9 | 77.9 | 5.49 | $4.768 \times 10^{-3}$ |
| $31 / 2$ | 101.6 | 90.1 | 5.74 | $6.381 \times 10^{-3}$ |
| 4 | 114.3 | 102.3 | 6.02 | $8.213 \times 10^{-3}$ |
| 5 | 141.3 | 128.2 | 6.55 | $1.291 \times 10^{-2}$ |
| 6 | 168.3 | 154.1 | 7.11 | $1.864 \times 10^{-2}$ |
| 8 | 219.1 | 202.7 | 8.18 | $3.226 \times 10^{-2}$ |
| 10 | 273.1 | 254.5 | 9.27 | $5.090 \times 10^{-2}$ |
| 12 | 323.9 | 303.2 | 10.31 | $7.219 \times 10^{-2}$ |
| 14 | 355.6 | 333.4 | 11.10 | $8.729 \times 10^{-2}$ |
| 16 | 406.4 | 381.0 | 12.70 | 0.1140 |
| 18 | 457.2 | 428.7 | 14.27 | 0.1443 |
| 20 | 508.0 | 477.9 | 15.06 | 0.1794 |
| 24 | 609.6 | 574.7 | 17.45 | 0.2594 |

## 6 References

### 6.1 Periodic Table of Elements

| A |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 8A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 18 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2 |
| H | 2 A |  |  |  |  |  |  |  |  |  |  | 3A | 4A | 5A | 6 A | 7A | He |
| 1.00 | 2 |  |  |  |  |  |  |  |  |  |  | 13 | 14 | 15 | 16 | 17 | 4.00 |
| 8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 3 |
| 3 | 4 |  |  |  |  |  |  |  |  |  |  | 5 | 6 | 7 | 8 | 9 | 10 |
| Li | Be |  |  |  |  |  |  |  |  |  |  | B | C | N | O | F | Ne |
| 6.94 | 9.01 |  |  |  |  |  |  |  |  |  |  | 10.8 | 12.0 | 14.0 | 16.0 | 19.0 | 20.1 |
| 1 | 2 |  |  |  |  |  |  |  |  |  |  | 1 | 1 | 1 | 0 | 0 | 8 |
| 11 | 12 |  |  |  |  |  |  |  |  |  |  | 13 | 14 | 15 | 16 | 17 | 18 |
| Na | Mg | 3B | 4B | 5B | 6B | 7B | 8B | 8B | 8B | 1B | 2B | Al | Si | P | S | Cl | Ar |
| 22.9 | 24.3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 26.9 | 28.0 | 30.9 | 32.0 | 35.4 | 39.9 |
| 9 | 1 |  |  |  |  |  |  |  |  |  |  | 8 | 9 | 7 | 7 | 5 | 5 |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| K | Ca | Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr |
| 39.1 | 40.0 | 44.9 | 47.9 | 50.9 | 52.0 | 54.9 | 55.8 | 58.9 | 58.7 | 63.5 | 65.3 | 69.7 | 72.5 | 74.9 | 78.9 | 79.9 | 83.8 |
| 0 | 8 | 6 | 0 | 4 | 0 | 4 | 5 | 3 | 0 | 5 | 8 | 2 | 9 | 2 | 6 | 0 | 0 |
| 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| Rb | Sr | Y | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I | Xe |
| 85.4 | 87.6 | 88.9 | 91.2 | 92.9 | 95.9 | 97.9 | 101. | 102. | 106. | 107. | 112. | 114. | 118. | 121. | 127. | 126. | 131. |
| 7 | 2 | 1 | 2 | 1 | 4 |  | 1 | 9 | 4 | 9 | 4 | 8 | 7 | 8 | 6 | 9 | 3 |
| 55 | 56 | 57 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 |
| Cs | Ba | La | Hf | Ta | W | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn |
| 132. | 137. | 138. | 178. | 180. | 183. | 186. | 190. | 192. | 195. | 197. | 200. | 204. | 207. | 209. | (209) | (210) | (222) |
| 9 | 3 | 9 | 5 | 9 | 8 | 2 | 2 | 2 | 1 | 0 | 6 | 4 | 2 | 0 |  |  |  |
| 87 | 88 | 89 | 104 | 105 | 106 | 107 | 108 | 109 |  |  |  |  |  |  |  |  |  |
| Fr | Ra | Ac | Rf | Db | Sg | Bh | Hs | Mt |  |  |  |  |  |  |  |  |  |
| (223) | 226. | 227. | (261) | (262) | (266) | (264) | (265) | (268) |  |  |  |  |  |  |  |  |  |
|  | 0 | 0 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ce | Pr | Nd | Pm | Sm | Eu | Gd | Tb | Dy | Ho | Er | Tm | Yb | Lu |
| 140. | 140. | 144. | $(145)$ | 150. | 152. | 157. | 158. | 162. | 164. | 167. | 168. | 173. | 175. |
| 1 | 9 | 2 |  | 4 | 0 | 3 | 9 | 5 | 9 | 3 | 9 | 0 | 0 |
| 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | 101 | 102 | 103 |
| Th | Pa | U | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr |
| 232. | 231. | 238. | 237. | $(244)$ | $(243)$ | $(247)$ | $(247)$ | $(251)$ | $(252)$ | $(257)$ | $(258)$ | $(259)$ | $(262)$ |
| 0 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |

### 6.2 Resistor Color Coding

| Color | Value |
| :--- | :--- |
| Black | 0 |
| Brown | 1 |
| Red | 2 |
| Orange | 3 |
| Yellow | 4 |
| Green | 5 |
| Blue | 6 |
| Violet / Purple | 7 |
| Grey | 8 |
| White | 9 |

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